A high-redshift calibration of the [O I]-to-H I conversion factor in star-forming galaxies

Wilson, Sophia N.; Heintz, Kasper E.; Jakobsson, Páll; Madden, Suzanne C.; Watson, Darach; Magdis, Georgios; Valentino, Francesco; Greve, Thomas R.; Vizgan, David

Published in:
Astronomy & Astrophysics

DOI:
10.1051/0004-6361/202346878

Publication date:
2024

Document version
Publisher's PDF, also known as Version of record

Document license:
CC BY

Citation for published version (APA):
A high-redshift calibration of the [O I]-to-H I conversion factor in star-forming galaxies

Sophia N. Wilson\textsuperscript{1,2}, Kasper E. Heintz\textsuperscript{1,2}, Páll Jakobsson\textsuperscript{3}, Suzanne C. Madden\textsuperscript{4}, Darach Watson\textsuperscript{1,2}, Georgios Magdis\textsuperscript{1,2,5}, Francesco Valentino\textsuperscript{1,6}, Thomas R. Greve\textsuperscript{1,5}, and David Vizgian\textsuperscript{7}

1 Cosmic Dawn Center (DAWN), Denmark
2 Niels Bohr Institute, University of Copenhagen, Jagtvej 128, 2200 Copenhagen N, Denmark
e-mail: sophia.wilson@nbi.ku.dk; keheintz@nbi.ku.dk
3 Centre for Astrophysics and Cosmology, Science Institute, University of Iceland, Dunhagi 5, 107 Reykjavik, Iceland
4 AIM, CEA, CNRS, Université Paris-Saclay, Université Paris Diderot, Sorbonne Paris Cité, 91191 Gif-sur-Yvette, France
5 DTU-Space, Technical University of Denmark, Elektrovej 327, 2800 Kgs. Lyngby, Denmark
6 European Southern Observatory, Karl-Schwarzschild-Str. 2, 85748 Garching bei Munchen, Germany
7 Department of Astronomy, University of Illinois, 1002 West Green St., Urbana, IL 61801, USA

Received 12 May 2023 / Accepted 21 December 2023

ABSTRACT

The assembly and build-up of neutral atomic hydrogen (H I) in galaxies is one of the most fundamental processes in galaxy formation and evolution. Studying this process directly in the early universe is hindered by the weakness of the hyperfine 21-cm H I line transition, impeding direct detections and measurements of the H I gas masses (\(M_{\text{HI}}\)). Here we present a new method to infer \(M_{\text{HI}}\) of high-redshift galaxies using neutral, atomic oxygen as a proxy. Specifically, we derive metallicity-dependent conversion factors relating the far-infrared [O I]-63 \(\mu\)m and [O I]-145 \(\mu\)m emission line luminosities and \(M_{\text{HI}}\) in star-forming galaxies at \(z \approx 2–6\) using gamma-ray bursts (GRBs) as probes. We calibrate the [O I]-to-H I conversion factor relying on a sample of local galaxies with direct measurements of \(M_{\text{HI}}\) and [O I]-63 \(\mu\)m and [O I]-145 \(\mu\)m line luminosities in addition to the SAGE hydrodynamical simulation framework at similar epochs (\(z \approx 0\)). We find that the \([\text{O I}]_{63\mu m} - \text{to-} \text{H I}\) and \([\text{O I}]_{145\mu m} - \text{to-} \text{H I}\) conversion factors, here denoted \(\beta_{[\text{O I}] - \text{H I}}\) and \(\beta_{[\text{O I}] - \text{H I}}\) respectively, universally appear to be anti-correlated with the gas-phase metallicity. The GRB measurements further predict a mean ratio of \(L_{\text{[O I]}-63\mu m}/L_{\text{[O I]}-145\mu m} = 1.55 \pm 0.12\) and reveal generally less excited [C II] over [O I] compared to the local galaxy sample. The \(z \approx 0\) galaxy sample also shows systematically higher \(\beta_{[\text{O I}] - \text{H I}}\) and \(\beta_{[\text{O I}] - \text{H I}}\) conversion factors than the GRB sample, indicating either suppressed [O I] emission in local galaxies likely due to their lower hydrogen densities or more extended, diffuse H I gas reservoirs traced by the H I 21-cm. Finally, we apply these empirical calibrations to the few detections of [O I]-63 \(\mu\)m and [O I]-145 \(\mu\)m line transitions at \(z \approx 2\) from the literature and further discuss the applicability of these conversion factors to probe the H I gas content in the dense, star-forming interstellar medium (ISM) of galaxies well into the epoch of reionization.

Key words. gamma-ray burst: general – ISM: abundances – galaxies: abundances – galaxies: high-redshift

1. Introduction

The neutral, atomic hydrogen (H I) content of galaxies in the early universe is one of the most fundamental ingredients in the overall process of galaxy formation and evolution (Kereš et al. 2005; Schaye et al. 2010; Dayal & Ferrara 2018). Constraining the abundance of H I in galaxies provides valuable insight into the accretion rate of neutral pristine gas from the intergalactic medium onto galaxy halos and the available gas fuel that can form molecules and subsequently stars. The H I gas mass can be inferred through the hyperfine H I 21-cm transition in local, massive galaxies (Zwaan et al. 2005; Walter et al. 2008; Hoppmann et al. 2015; Jones et al. 2018; Catinella et al. 2018), but due to the weakness of the transition this is only feasible out to \(z \approx 0.5\) for individual sources (Fernández et al. 2016; Maddox et al. 2021). Recent efforts have pushed this out to \(z \approx 1\) by measuring the combined 21-cm signal from a stack of several thousand galaxies (Chowdhury et al. 2020) or detected in one particular strongly lensed galaxy (Chakraborty & Roy 2023). Strong integrated H I column densities in galaxy sightlines have also been inferred at \(z \approx 9\) with the James Webb Space Telescope (JWST; Heintz et al. 2023c). However, to probe and study the total neutral gas reservoirs of these distant galaxies, an alternative probe of H I in emission is required.

A similar observational challenge has been encountered in the study of the molecular gas reservoirs of high-redshift galaxies (see e.g., Bolatto et al. 2013; Carilli & Walter 2013, for reviews). Molecular clouds are predominantly comprised of molecular hydrogen H$_2$, but the electronic transitions of H$_2$ are only excited at high temperatures (\(T \approx 10^4\) K), much warmer than the typical temperatures observed in the cold, molecular gas phase (\(T \approx 20–30\) K; Weiß et al. 2003; Glover & Smith 2016). To circumvent this limitation, carbon monoxide (CO) or neutral-atomic carbon ([C I]) has been used as physical tracers of H$_2$ to determine the molecular gas mass of high-redshift galaxies (Tacconi et al. 2010, 2013; Walter et al. 2011; Magdis et al. 2012; Genzel et al. 2015; Valentino et al. 2018; Crocker et al. 2019; Heintz & Watson 2020). Since CO and [C I] can only be shielded from the UV radiation field of the interstellar medium (ISM) by abundant H$_2$ molecules, these tracers are uniquely linked to molecular gas. Measuring the relative abundance of CO- or [C I]-to-H$_2$ in these molecular clouds thus enables estimates of the expected molecular gas mass from these tracers (Bolatto et al. 2013).
To infer the neutral atomic gas mass of high-redshift galaxies, we thus have an incentive to establish a similar proxy for H1. The [CII]-158 µm line transition is one of the strongest ISM cooling lines and likely a robust tracer of H1, as the ionization potential of neutral carbon (11.26 eV) is below that of neutral hydrogen (13.6 eV). Carbon is thus expected to primarily be in the singly ionized state in the neutral ISM. Moreover, extended [CII] emission has been observed spatially coincident with H1 21-cm emission in nearby galaxies (Madden et al. 1993, 1997) and has been shown observationally to predominantly originate from the neutral gas phase of the ISM (Pineda et al. 2014; Croxall et al. 2017; Cormier et al. 2019; Tarantino et al. 2021). Simulations (Francke et al. 2018; Olsen et al. 2021; Ramos Padilla et al. 2021) and semi-analytical models (SAMs; Vallini et al. 2015, 2017; Lagache et al. 2018; Popping et al. 2016, 2019; Ferrara et al. 2019), however, have not yet converged on the actual fraction of [CII] originating from atomic, molecular or photo-dissociation regions (PDRs), predicting a large variety from less than a few percent to the dominant contributions coming from H1 regions.

The far-infrared [CII]-158 µm emission is further very bright and can be detected well into the epoch of reionization at z ≥ 6 (Smit et al. 2018; Bouwens et al. 2022; Fujimoto et al. 2024; Heintz et al. 2023b), enabling constraints of the H1 gas mass of galaxies at similar early epochs (Heintz et al. 2022). However, [CII] may also trace ionized gas in some environments as well (e.g., Hollenbach & Tielens 1999; Ramos Padilla et al. 2021; Wolfire et al. 2022), hindering a universal connection of this feature to H1. Recent efforts have attempted to calibrate the far-infrared fine-structure transition of singly ionized carbon [CII]-158 µm to the H1 gas mass using gamma-ray burst (GRB) sightlines through star-forming galaxies (Heintz et al. 2021). While these narrow pencil-beam sightlines do not provide information about the total gas mass of the absorbing galaxies, they can accurately determine the relative abundance between [CII] and H1. This [CII]-to-H1 calibration has also been investigated with hydrodynamical simulations of galaxies at z ~ 6–9, which were found to be in good agreement (Pallottini et al. 2017; Vizgudan et al. 2022; Liang et al. 2024).

Here we thus seek to establish a novel, more robust proxy for H1. We consider the far-infrared transitions of neutral atomic oxygen; [OI]-63 µm and [OI]-145 µm. Since neutral oxygen has an ionization potential of 13.62 eV, almost identically as bright as [CII] (Cormier et al. 2015), the rest-frame wavelength is inaccessible to ALMA below redshifts z ≥ 4. The [OI]-145 µm is more easily accessible, but it is typically an order of magnitude weaker than [CII] and [OI]-63 µm, though there is currently a debate on whether this is accurate for high-z galaxies as well (Lupi et al. 2020; Pallottini et al. 2022). As a consequence, [OI] emission has still only been observed in a small sample of galaxies at z > 1 (Coppin et al. 2012; Brisbin et al. 2015; Wardlow et al. 2017; Rybak et al. 2020; Meyer et al. 2022). However, this is likely to change in the near future.

Here we derive and provide calibrations to infer the H1 gas mass of the dense, star-forming ISM of high-redshift star-forming galaxies using the far-infrared [OI]-63 µm and [OI]-145 µm transitions as proxies, based on empirical measurements and guided by hydrodynamic simulations. We have structured the paper as follows. In Sect. 2, we detail the observations and analysis of a large sample of z ≥ 2 GRB afterglow spectra, used to derive the [OI]-to-H1 conversion factor, and in Sect. 3 we present the results. Here we also compare our observations to predictions from the SIGAME hydrodynamical simulations and two local reference samples of galaxies at z ≈ 0. In Sect. 4 we apply the calibration to a small sample of high-redshift sources and discuss the implications of the derived H1 gas masses. In Sect. 5 we summarize and conclude on our work.

Throughout the paper we assume the concordance ΛCDM cosmological model with Ω_m = 0.315, Ω_Λ = 0.685, and H_0 = 67.4 km s^{-1} Mpc^{-1} (Planck Collaboration VI 2020). We report the relative abundances of specific elements X and Y, [X/Y] = log(N_X/N_Y) − log(N_X/S'), assuming the solar chemical abundances from Asplund et al. (2021) following the prescriptions by Lodders et al. (2009).

2. Deriving the [OI]-to-H1 calibrations with GRBs

2.1. GRB sample selection and observations

Long-duration GRB afterglows have proven to be powerful probes for studying the ISM of their host galaxies (Jakobsson et al. 2004; Fynbo et al. 2006; Prochaska et al. 2007). The progenitors of GRBs are thought to occur from the collapse and death of massive (M ≥ 20–30 M☉) stars (Yoon et al. 2006; Woosley & Bloom 2006; Cano et al. 2017), linking them directly to the redshift-dependent star formation rate density (e.g., Robertson & Ellis 2012). Measuring the properties of their host galaxies thus provides a complementary view into the physical conditions in the ISM of star-forming galaxies. Since GRBs and their afterglows are some of the brightest transient events (Gehrels et al. 2009), they enable studies of the ISM for galaxies even out to z ≥ 6 (Hartog et al. 2015; Saccardi et al. 2023).

The GRB sample used in this work was mainly adopted from the sample presented by Bolmer et al. (2019), Heintz et al. (2021, 2023a). The majority of these bursts are from the X-shooter GRB (XS-GRB) afterglow legacy survey (Selsing et al. 2019). The observational strategy of this GRB afterglow survey was constructed such that the observed sample provides an unbiased representation of the underlying population of Swift-detected bursts. In order to obtain reliable column density estimates, we only considered spectra with a signal-to-noise ratio (S/N) in the wavelength region encompassing the two excited oxygen transitions, O^+**1.1304 and O1**1.1306, of S/N ≥ 3 per wavelength bin. Further, we required a simultaneous wavelength coverage and detection of the Lyman-α (Lyα) absorption feature to determine the neutral hydrogen abundance in the line of sight, effectively limiting our sample to z ≥ 1.7 due to the atmospheric cutoff at lower wavelengths. We show the O1-detected GRB sample in Fig. 1, in addition to the underlying parent sample of GRBs. The final GRB afterglow sample considered in this work consists of 19 bursts as summarized in Table 1. The distribution of the redshifts and the metallicities in the GRB sample grade p = 0.86 and p = 0.99 in a two-sided Student’s t-test and the sample is therefore generally representative of the full underlying GRB sample.

The O1-detected bursts probe galaxies spanning redshifts from z = 1.7204 (GRB 191011A) to z = 6.3118 (GRB 210905A). We adopted the H1 column densities and dust-corrected metallicities derived by Bolmer et al. (2019), Heintz et al. (2023a) for each burst. The gas-phase metallicities...
were derived as $\log([X/Y]) = \log(N_X/N_H) - \log(N_Y/N_H)_{\odot}$, with $(X/H)_{\odot}$ representing solar abundances (Asplund et al. 2021). However, since some of the metals in the interstellar medium are depleted by condensation onto interstellar dust grains, the observed depletion level $[X/Y]$ – which is correlated with the galaxy’s metallicity – was also considered (De Cia et al. 2016). By correcting for the depletion level, an estimate of the total, dust-corrected metallicity $[X/H] + [X/Y] = [M/H]$ was obtained, which is represented as $\log(Z/Z_\odot)$ (with $\log(Z/Z_\odot) = 0$ equivalent to $12 + \log(O/H) = 8.69$). The GRB sample probes galaxies with H1 column densities in the line of sight in excess of $N_{HI} = 2 \times 10^{20}$ cm$^{-2}$, classifying them as damped Lyman-$\alpha$ absorbers (DLAs; Wolfe et al. 2005). This ensures a large neutrality of the gas due to self-shielding, and is further representative of typical dense, star-forming regions (Jakobsson et al. 2006). The observed metal abundances range from $\log(Z/Z_\odot) = -2.00$ (GRB 140311A) to $\log(Z/Z_\odot) = -0.29$ (GRB 120909A) (that is gas-phase metallicities of 1–50% solar).

### 2.2. Absorption-line fitting

The procedure used for modelling the absorption line profiles is identical to previous work by Heintz et al. (2018, 2021). In this work, we determined the column densities of the excited fine-structure transitions OI$^\ast$ 1304 and OII$^\ast$ 1306 for each GRB in our sample. The absorption line profiles were modelled using VoigtFit (Krogager 2018) which fits a set of Voigt profiles to the observed absorption features and provides the redshift $z_{\text{abs}}$, column density $N$ and broadening parameter $b$ as output. Both OI$^\ast$ and OII$^\ast$ were observed to trace the same neutral interstellar gas components as several other transitions such as FeII, SiII and CII for the GRB sightlines in our sample. This is further evident that the excited OI states predominantly traces the neutral gas-phase. We thus used these other transitions to constrain the velocity, number, content of components, and broadening parameters, when fitting the OI$^\ast$ 1304 and OII$^\ast$ 1306 line complexes. The intrinsic profiles were first convolved by the measured spectral resolution of each afterglow spectrum. In the case of systems where multiple velocity components were detected, representing individual gas complexes along the line of sight, the sum of the individual column densities was reported. This is consistent with the procedure used to measure the H1 abundances and the gas-phase metallicities. An example of the Voigt-profile modelling of the OI$^\ast$ 1304 and OII$^\ast$ 1306 transitions in GRB 161023A is shown in Fig. 2. The resulting column densities are listed for the full GRB OI sample in Table 1.

### 2.3. Calibrating the $[O I]$-to-$H I$ conversion factor

The excited fine-structure transitions OI$^\ast$ 1304 and OII$^\ast$ 1306 detected in absorption arise from the $^3P_{1} \rightarrow ^3P_{0}$ and $^3P_{3} \rightarrow ^3P_{0}$ levels of neutral atomic oxygen, and were explicitly chosen because they give rise to the far-infrared $[O I]–63 \mu m$ $(^3P_1 \rightarrow ^3P_2)$ and $[O I]–145 \mu m$ $(^3P_0 \rightarrow ^3P_1)$ emission line transitions, respectively. This allowed us to derive the corresponding line-of-sight “column” luminosity of $[O I]–63 \mu m$ and $[O I]–145 \mu m$ from the spontaneous decay rates, expressed as $L_{[OI]}–63 \mu m = h \nu_{63} A_6 N_{OI}$ and likewise for $L_{[OI]}–145 \mu m$ for each GRB sightline (see also Heintz & Watson 2020; Heintz et al. 2021). Here, $h$ is the Planck constant, $\nu_{63}$ and $A_6$ are the line frequency and Einstein coefficient, respectively and $N$ is the column density of the excited transition. For $[O I]–63 \mu m$, $\nu_{63} = 4744.8$ GHz and $A_6 = 8.91 \times 10^{-5}$ s$^{-1}$, and for $[O I]–145 \mu m$, $\nu_{63} = 2060.1$ GHz and $A_2 = 1.75 \times 10^{-5}$ s$^{-1}$. Similarly, the line-of-sight H1 mass “column” density can be determined, $M_{HI} = m_{HI} N_{HI}$, where $m_{HI}$ is the mass of a single hydrogen atom and $N_{HI}$ is the total H1 column number density.

For each line of sight, we could thus determine the ratios of the column line luminosities, $L_{[OI]}–63 \mu m / L_{[OI]}–145 \mu m$, and relate them to the H1 mass column density directly as

$$
\beta_{[OI]}–63 \mu m \equiv \frac{M_{HI}}{L_{[OI]}–63 \mu m} = \frac{m_{HI} N_{HI}}{h \nu_{63} A_6 N_{OI}}.
$$

(1)

and

$$
\beta_{[OI]}–145 \mu m \equiv \frac{M_{HI}}{L_{[OI]}–145 \mu m} = \frac{m_{HI} N_{HI}}{h \nu_{145} A_2 N_{OI}}.
$$

(2)

These two expressions provide direct $[O I]–63 \mu m$-to-H1 and $[O I]–145 \mu m$-to-H1 conversion factors based on the measured column densities in the line of sight. Assuming that the derived ratios of the column densities for each sightline are representative of the mean of the relative total population that is $N_{HI}/N_{OI} = \Sigma_{HI}/\Sigma_{OI}$. The calibrations derived per unit column are thus equal to the global $[O I]–63 \mu m$-to-H1 and $[O I]–145 \mu m$-to-H1 conversion factors.

This scaling has been derived for both transitions for each GRB in the sample and converted into solar units, $M_{\odot}/L_{\odot}$, which can simply be expressed as constant factors of the absorption-derived column density ratios as

$$
\beta_{[OI]}–63 \mu m = 1.150 \times 10^{4} \frac{N_{HI}}{N_{OI}} \frac{m_{HI}}{L_{\odot}} M_{\odot}.
$$

(3)

and

$$
\beta_{[OI]}–145 \mu m = 1.138 \times 10^{5} \frac{N_{HI}}{N_{OI}} \frac{m_{HI}}{L_{\odot}} M_{\odot}.
$$

(4)

We emphasize that this approach only determines the relative mass to luminosity ratios of H1 and the two [OI] transitions and not the global properties for the GRB-selected galaxies.
Table 1. GRB line-of-sight metal abundances and the H\textsc{i}, O\textsc{i}**, .1304 and O\textsc{i}**, .1306 column densities.

<table>
<thead>
<tr>
<th>GRB</th>
<th>z</th>
<th>log $N_{\text{HI}}$ (cm$^{-2}$)</th>
<th>log($Z/Z_{\odot}$)</th>
<th>log $N_{\text{Fe}}$ (cm$^{-2}$)</th>
<th>log $N_{\text{O}^{*}}$ (cm$^{-2}$)</th>
<th>log $\beta_{\text{[OII]-63} , \mu \text{m}}$ ($M_{\odot}/L_{\odot}$)</th>
<th>log $\beta_{\text{[OII]-145} , \mu \text{m}}$ ($M_{\odot}/L_{\odot}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>090809A</td>
<td>2.7373</td>
<td>21.48 ± 0.07</td>
<td>-0.46 ± 0.15</td>
<td>15.28 ± 0.68</td>
<td>15.28 ± 0.68</td>
<td>0.26 ± 0.69</td>
<td>2.22 ± 0.50</td>
</tr>
<tr>
<td>090926A</td>
<td>2.1069</td>
<td>21.58 ± 0.01</td>
<td>-1.72 ± 0.05</td>
<td>14.77 ± 0.06</td>
<td>14.77 ± 0.06</td>
<td>0.87 ± 0.06</td>
<td>2.19 ± 0.05</td>
</tr>
<tr>
<td>100219A</td>
<td>4.6676</td>
<td>21.28 ± 0.02</td>
<td>-1.16 ± 0.11</td>
<td>13.71 ± 0.53</td>
<td>13.71 ± 0.53</td>
<td>1.63 ± 0.53</td>
<td>3.12 ± 0.89</td>
</tr>
<tr>
<td>111008A</td>
<td>4.9910</td>
<td>22.39 ± 0.01</td>
<td>-1.79 ± 0.10</td>
<td>14.25 ± 0.78</td>
<td>14.25 ± 0.78</td>
<td>2.21 ± 0.78</td>
<td>2.88 ± 0.39</td>
</tr>
<tr>
<td>120815A</td>
<td>2.3582</td>
<td>22.09 ± 0.01</td>
<td>-1.23 ± 0.03</td>
<td>15.17 ± 0.42</td>
<td>15.17 ± 0.42</td>
<td>0.98 ± 0.42</td>
<td>2.65 ± 0.12</td>
</tr>
<tr>
<td>120909A</td>
<td>3.9290</td>
<td>21.82 ± 0.02</td>
<td>-0.29 ± 0.10</td>
<td>15.21 ± 0.56</td>
<td>15.21 ± 0.56</td>
<td>0.67 ± 0.56</td>
<td>2.16 ± 0.14</td>
</tr>
<tr>
<td>130408A</td>
<td>3.7579</td>
<td>21.90 ± 0.01</td>
<td>-1.46 ± 0.05</td>
<td>14.38 ± 0.38</td>
<td>14.38 ± 0.38</td>
<td>1.58 ± 0.38</td>
<td>1.56 ± 0.24</td>
</tr>
<tr>
<td>140311A</td>
<td>4.9550</td>
<td>22.30 ± 0.02</td>
<td>-2.00 ± 0.11</td>
<td>14.40 ± 0.55</td>
<td>14.40 ± 0.55</td>
<td>1.96 ± 0.55</td>
<td>3.59 ± 0.71</td>
</tr>
<tr>
<td>150403A</td>
<td>2.0571</td>
<td>21.73 ± 0.02</td>
<td>-0.92 ± 0.05</td>
<td>15.49 ± 0.28</td>
<td>15.49 ± 0.28</td>
<td>0.30 ± 0.28</td>
<td>2.03 ± 0.13</td>
</tr>
<tr>
<td>151021A</td>
<td>2.3297</td>
<td>22.14 ± 0.03</td>
<td>-0.97 ± 0.07</td>
<td>14.50 ± 0.41</td>
<td>14.50 ± 0.41</td>
<td>1.70 ± 0.41</td>
<td>2.63 ± 0.23</td>
</tr>
<tr>
<td>151027B</td>
<td>4.0650</td>
<td>20.54 ± 0.07</td>
<td>-0.59 ± 0.27</td>
<td>14.99 ± 0.30</td>
<td>14.99 ± 0.30</td>
<td>-0.39 ± 0.31</td>
<td>1.63 ± 0.31</td>
</tr>
<tr>
<td>160203A</td>
<td>3.5187</td>
<td>21.74 ± 0.02</td>
<td>-0.92 ± 0.04</td>
<td>14.50 ± 0.55</td>
<td>14.50 ± 0.55</td>
<td>1.30 ± 0.55</td>
<td>2.96 ± 0.58</td>
</tr>
<tr>
<td>161023A</td>
<td>2.7100</td>
<td>20.95 ± 0.01</td>
<td>-1.05 ± 0.04</td>
<td>14.92 ± 0.10</td>
<td>14.92 ± 0.10</td>
<td>0.09 ± 0.10</td>
<td>1.76 ± 0.04</td>
</tr>
<tr>
<td>170202A</td>
<td>3.6456</td>
<td>21.53 ± 0.04</td>
<td>-1.02 ± 0.13</td>
<td>14.43 ± 0.12</td>
<td>14.43 ± 0.12</td>
<td>1.16 ± 0.13</td>
<td>3.03 ± 0.32</td>
</tr>
<tr>
<td>181020A</td>
<td>2.9379</td>
<td>22.24 ± 0.03</td>
<td>-1.20 ± 0.08</td>
<td>15.38 ± 0.27</td>
<td>15.38 ± 0.27</td>
<td>0.92 ± 0.27</td>
<td>3.18 ± 0.30</td>
</tr>
<tr>
<td>190106A</td>
<td>1.8599</td>
<td>21.00 ± 0.04</td>
<td>-0.40 ± 0.10</td>
<td>15.40 ± 0.12</td>
<td>15.40 ± 0.12</td>
<td>-0.34 ± 0.13</td>
<td>2.67 ± 0.90</td>
</tr>
<tr>
<td>190114A</td>
<td>3.3764</td>
<td>22.19 ± 0.05</td>
<td>-1.17 ± 0.06</td>
<td>15.32 ± 0.48</td>
<td>15.32 ± 0.48</td>
<td>0.93 ± 0.48</td>
<td>2.34 ± 0.34</td>
</tr>
<tr>
<td>191011A</td>
<td>1.7204</td>
<td>21.65 ± 0.08</td>
<td>-0.63 ± 0.07</td>
<td>14.40 ± 0.39</td>
<td>14.40 ± 0.39</td>
<td>1.31 ± 0.39</td>
<td>2.86 ± 0.53</td>
</tr>
<tr>
<td>210905A</td>
<td>6.3118</td>
<td>21.00 ± 0.02</td>
<td>-1.24 ± 0.10</td>
<td>14.73 ± 0.52</td>
<td>14.73 ± 0.52</td>
<td>0.33 ± 0.52</td>
<td>2.27 ± 0.38</td>
</tr>
</tbody>
</table>

Notes. The H\textsc{i} column densities and dust-corrected gas-phase metallicities are partly from Bolmer et al. (2019) and partly from Heintz et al. (in prep.). The O\textsc{i}**, .1304 and O\textsc{i}**, .1306 column densities are derived in this work. The last two columns, $\beta_{\text{[OII]-63} \, \mu \text{m}}$ and $\beta_{\text{[OII]-145} \, \mu \text{m}}$, denote the absorption-derived conversion factors per unit column for each GRB.

Fig. 2. Representative VLT/X-shooter GRB afterglow spectrum of GRB 161023A (de Ugarte Postigo et al. 2018). The observed spectrum is shown in black, the solid red line represents the best-fit model of the marked absorption features. The low-ion Fe\textsc{ii} and Si\textsc{ii} are used to improve the modelling of the velocity components and line broadening of the O\textsc{i}**, .1302, O\textsc{i}**, .1304 and O\textsc{i}**, .1306 line complexes.

These relations thus only provide a conversion between the integrated [O\textsc{i}] luminosities to the total H\textsc{i} gas masses assuming that the GRB sightlines are representative of the overall ISM conditions. As already showcased by Heintz & Watson (2020) using a similar methodology to determine the [C\textsc{ii}]-to-H\textsc{i} calibration and Heintz et al. (2021) for an equivalent [C\textsc{ii}]-to-H\textsc{i} calibration, this methodology provides results in remarkable agreement with hydrodynamical simulations of galaxies with similar metallicities (Glover & Smith 2016; Vizgan et al. 2022; Liang et al. 2024), albeit still with the uncertainty on how well the GRB sightlines represent the global properties of the galaxies. Further, the [C\textsc{ii}]-to-H\textsc{i} scaling is also reproduced in local galaxies where the H\textsc{i} gas mass can be constrained directly from the 21-cm hyperfine transitions (Rémy-Ruyer et al. 2014; Cormier et al. 2015). This substantiates the assumption that the GRB sightline trace representative regions of the star-forming ISM.

We derived conversion factors in the range log $\beta_{\text{[OII]-63} \, \mu \text{m}} = -0.389$–$2.205$ and log $\beta_{\text{[OII]-145} \, \mu \text{m}} = 1.561$–$3.589$. The full list of measurements for each GRB sightline is provided in Table 1. As a conservative estimate, we set the systematic uncertainty associated with the column densities for the log $\beta_{\text{[OII]-63} \, \mu \text{m}}$ and log $\beta_{\text{[OII]-145} \, \mu \text{m}}$ measurements to 0.1 dex and 0.2 dex, respectively, to take into account the uncertainty in the normalization of the spectra and the separation of the absorption-line velocity components. The systematic uncertainty is higher for log $\beta_{\text{[OII]-145} \, \mu \text{m}}$ due to the column density of the second excited fine-structure transition often not being
The chemical evolution of galaxies. We thus simply compute the metal enrichment of the gas should a physical explanation describing why the chemical evolution of galaxies is linked to the gas density and temperature (albeit less than at the 2σ level) between the absorption-derived $L_{\text{[OI]-63} \mu\text{m}}/L_{\text{[OI]-145} \mu\text{m}}$ ratio and the gas-phase metallicity with a Pearson correlation coefficient of $\rho = 0.435$ and a p-value at $p = 0.063$. There is no apparent physical explanation describing why the metal enrichment of the gas should affect the excitation states of [O I], but it may be driven by the density and temperature of the gas (Kauffmann et al. 1999; Hollenbach & Tielens 1999).

The $L_{\text{[OI]-63} \mu\text{m}}/L_{\text{[OI]-145} \mu\text{m}}$ ratio is not observed to depend significantly on the redshift ($\rho = 0.192$ and $p = 0.431$), which is also indirectly related to the metallicity through the overall chemical evolution of galaxies. We thus simply compute the weighted mean, finding $\log(L_{\text{[OI]-63} \mu\text{m}}/L_{\text{[OI]-145} \mu\text{m}}) = 1.55 \pm 0.12$, such that [O I]–63 μm will on average be ≈30x as bright as [O I]–145 μm, at least for galaxies with metallicities of 1–50% solar.

To place our results into context we compare our measurements to a compiled set of local, $z \approx 0$ galaxies, with direct measurements of the [O I]-63 μm and [O I]-145 μm line emission from the Herschel Dwarf Galaxy Survey (DGS; Madden et al. 2013) as presented by Cormier et al. (2015) in Fig. 3. All these local galaxies show [O I]-64 μm to [O I]-145 μm line ratios of 10–20, which is significantly lower than our inferred weighted mean (at >2σ confidence). The oxygen ratios of the two nearby, more massive galaxies M51 (Parkin et al. 2013) and NGC 891 (Hughes et al. 2015) are further consistent with our average estimate, with $L_{\text{[O I]-63} \mu\text{m}}/L_{\text{[O I]-145} \mu\text{m}} = 20 \pm 9$, and $=10.7 \pm 3.4$, respectively. The dwarf galaxies are arguably more representative of the high-redshift galaxy population due to their lower metallicities and more compact physical sizes.

We also consider the predictions from the Simulator of Galaxy Millimeter/submillimeter Emission (SIGMAME) framework (v3; Olsen et al. 2021). This code provides far-infrared line emission estimates calculated through radiative transfer and physically motivated recipes from a particle-based cosmological hydrodynamics simulation (SIMBA; Davé et al. 2019), with this particular version of the code including 400 simulated star-forming galaxies at $z = 0$. The range of gas densities probed by SIGMAME is $10^{-2}–10^{3} \text{cm}^{-3}$ and the far-infrared (FIR) lines are modelled using large grid of over 100,000 CLOUDY one-zone models that span the physical conditions (for example density, metallicity, ultraviolet (UV) radiation field, cosmic ray ionisation rate) encountered in the simulations. Comparing these simulations to our results and the compiled sample of local galaxies in Fig. 3 reveal that they substantially underpredict the observed line ratio. This might mainly be due to an incorrect estimate of the excitation of [O I]-63 μm (see also below), limiting the use of these simulations to corroborate our observations at least for the results including the [O I]-63 μm line emission. Indeed, Lupi et al. (2020) finds that inferring [O I] emission line strengths might be particularly model-dependent, as they can be strongly affected by photoionization effects and the thermodynamic state of the gas.

3.2. The [O I]-to-H$^\text{I}$ conversion factor

Next, we consider the conversion factors $\log(\beta_{\text{[O I]-63} \mu\text{m}})$ and $\log(\beta_{\text{[O I]-145} \mu\text{m}})$, shown in Fig. 4 as a function of gas-phase metallicity. We observe a significant log-linear anti-correlation of $\log(\beta_{\text{[O I]-63} \mu\text{m}})$ with the metallicity, with a Pearson correlation coefficient of $\rho = -0.561$ and a p-value at $p = 0.012$. Similarly for $\log(\beta_{\text{[O I]-145} \mu\text{m}})$, there appears to be a mild log-linear anti-correlation, with a Pearson correlation coefficient of $\rho = -0.258$ and a p-value at $p = 0.287$. We derive best-fit [O I]-to-H$^\text{I}$ scaling relations of

\[
\log(M_{\text{[O I]}}/M_{\odot}) = (-0.77 \pm 0.14) \times \log(Z/Z_{\odot}) \\
+ (0.26 \pm 0.18) \times \log(L_{\text{[O I]-63} \mu\text{m}}/L_{\odot}) \tag{5}
\]

and

\[
\log(M_{\text{[O I]}}/M_{\odot}) = (-0.77 \pm 0.18) \times \log(Z/Z_{\odot}) \\
+ (1.40 \pm 0.22) \times \log(L_{\text{[O I]-145} \mu\text{m}}/L_{\odot}) \tag{6}
\]

In Eq. (6), we have fixed the slope in the [O I]–145 μm-to–H$^\text{I}$ scaling relation to the slope found from the best-fit of [O I]–63 μm-to–H$^\text{I}$ scaling relation (Eq. (5)) and instead only fitted the intercept. This is mostly motivated by the significantly larger scatter of the $\log(\beta_{\text{[O I]-145} \mu\text{m}}$ measurements due to the more uncertain column density measurements of O$^\text{I*}$.1306, and the fact that the [O I]–63 μm to [O II]–37 μm ratio is theoretically expected to be constant. The larger scatter of the O$^\text{I*}$.1306 measurements,
Fig. 4. Absorption-derived $[\text{O}\ i\ 63\ \mu\text{m}]$-to-$\text{H}\ i$ (top panel) and $[\text{O}\ i\ 145\ \mu\text{m}]$-to-$\text{H}\ i$ (bottom panel) conversion factors as a function of metallicity. The color and symbol notation follow Fig. 3. The black solid line and the grey-shaded region in the top panel represents the best fit linear relation and the associated uncertainty. The dotted line in the bottom panel shows the best fit of the intersection with the slope fixed at the value of the slope from the fit in the top panel. The dashed line consists of the fit from the top panel with the weighted mean added. The grey-shaded region includes the uncertainties associated with the fit from the top panel as well as the weighted mean. The local samples are shown as upper limits and are in fine agreement with the absorption-derived conversion factors for both transitions in the GRB observations. The simulation is in good agreement with the $[\text{O}\ i\ 63\ \mu\text{m}]$-to-$\text{H}\ i$ conversion factor, while there seems to be a systematical displacement towards higher values for the $[\text{O}\ i\ 145\ \mu\text{m}]$-to-$\text{H}\ i$ conversion factor.

3.3. The $[\text{C}\ ii]/[\text{O}\ i]$ ratio

Finally, in Fig. 5 we show the absorption-derived $[\text{C}\ ii\ 158\ \mu\text{m}]$ to the $[\text{O}\ i\ 63\ \mu\text{m}]$ and $[\text{O}\ i\ 145\ \mu\text{m}]$ luminosity ratios as a function of metallicity and redshift. The color and symbol notation follow Fig. 3. The black solid lines and the grey-shaded regions show the weighted means and the associated 1- and 2-sigma uncertainty of each line ratio. Similar to Fig. 4 the local samples are shown as upper limits and are in fine agreement with the absorption-derived conversion factors for both transitions in the GRB observations. Similarly to the absorption-derived $[\text{O}\ i\ 63\ \mu\text{m}]$-to-$\text{H}\ i$ conversion factor, the simulation suggests a systematical displacement in the absorption-derived $[\text{O}\ i\ 145\ \mu\text{m}]$-to-$[\text{C}\ ii\ 158\ \mu\text{m}]$ line luminosity.
function of metallicity, respectively. For this, we primarily adopt the CII $\lambda 1335.7$ measurements from Heintz et al. (2021), but also derive additional CII $\lambda 1335.7$ abundances for GRBs 181020A, 190106A, 190114A, 190111A and 210905A following the same approach outlined in Sect. 2.2 (see Table 1). We do not observe any strong correlation for $L_{\text{CII}}$-[158]-[145] vs. metallicity, with Pearson correlation coefficient of $\rho = -0.063$ and $p$-value $p = 0.804$. For $L_{\text{CII}}$-[158]-[145] and $L_{\text{CII}}$-[158]-[145] vs. metallicity we compute weighted means of $-1.91 \pm 0.07$ and $-0.27 \pm 0.09$, respectively. These results indicate that the gas probed by the GRB sightlines generally predict weaker CII-[158] emission than either of the two far-infrared [O I] transitions.

Comparing our observations again to the simulations and local galaxy samples mentioned in the previous sections, we find that the GRBs generally probe lower line ratios $L_{\text{CII}}$-[158]-[145] and $L_{\text{CII}}$-[158]-[145] for the local galaxy vs. GRB sample, we observe that the SIGAME simulations are in better agreement with our observations (similar to the [O I]-H1 ratio). This might suggest that the GRB sightlines generally probe warmer and much denser gas in the ISM of their host galaxies, compared to the ISM gas in local galaxies (see e.g., Popping et al. 2014; De Breuck et al. 2019).

### 4. Application to [O I]-emitting galaxies at high redshifts

In an attempt to enable estimates of the H1 gas masses of high-redshift galaxies, we have derived the [O I]$_{145}$-to-H1 and [O I]$_{145}$-to-[H1] conversion factors as a function of gas-phase metallicity in star-forming galaxies at $z \approx 2-6$ using GRBs as probes. The conversion factors derived here are observed either in absorption or directly in emission from the ISM of "normal" main-sequence star-forming galaxies, albeit over a large span in redshift and metallicity. These scaling relations are therefore only applicable to sources with similar ISM properties. We consider the main-sequence galaxies at $z \approx 1.5$ from Wagg et al. (2020), who presents a single [O I]$_{63}$ line detection for the galaxy BzK-21000 at $z = 1.5213$ with a luminosity of $L_{\text{O I}}$-[63] = $3.9 \pm 0.7 \times 10^{6} L_{\odot}$. While [O I] is not detected in the remaining spectra, their stacking analysis reveals $L_{\text{O I}}$-[63] = $(1.1 \pm 0.2) \times 10^{6} L_{\odot}$. Since their targets all have stellar masses, $M_{*} \geq 10^{9.5} M_{\odot}$, we assume solar metallicities and infer from Eq. (6) H1 gas masses of $M_{\text{H1}} \approx 5 \times 10^{6} - 2 \times 10^{8}$.

These results imply low H1 gas fractions of $M_{\text{H1}}/M_{*} \approx 2-6\%$ for the star-forming galaxies at $z \approx 1.5$.

In the near future we are likely to expect an increasing number of [O I] detections from "regular" star-forming galaxies at greater redshifts. In particular, the [O I]$_{63}$ transition will be redshifted into the ALMA band 9 and the [O I]$_{145}$ transition will be placed in band 7 at $z \geq 6$, enabling measurements of these important neutral gas tracers with few hours of on-target integration for the brightest [O I]-emitting sources in the epoch of reionization (as also proposed by Lupi et al. 2020; Pallottini et al. 2022). To fully optimize the use of the derived [O I]$_{145}$-to-H1 and [O I]$_{145}$-to-[H1] gas tracers, complementary JWST observations are needed to provide constraints on the metallicity of the sources at $z > 6$ (see e.g., Heintz et al. 2023b).

### 5. Conclusions

In this paper we present the first high-redshift calibrations of the [O I]$_{145}$-to-H1 and [O I]$_{145}$-to-[H1] conversion factors, here denoted $\beta_{[O I]-63}$ and $\beta_{[O I]-145}$, respectively. This work was made in continuation of recent attempts to establish a similar [C II]-H1 calibration (e.g., Heintz et al. 2021, 2022). Due to the weakness of the direct 21-cm H1 gas tracers, such calibrations are the only alternative, and therefore vital, to infer the neutral atomic gas content of the most distant galaxies. While the far-infrared [C II]-158 μm transition is typically the brightest of the ISM cooling lines, this feature can originate from both neutral and ionized gas, making it a less optimal tracer of the neutral atomic gas only. The ionization potential and critical density of [O I] on the other hand, ensures that the far-infrared [O I]-63 μm and [O I]-145 μm transitions predominantly originates from the neutral ISM (Hollenbach & Tielens 1999).

We calibrate the $\beta_{[O I]-63}$ and $\beta_{[O I]-145}$ conversion factors using GRBs as probes of the dense, star-forming ISM in their host galaxies, spanning redshifts $z = 1.7$–6.3 and gas-phase metallicities from 1–50% solar. We derive the calibrations from the measured column densities of the excited O1$^{+}$,$\lambda 1304$ and O1$^{+}$,$\lambda 1306$ transitions detected in absorption, which give rise to the far-infrared [O I]-63 μm and [O I]-145 μm emission lines, and from Lyman-$\alpha$ for H1. The excited O1 transitions provide a measure of the luminosity per unit column assuming spontaneous decay, and Lyman-$\alpha$ the H1 mass per unit column. We found that both [O I]-H1 conversion factors are anti-correlated with the gas-phase metallicity, with best-fit scaling relations given in Eqs. (5) and (6). These indicate that galaxies with 10% solar metallicities have approx. $\times 10$ higher H1 gas masses for a given [O I] line luminosity compared to galaxies at solar metallicities.

We further made predictions for the line luminosity ratios of [O I]-63 μm, [O I]-145 μm, and [C II]-158 μm based on the absorption-derived conversion factors, for which we derived weighted means of $\log(L_{\text{O I}}-[63] \mu m/L_{\text{O I}}-[145] \mu m) = 1.55 \pm 0.12$, $\log(L_{\text{C II}}-[158] \mu m/L_{\text{O I}}-[145] \mu m) = -1.91 \pm 0.07$, and $\log(L_{\text{O II}}-[158] \mu m/L_{\text{O I}}-[145] \mu m) = -0.27 \pm 0.09$. Overall, these results indicate that the [O I] transitions might be the brightest far-infrared ISM cooling lines at high redshifts. We further compared our measurements with hydrodynamical simulations from the SIGAME framework and local galaxy samples (Madden et al. 2013; Parkin et al. 2013; Hughes et al. 2015; Cigan et al. 2016) for which the H1 gas mass could be measured directly through the 21-cm line emission. The predicted [O I]$_{145}$-to-H1 ratio from the simulations were found to be statistically consistent with our results, whereas the simulated [O I]$_{145}$-to-H1 ratios showed significant offset (at $\sigma > 3\sigma$) towards higher ratios than our inferred relation. The compiled local Herschel dwarf galaxy

<table>
<thead>
<tr>
<th>$\log(L_{\text{O I}}-[63]/L_{\text{O I}}-[145])$</th>
<th>$\log(L_{\text{O I}}-[63]/L_{\text{O I}}-[145])$</th>
<th>$\log(L_{\text{C II}}-[158]/L_{\text{O I}}-[145])$</th>
<th>$\log(L_{\text{C II}}-[158]/L_{\text{O I}}-[145])$</th>
</tr>
</thead>
<tbody>
<tr>
<td>vs. $z$</td>
<td>$-0.192$</td>
<td>$0.431$</td>
<td>$0.435$</td>
</tr>
<tr>
<td>vs. $\log(Z/Z_{\odot})$</td>
<td>$0.356$</td>
<td>$0.012$</td>
<td>$0.258$</td>
</tr>
<tr>
<td>vs. $L_{\text{C II}}-[158]/L_{\text{O I}}-[145]$</td>
<td>$-0.063$</td>
<td>$0.804$</td>
<td>$0.407$</td>
</tr>
</tbody>
</table>
sample at $z \approx 0$ (Madden et al. 2013; Rémy-Ruyer et al. 2014; Cormier et al. 2015), generally showed suppressed [OII] emission for both transitions at any given H1 gas mass and metallicity, which we surmised could be related to the typical lower volumetric hydrogen gas densities of low-redshift galaxies, or conversely more extended, diffuse H1 gas components traced by the 21-cm line.

While the next generation radio detection facilities such as the Square Kilometre Array (SKA) will significantly improve the sensitivity and the redshift range for which the H1 21-cm line transition can be detected directly, these measurements will still be limited to the most massive galaxies and out to moderate distances only at $z \approx 1.7$ (Blyth et al. 2015). Inferring the neutral gas content of the most distant galaxies thus necessitates the development and use of alternative gas tracers. We encourage further simulations and empirical observations to substantiate the high-redshift [OII]-to-H1 calibrations derived here to establish a new window into the build-up of neutral gas in the star-forming ISM galaxies in the early universe.

Acknowledgements. K.E.H. acknowledges support from the Carlsberg Foundation Reintegration Fellowship Grant CF21-0103. The Cosmic Dawn Center (DAWN) is funded by the Danish National Research Foundation under grant No. 140. This work is partly based on observations collected at the European Organisation for Astronomical Research in the Southern Hemisphere.

References
Blyth, S., van der Hulst, T. M., Verheijen, M. A. W., et al. 2015, in Advancing Astrophysics with the Square Kilometre Array (AASKA14), 128