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Published in:
Monthly Notices of the Royal Astronomical Society

DOI:
10.1093/mnras/stae266

Publication date:
2024

Document version
Publisher's PDF, also known as Version of record

Document license:
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Citation for published version (APA):
The reionizing bubble size distribution around galaxies

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Accepted 2024 January 19. Received 2024 January 19; in original form 2023 April 21

ABSTRACT
Lyman-alpha (Lyα) emission from galaxies is currently our most promising probe for constraining when and how reionization began, and thus when the first galaxies formed. At z > 7, the majority of galaxies detected with Lyα are in candidate overdensities. Here, we quantify the probability of these galaxies residing in large ionized bubbles. We create (1.6 Gpc)³ intergalactic medium (IGM) simulations; sufficient volume to robustly measure bubble size distributions around UV-bright galaxies and rare overdensities. We find MUV ≳ −16 galaxies and overdensities are ≳ 10−100 × more likely to trace ionized bubbles compared to randomly selected positions. The brightest galaxies and strongest overdensities have bubble size distributions with highest characteristic size and least scatter. We compare two models: gradual reionization driven by numerous UV-faint galaxies versus rapid reionization by rarer brighter galaxies, producing larger bubbles at fixed neutral fraction. We demonstrate that recently observed z ∼ 7 overdensities are highly likely to trace large ionized bubbles, corroborated by their high Lyα detection rates. However, Lyα detections at z ≈ 8.7 in EGS and z = 10.6 in GN-z11 are unlikely to trace large bubbles in our fiducial model − 11 and 7 percent probability of >1 proper Mpc bubbles, respectively. Lyα detections at such high redshifts could be explained by: a less neutral IGM than previously expected; larger ionized regions at fixed neutral fraction; or if intrinsic Lyα flux is unusually strong in these galaxies. We discuss how to test these scenarios with JWST and prospects for upcoming wide-area surveys to distinguish between reionization models.

Key words: galaxies: high-redshift – intergalactic medium – dark ages, reionization, first stars – cosmology: theory.

1 INTRODUCTION
The reionization of intergalactic hydrogen in the Universe’s first billion years was likely caused by photons emitted from the first galaxies, and is thus intimately linked to their nature (e.g. Stark 2016; Dayal & Ferrara 2018; Mesinger 2019). Constraining the reionization process thus enables us to infer properties of these first luminous sources, importantly giving us information about the earliest generations of galaxies which are too faint to observe directly, even with JWST. In the past decade, substantial progress has been made in measuring the timing of the late stages of reionization. The electron scattering optical depth to the CMB indicates reionization was on-going at z ∼ 7–8 (Planck Collaboration VI 2020) and the attenuation of Lyman-alpha (Lyα, 1216 Å) photons by neutral hydrogen in the intergalactic medium (IGM) in the spectra of z ∼ 5 quasars and galaxies implies the IGM was almost entirely ionized by z ∼ 5.5–6 (McGreer, Mesinger & D’Odorico 2015; Qin et al. 2021; Bosman et al. 2022; Lu et al. 2022) but that the IGM was significantly neutral (volume-averaged neutral fraction Tν ≥ 0.7) just ∼300 Myr earlier at z ∼ 8 (e.g. Davies et al. 2018b; Hoag et al. 2019; Mason et al. 2019b; Bolan et al. 2022).

While we are beginning to reach a consensus on when the end stages of reionization occurred, we still do not understand how it happened. Which sources drove it and when did it start? The onset of reionization provides pivotal information about the onset of star formation. Simulations predict the first ionized regions grow around overdensities (e.g. Furlanetto, Zaldarriaga & Hernquist 2004b; Mesinger & Furlanetto 2007; Trac & Cen 2007; Zahn et al. 2007; Ocvirk et al. 2020; Hutter et al. 2021; Qin et al. 2022), but, while there are strong hints (Castellano et al. 2016; Tilvi et al. 2020; Hu et al. 2021; Endsley & Stark 2022; Jung et al. 2022; Larson et al. 2022), this is yet to be robustly confirmed observationally. Furthermore, the ionizing emission properties of high-redshift sources are still highly uncertain, and, with current constraints on the reionization timeline alone, there is a degeneracy between reionization driven by numerous low-mass galaxies with low-ionizing emissivity (e.g. ionizing photon escape fraction ∼ 5% per cent), and rarer bright
galaxies with high ionizing emissivity (e.g. Greig & Mesinger 2017; Finkelstein et al. 2019; Mason et al. 2019a; Naidu et al. 2020). However, the clustering strength of the dominant source population has a large impact on the expected size distribution of ionized bubbles (e.g. McQuinn et al. 2007a; Mesinger, Greig & Sobacchi 2016; Hassan et al. 2018; Seiler et al. 2019). Thus, identifying and measuring large ionized regions at early times provides vital information about the reionization process.

Before we will detect the 21-cm power spectrum (e.g. Morales & Wyithe 2010; Pober et al. 2014), the most promising tool to study the early stages of reionization and the morphology of ionized regions is Ly α emission from galaxies, which is strongly attenuated by neutral hydrogen (e.g. Malhotra & Rhoads 2006; Stark et al. 2010; Dijkstra 2014; Mesinger et al. 2015; Mason et al. 2018a). If reionization starts in overdensities, we expect a strong increase in the clustering of Ly α-emitting galaxies (LAEs) in the early stages of reionization (McQuinn et al. 2007b; Hutter, Dayal & Müller 2015; Sobacchi & Mesinger 2015). Strong evidence of enhanced clustering has not yet been detected in wide-area Ly α narrow-band surveys (e.g. Ouchi et al. 2017), likely because these surveys have mostly observed at z < 7, when the IGM is probably still < 50 per cent neutral (e.g. Mason et al. 2019a; Qin et al. 2021) and thus the clustering signal is expected to be weak (Sobacchi & Mesinger 2015).

However, spectroscopic studies of z > 7 galaxies selected by broad- and narrow-band imaging in smaller fields have yielded tantalizing hints of spatial inhomogeneity in the early stages of reionization. In particular, an unusual sample of four UV luminous (M V ∼ −22) galaxies detected in CANDELS (Grogin et al. 2011; Koekemoer et al. 2011) fields (three of which are in the EGS field) with strong Spitzer/IRAC excesses, implying strong rest-frame optical emission, were confirmed with Ly α emission at z ∼ 7.1, 7.3, 7.7, and 8.7 (Oesch et al. 2015; Zitrin et al. 2015b; Roberts-Borsani et al. 2016; Stark et al. 2017). Furthermore, Ly α was recently detected at z = 10.6 in the UV-luminous galaxy GNz11 (Bunker et al. 2023). The high detection rate of Ly α in these UV bright galaxies is at odds with expectations from lower redshifts, where UV-faint galaxies are typically more likely to show strong Ly α emission (e.g. Stark, Ellis & Ouchi 2011; Cassata et al. 2015).

This may imply that these galaxies trace overdensities which reionize early, or that they have enhanced Ly α emission due to young stellar populations and hard ionizing spectra, or, more likely, a combination of these two effects (Stark et al. 2017; Mason et al. 2018b; Endsley et al. 2021a; Roberts-Borsani et al. 2023; Tang et al. 2023). Photometric follow-up around some of these galaxies has found evidence they reside in regions that are ≳ 3 × overdense (Leonova et al. 2022; Tacchella et al. 2023). Furthermore, spectroscopic follow-up for Ly α in neighbours of these bright sources has proved remarkably successful: to date, of the ∼30 galaxies detected with Ly α emission at z > 7, 14 of these lie within a few physical Mpc of three UV luminous galaxies detected in the CANDELS/EGS field at z ∼ 7.3, 7.7 and 8.7 (Tilvi et al. 2020; Jung et al. 2022; Larson et al. 2022; Tang et al. 2023). Do these galaxies reside in large ionized regions? Due to the high recombination rate at z > 10, large ionized regions require sustained star formation over ∼100 Myr (e.g. Shapiro & Giroux 1987), thus detection of large ionized regions at early times would imply significant early star formation.

Assessing the likelihood of detecting Ly α emitting galaxies during reionization requires knowledge of the expected distribution of ionized bubble sizes around the observed galaxies. Previous work has focused on predicting the size distribution of all ionized regions during reionization, as is required for forecasting the 21-cm power spectrum (e.g. Furlanetto & Oh 2005; Mesinger & Furlanetto 2007; Geil et al. 2016; Lin et al. 2016). However, as galaxies are expected to be biased tracers of the density field (e.g. Adelberger et al. 1998; Overzier et al. 2006; Barone-Nugent et al. 2014), these ionized bubble size distributions likely underestimate the expected ionized bubble sizes around observable galaxies. The 21-cm galaxy cross-power spectrum for different halo masses (e.g. Lidz et al. 2009; Park et al. 2014) reflects the typical ionized region size around different halo masses. However, the size distributions of ionized regions were not discussed in previous works. Mesinger & Furlanetto (2008b) show the Ly α damping wing optical depth distributions around galaxies of various masses at z ∼ 9, finding the most massive haloes have the lowest optical depth with smallest dispersion in optical depth, which corresponds to being hosted by larger bubble sizes with smaller variance in bubbles compared to lower mass haloes, though that work did not model the UV magnitude of the haloes and only presented optical depths for haloes M h < 2 × 10 11 M ⊙. The correlation between galaxy properties and their host ionized bubbles has been explored in some semi-analytic simulations (Mesinger & Furlanetto 2008b; Geil et al. 2017; Yajima, Sugimura & Hasegawa 2018; Qin et al. 2022), finding that more luminous galaxies are likely to reside in large ionized bubbles. However, these studies have been restricted to small volumes, (100 cMpc) 3, simulations with only a handful of UV-bright galaxies and overdensities, so Poisson noise is large, or models of cosmological Strömgren spheres which do not account for the overlap of bubbles (Yajima et al. 2018).

In this paper, we create robust predictions for the size distribution of ionized bubbles around observable (M h < −16) galaxies. We create large volume (1.6 Gpc) 3 simulations of the reionizing IGM using the semi-numerical code 21 cmFAST (Mesinger, Furlanetto & Cen 2011). With these simulations, we can robustly measure the expected bubble size distribution around rare overdensities and UV-bright galaxies (M V < −22 or M h < 10 11 M ⊙) to compare with observations. We assess how likely the observed z > 7 associations of Ly α emitters are to be in large ionized bubbles, finding that while z > 7 observations are consistent with our current consensus on the reionization timeline, Ly α detections at z > 8 are very unexpected. We further demonstrate how different reionizing source models produce very different predictions for the bubble size distribution at any neutral fraction. We discuss the prospect of using upcoming wide-area surveys to distinguish the reionizing source models based on our bubble size prediction distributions by observing a large number of overdensities to chart the growth of the first ionized regions.

This paper is structured as follows: we describe our simulations in Section 2, we present our results on the bubble size distributions as a function of galaxy luminosity and overdensity, and compare with observations in Section 3. We discuss our results in Section 4 and conclude in Section 5. We assume a flat ΛCDM cosmology with Ω m = 0.31, Ω Λ = 0.69, h = 0.68 and magnitudes are in the AB system.

2 METHODS

In the following sections, we describe our simulation set-up and analysis framework. In Section 2.1 we describe our reionization simulations. In Section 2.2, we describe how we populate simulated haloes with galaxy properties and in Section 2.3, we describe how we measure the ionized bubble size distribution using the mean free path method and the watershed algorithm.
2.1 Reionization simulations

To study the link between galaxy environment and reionization, we use the semi-numerical cosmological simulation code, 21cmfast v2 (Mesinger et al. 2011; Sobacchi & Mesinger 2014; Mesinger et al. 2016). 21cmfast first creates a 3D linear density field at high redshift, which is evolved to the redshift of interest using linear theory and the Zel’dovich approximation. The ionization field (and other reionization observables such as 21 cm brightness temperature) is then generated using an excursion-set theory approach assuming an ionization-density relation and a given reionization model. In this way, 21cmfast can quickly simulate reionization on large scales (>100 Mpc), with a simple, flexible model for the properties of reionizing galaxies.

Here, we briefly describe the creation of ionization boxes before proceeding to our simulation set-ups, and refer the reader to Mesinger & Furlanetto (2007); Mesinger et al. (2011); Mesinger et al. (2016) for more details. For a density box at redshift, z, a cell (at position x) is flagged as ionized if

\[ \xi(x, z, R, \mathcal{M}_{\text{min}}) \geq 1 + \frac{1}{2} \ln(\xi(x, z, R, \mathcal{M}_{\text{min}}), \mathcal{M}_{\text{min}}), \]

where \( \xi(x, z, R, \mathcal{M}_{\text{min}}) \) is the fraction of a collapsed matter residing in halos larger than a minimum halo mass, \( \mathcal{M}_{\text{min}} \) inside a sphere of radius \( R \), and \( \mathcal{M}_{\text{rec}} \) is the average cumulative number of recombinations. \( \xi \) is an ionizing efficiency parameter:

\[ \xi = 20 \left( \frac{N_p}{4000} \right) \left( \frac{f_{\text{esc}}}{0.1} \right) \left( \frac{f_\gamma}{0.05} \right) \left( \frac{f_b}{1} \right), \]

where \( N_p \) and \( f_{\text{esc}} \) are the input ionization parameters, the number of ionizing photons per stellar baryon, and the ionizing photon escape fraction, respectively. \( f_\gamma \) is the fraction of galactic gas in stars. \( f_b \) is the fraction of baryons inside the galaxy. While we expect a variation of these parameters with halo mass and/or time (see e.g. Kimm & Cen 2014; Wise et al. 2014; Xu et al. 2016; Trebitsch et al. 2017; Lewis et al. 2020; Ma et al. 2020), simply changing \( \xi \) and \( \mathcal{M}_{\text{min}} \) can encompass a broad range of scenarios for reionizing source models and thus produce different reionizing bubble morphologies (e.g. Mesinger et al. 2016). High values of \( \xi \) and \( \mathcal{M}_{\text{min}} \) correspond to reionization dominated by rare, massive galaxies, which require a larger output of ionizing photons to produce a reionization timeline consistent with observations, while low \( \xi \) and \( \mathcal{M}_{\text{min}} \) values correspond to reionization driven by numerous faint galaxies with weaker ionizing emissivity.

Ionized bubbles are identified by filtering the density field with a real-space top-hat filter from simulation-box scale down to grid scale and flagging the central cell in each filter ionized using the criteria in equation (1) (Mesinger et al. 2011; Zahn et al. 2011). Zahn et al. (2011) and Hutter, Trot & Dayal (2018) tested the accuracy of this method by comparing the resulting bubble size distribution to that created using radiative transfer simulations and found the resulting reionization morphologies are very similar between the two methods, and the bubble size distributions are in excellent agreement.

In this paper, we simulate large-scale boxes of dark matter haloes and the IGM ionization field in order to produce robust bubble size distributions as a function of galaxy properties with minimal Poisson noise, using two different reionizing source models. We produce (1600 cMpc)³ coeval boxes at \( z = [7, 8, 9, 10] \), with a grid size of 1024 pixels, resulting in a resolution of \( \sim 1.6 \delta \text{Mpc} \). We generate a catalogue of dark matter haloes from the density fields associated with these boxes using extended Press–Schechter theory (Sheth, Mo & Tormen 2001) and a halo-filtering method (see Mesinger & Furlanetto 2007 for full description of the method) which allows us to generate haloes with accurate halo mass function down to \( M_\delta \geq 10^8 \). We use identical initial conditions (and thus density field and halo catalogue at each redshift) for all of our models, so in our analysis below, we can isolate the impact of the reionization source model on the bubble size distribution in different galaxy environments.

We create ionization boxes spanning \( \Delta x_{\text{bin}} = 0.1 - 0.9 \) \( \Delta x_{\text{bin}} = 0.1 \), using equation (1), for two reionizing source models, similar to the approach of Mesinger, Greig & Sobacchi (2016), which span the plausible range expected by early galaxies:

(i) \textbf{Gradual}: Reionization driven by faint low-mass galaxies down to the atomic cooling limit \( (M_{\min} = 5 \times 10^8 M_\odot, M_\delta \leq -11.0) \).2

Reionization driven by numerous faint galaxies leads to a gradual reionization process, where the IGM can begin to reionize very early. We show in Fig. 1 that the ionized regions in this model start slowly and gradually grow and overlap. We use this as our fiducial model.

(ii) \textbf{Rapid}: Reionization driven by rarer bright galaxies \( (M_{\min} = 10^{10} M_\odot, M_\delta \leq -19.5) \). As massive galaxies take more time to assemble, reionization starts later and the morphology is characterized by rarer larger ionized regions at fixed neutral fractions.

For each model, at each redshift, we vary \( \xi \) so as to compare different reionization morphologies at the same \( \Delta x_{\text{bin}} \). In the end, we create a total of 72 simulations: 4 (redshift) \( \times 2 \) (reionization model) \( \times 9 \) \( \Delta x_{\text{bin}} \) ionization boxes, and 4 (redshift) halo catalogues. In addition, in Section 3.4, to compare our simulations with observations, we expand the \( \Delta x_{\text{bin}} \) range at the high-\( \Delta x_{\text{bin}} \) end to \( \Delta x_{\text{bin}} = [0.85, 0.90, 0.95] \) at \( z = 9 \) for the two models.

Example slices of the ionization field from the two sets of simulations are shown in Fig. 1. This clearly shows that the \textit{Rapid} model has larger rarer bubbles compared to the \textit{Gradual} model at fixed \( \Delta x_{\text{bin}} \). Underdense regions are more likely to be ionized in the \textit{Gradual} model. This is because in the \textit{Gradual} model, faint galaxies, which live in a wider density range, are able to ionize the IGM. While in the \textit{Rapid} model, only bright, more massive galaxies, which most likely only live in overdensities, can ionize the IGM.

Fig. 2 shows potential reionization timelines of the two reionization models, for demonstration purposes only. To produce example reionization histories for our two models we follow the standard procedure (e.g. Robertson 2010) and generate an ionizing emissivity from the product of the halo mass density, integrated down to the two mass limits described above, and an ionizing efficiency, \( \xi \). We alter \( \xi \) for both models to fix the redshift of the end of the reionization to \( z \sim 6 \). The \textit{Gradual} model has an earlier onset of reionization and slower redshift evolution of \( \Delta x_{\text{bin}} \) compared to the \textit{Rapid} model. We note that as we use coeval boxes we do not assume a model reionization history in this work, rather we will use non-parametric reionization timeline inferred by Mason et al. (2019b) from independent constraints on the IGM neutral fraction, including the Ly \( \alpha \) equivalent width distribution (Mason et al. 2018a; Hoag et al. 2019; Mason et al. 2019a), Ly \( \alpha \) emitter clustering (Sobacchi & Mesinger 2015), Ly \( \alpha \) forest dark pixels fraction (McGreer et al. 2015), and QSO damping wings

1https://github.com/andreimesinger/21cmFAST
Figure 1. Slices from our simulations at $\tau_{\text{HI}} = 0.2, 0.5, 0.7, 0.9$ for Gradual (upper panel) and Rapid (lower panel). White regions show ionized gas and black regions show neutral gas. We show 1.5 cMpc slices in a $300 \times 300$ cMpc region of our $(1.6 \text{cGpc})^3$ coeval cubes. We plot galaxies in this slice, colour-coded by $M_{\text{UV}}$, in the leftmost column. Here, we only show galaxies with $-22 \leq M_{\text{UV}} \leq -16$ for demonstration purposes.

Figure 2. Example reionization timelines for the Gradual model (solid line) and the Rapid model (dashed line) for demonstration purposes. Different symbols are neutral fractions constrained by Lyα equivalent width (stars; Mason et al. 2018a, 2019a; Bolan et al. 2022), Lyα emitter clustering (squares; Sobacchi & Mesinger 2015), Lyα forest dark pixels fraction (circles; McGreer et al. 2015), and QSO damping wings (diamonds; Davies et al. 2018a; Greig et al. 2019) observations. The grey line with shaded region is the reionization timeline and its 16–84 percentile inferred using the aforementioned observations (Mason et al. 2019a). In the following, we will use this grey posterior for $\tau_{\text{HI}}$ for comparing to observations as a function of redshift, the Rapid and Gradual models are shown just to illustrate how these models differ when the ionization efficiency is fixed (see Section 2.1).

(Davies, Becker & Furlanetto 2018a; Greig, Mesinger & Bahados 2019) and the Planck Collaboration VI (2020) electron scattering optical depth.

2.2 Galaxy population model

To populate haloes with realistic galaxy properties, we use a conditional UV luminosity to halo mass relation, to assign UV luminosities, with intrinsic scatter, to our halo catalogue. We follow Ren, Trenti & Mason (2019) and assume UV magnitudes at a given halo mass are drawn from a Gaussian distribution with dispersion $\sigma$ and median $M_{\text{UV}}(M_h, \sigma, z)$:

$$p(M_{\text{UV}} | M_h) = \frac{1}{\sqrt{2\pi\sigma}} \exp \left( -\frac{(M_{\text{UV}} - M_{\text{UV}}(M_h, \sigma, z))^2}{2\sigma^2} \right).$$

The dispersion was originally introduced to explain scatter in the Tully–Fisher relation (Yang et al. 2005). It is a free parameter in our model, and following Whilter et al. (2020) we assume $\sigma = 0.5$ mag. Ren et al. (2019) found that this value is consistent with observed luminosity functions over $z \sim 6–10$, and this value is also consistent with the expected variance due to halo assembly times (Ren, Trenti & Mutch 2018; Mason, Trenti & Treu 2023). Whilter et al. (2020) found that this scatter has only a minor impact on the transmission of Lyα from galaxies in the reionizing IGM, so we do not expect it to significantly change the relationship between galaxy luminosity and the size of the ionized bubbles they reside in.

The median relation $M_{\text{UV}}(M_h, \sigma, z)$ is set by calibration to the UV luminosity function. Ren et al. (2019) showed that above $M_h \gtrsim 10^{12} \text{M}_\odot$ a flattening is required in $M_{\text{UV}}(M_h)$ to maintain consistency with the observed UV LFs — which can be thought of as a critical mass or luminosity threshold for star formation. Given that our halo catalogue contains only a small number (0.001 per cent of the total catalogue) of $>10^{12} \text{M}_\odot$ haloes at $z \sim 7$, and far fewer at $z > 7$ due to the steepness of the halo mass function, we do not consider this
flattening. We thus use the $M_{\nu\nu}(M_\text{h}, z)$ relations from the Mason, Trenti & Treu (2015) UV luminosity function model as the median UV magnitudes for equation (3). Our resulting luminosity functions are consistent with $z \sim 7$–10 observations over the range where observations are currently magnitude complete: $-22 \lesssim M_{\nu\nu} \lesssim -17$ (e.g. Bouwens et al. 2021, see Appendix A).

2.3 Measuring bubble sizes

We measure the size of ionized regions, $R_{\text{ion}}$, using both the mean-free-path (MFP) method (Mesinger & Furlanetto 2007) and the watershed algorithm (Vincent & Soille 1991), an image segmentation algorithm which was first applied to reionization simulations by Lin et al. (2016).

Lin et al. (2016) tested a range of approaches for estimating the sizes of ionized bubbles in simulations and determined these two methods were optimal compared to other techniques in the literature because they most accurately recover input ionized bubble size distributions, can account for overlapping bubbles, and produce sizes corresponding to a physically intuitive quantity. Other commonly used approaches for modelling the bubble size distribution, i.e. the excursion set formulation (Furlanetto et al. 2004b; Furlanetto & Oh 2005) or approaches which grow cosmological Strömgren spheres around haloes (e.g. Yajima et al. 2018) will underestimate the largest bubble sizes because these approaches do not include the effect of overlapping bubbles.

Here, we describe these two methods, and their advantages and limitations. We will discuss how our resulting bubble size distributions compare to works using other methods in Section 4.1.

2.3.1 Mean free path (MFP)

This method was first used to measure ionized bubble sizes by Mesinger & Furlanetto (2007). It is essentially a Monte Carlo ray-tracing algorithm, which enables us to measure a probability distribution for ionized bubble sizes by estimating the distance photons travel before they encounter neutral gas. We randomly choose a starting position (or the position of a galaxy, as described later), if the cell is fully ionized, we measure the distance from that position to where we encounter the first neutral or partially ionized cell at a random direction. Given our simulation resolution, the smallest bubble size we can measure is $\sim 1$ cm$^{-1}$. If the position is neutral, we set $R_{\text{ion}} = 0$ cm$^{-1}$. We measure bubble sizes over the full simulation volume by sampling the distance to neutral gas from $10^5$ random positions and sightlines to build bubble size distributions for our simulations. The MFP method will induce scatter in the measurement of the ‘real’ bubble size. For example, the size distribution of a spherical bubble measured with the MFP method will range from 0 to 2 times the true radius of the bubble. In the context of galaxy Ly $\alpha$ emission line visibility, which is a main focus of this work, such scatter should be included in bubble size distribution because the observed Ly $\alpha$ is sightline dependent. In the context of bubble size studies related to the volume occupation fraction of ionized bubbles, the watershed algorithm may be more appropriate.

In Section 3.1, we will show the bubble size distribution as a function of galaxy $M_{\text{ion}}$, to estimate the sizes of ionized bubbles around observable galaxies. For this, we use the mean free path method as defined above, but start our measurements at the position of each galaxy in the simulation box.

We also will measure the bubble size distribution as a function of galaxy overdensity to compare with current observations. Galaxy overdensity depends on the dark matter density of the underlying field (e.g. Cole & Kaiser 1989; Mo, Jing & White 1997; Sheth et al. 2001): $n = \pi(1 + \delta b)$, where $n$ is the number density of galaxies observed in a field, $\pi$ is the mean cosmic number density, $b$ is the bias, and $\delta$ is the dark matter density in the field. Since $21\text{cmFast}$ populates haloes and calculates $\pi_{\text{halo}}$ based on galaxy number density via the excursion set formulation (Furlanetto et al. 2004b), we expect a strong relation between bubble size and galaxy overdensity (e.g. Mesinger & Furlanetto 2007).

We define the observed overdensity, $N/N_{\text{cross}}$, as the number, $N$, of galaxies brighter than a given limit in a survey volume relative to the number expected in that volume based on the average in the whole simulation box, $N_{\text{cross}}$. To measure overdensity using our galaxy catalogue, described in Section 2.2, for a mock survey, we discard galaxies with $M_{\nu\nu} > M_{\nu\nu, \lim}$, where $M_{\nu\nu, \lim}$ is the UV magnitude limit in an observed overdensity. While the galaxy catalogue and $\pi_{\text{halo}}$ boxes are generated from the same density field, as described in Section 2.1, galaxies are given sub-grid positions, thus to compare the overdensity and $\pi_{\text{halo}}$ fields, we convert the resulting galaxy catalogue into a galaxy number count grid of the same size as the $\pi_{\text{halo}}$ grids. Then, we convolve the galaxy number count grid with a 3D kernel of the survey volume and divide the value of each cell by $N_{\text{cross}}$, the mean number count per cMpc$^3$ in the halo box, to obtain the overdensity in each cell.

Cells in the resulting overdensity box correspond to positions with a given overdensity above the magnitude limit within the volume. We can then carry out an analogous procedure to that described above using the mean free path algorithm to find the bubble size distribution as a function of overdensity using the mean free path method, by starting in positions of a given overdensity.

2.3.2 Watershed algorithm

This method was first used to measure ionized bubble sizes in reionization simulations by Lin et al. (2016). It is an image segmentation algorithm which treats constant values of a scalar field as contour lines corresponding to depth in a tomographic map, which it then ‘floods’ to break up the images into separate water basins (Vincent & Soille 1991).

We use the implementation of the watershed algorithm in skikit-image (van der Walt et al. 2014). We apply the algorithm to 3D binary $\pi_{\text{halo}}$ cubes. We first apply the ‘distance transform’ to calculate the Euclidean distance, $d_i$, of every point to the nearest neutral region (if the point is neutral then the distance is zero). We invert the distances to ‘depths’: $d_i \rightarrow -d_i$. Centres of bubbles are then local minima in the depth cube and the bubble boundaries are identified by flooding regions starting from the local minima, and marking where regions meet – these are contours of constant depth $d_i$.

As with any image segmentation algorithm, the identification of local minima will lead to oversegmentation, as every local minimum will be marked as a unique bubble, even if it is overlapping with a larger one, thus a threshold must be used to avoid this. We follow the prescription of Lin et al. (2016) and use the ‘H-minima transform’ to essentially ‘fill in’ small basins. We identify basins with a relative depth of $h$ from the local minimum to the bubble boundary and set $d_i \rightarrow d_i + h$ for these regions, reducing the depth of the local minima. After the H-minima transform, we can again identify bubbles as above and see that large bubbles are correctly identified. This process may remove small isolated bubbles which had depth $< h$. These can be added back in manually using the initial segmentation cube.
The H-minima threshold $h$ is a free parameter, we use $h = 2.5$, which is fixed so that the resulting bubble size distribution is comparable to that obtained with the MFP method above and bubbles do not suffer too much from oversegmentation. We solve for the value of $h$ by minimizing the Kullback–Leibler divergence (KL divergence; Kullback 1968) between the watershed bubble size distribution and MFP bubble distribution in a $(500$ cMpc)$^3$ sub-volume of our simulation. We obtain a cube with the cells corresponding to unique bubbles labelled. From this, we can calculate the volume of each bubble and calculate the size as the radius of each bubble assuming they are spherical: $R = (3V/4\pi)^{1/3}$.

The watershed algorithm is a more computationally intensive method than the MFP method, and requires some tuning of the $h$ threshold, so we predominantly use the MFP approach. However, the watershed algorithm has a significant advantage in that it can measure the absolute number of bubbles in a volume. It is also possible to use it to directly connect galaxies and their host bubbles. We will use it in Section 3.5 to make forecasts for the number of large bubbles expected in upcoming wide-area surveys.

3 RESULTS

Previous works have focused on simulating the global bubble size distribution, in order to produce predictions for 21-cm experiments (e.g. Furlanetto & Oh 2005; Mesinger & Furlanetto 2007; Geil et al. 2016; Lin et al. 2016). Some 21-cm-galaxy cross-correlation studies (e.g. Lidz et al. 2009; Park et al. 2014) calculate the correlation scales for various halo masses but do not directly calculate the bubble size distribution. Here, we focus on the expected bubble size distribution around observable galaxies, which are likely to be more biased density tracers, and thus, we expect are likely to trace the largest bubbles.

In Section 3.1, we present the bubble size distribution as a function of galaxy UV luminosity, and in Section 3.2, we show the bubble size distribution as a function of galaxy overdensity. The impact of different reionizing source models on the bubble size distribution is discussed in Section 3.3. We demonstrate in Appendix B that our results do not significantly depend on redshift. In Section 3.4, we use our simulations to interpret recent observations of Ly $\alpha$ emission in overdensities at $z \gtrsim 7$, and we make predictions for upcoming wide-area observations in Section 3.5.

3.1 Bubble size distribution as a function of UV luminosity

To first order, UV luminosity traces dark matter halo mass and thus density (e.g. Cooray & Milosavljevic 2005; Tempel et al. 2009; Mason et al. 2015). We thus expect the brightest galaxies to reside in the most massive haloes in overdense regions, and therefore these galaxies are likely to sit in large bubbles which reionized early.

We quantify this in Fig. 3, where we show the size distribution of ionized bubbles around galaxies of a given UV luminosity as a function of the volume-averaged IGM neutral fraction, $\tau_{\rm UV}$, in our simulations, compared to the bubble size distribution in the full volume. This is essentially the distribution at the mean density, $\delta = 0$. We measure the distribution of bubble sizes in $4$ $M_{\rm UV}$ bins: $M_{\rm UV} = -16, -18, -20, -22$, with $\Delta M_{\rm UV} = 0.1$. We show our fiducial Gradual simulation but will compare it to the Rapid simulation in Section 3.3.

In contrast to previous literature, we also include the fraction of galaxies (or randomly selected pixels for our full volume bubble size distribution) which are in neutral regions in our simulation. We mark these fractions with arrows in Fig. 3. These sources may reside in ionized bubbles below our resolution limit ($\sim 1$ cMpc for bubble radius). Including these occurrences in our bubble size distribution leads to important insights about the environments of galaxies as we discuss below. We note that the ‘full volume’ bubble size distribution excluding neutral cells and those below our resolution limit is equivalent to the bubble size distributions presented in previous literature (e.g. Furlanetto & Oh 2005; Mesinger & Furlanetto 2007).

Fig. 3 shows that as $\tau_{\rm UV}$ decreases, the bubble size distributions shift to higher values, which is expected as ionized regions grow. Compared to the bubble size distribution in the full volume, we see three important features of the bubble size distributions which we describe below.

First, while the bubble size distribution in the full volume has a high fraction of bubbles with $R \lessapprox 1$ cMpc, observable galaxies ($M_{\rm UV} \lessapprox -16$) are $> 10 - 1000 \times$ more likely to be in bubbles rather than neutral regions. This is because galaxies are biased tracers of the density field and therefore trace ionized regions more closely. At the end stages of reionization, $\tau_{\rm UV} \lessapprox 0.5$, we find only $\lesssim 10$ per cent of observable galaxies are in small ionized or neutral regions below our resolution limit. This is consistent with the idea of the ‘post-overlap’ phase of reionization (e.g. Miralda-Escudé, Haehnelt & Rees 2000), where the majority of galaxies lie within ionized regions and only voids remain to be ionized.

We see a strong trend with UV luminosity, where the brightest galaxies are almost always likely to be in small ionized or neutral regions. By contrast, the proportion of UV-faint galaxies in small ionized or neutral regions is high early in reionization, but declines rapidly from $\sim 60$ per cent at $\tau_{\rm UV} \sim 0.9$ to $\sim 10$ per cent at $\tau_{\rm UV} \sim 0.5$ for $M_{\rm UV} \lesssim -18$ galaxies. This is driven by the clustering properties of the UV-faint galaxies as we discuss below. This may explain the low detection rate of Ly $\alpha$ in UV-faint galaxies at $z \gtrsim 8$ (Hoag et al. 2019; Mason et al. 2019a; Morishita et al. 2023) compared to the higher detection rate in UV bright galaxies seen by Jung et al. (2022) at the same redshift.

Second, we see that the bubble size distribution around observable galaxies peaks at a similar size for all $M_{\rm UV}$ bins, which indicates that, on average, these galaxies are in the same bubbles. This peak, corresponding to the mean size of ionized regions, has been described as a ‘characteristic’ scale, $R_{\rm char}$ (e.g. Furlanetto & Oh 2005). In the following, we refer to the mean size of ionized regions as the characteristic size. We see that the characteristic scale of ionized regions increases by over two orders of magnitude during reionization. However, we do find an increasing characteristic scale as a function of UV luminosity: galaxies brighter than $M_{\rm UV} \gtrsim -20$ are expected to reside in bubbles $\sim 1.5–2 \times$ larger than the characteristic bubble scale in the full volume.

Finally, we see that the width of the bubble size distribution decreases as galaxy UV luminosity increases. This is due to the clustering of galaxies: UV bright galaxies are more likely to be in overdense regions which will reionize early, whereas UV faint galaxies can be both ‘satellites’ in overdense, large ionized regions, or ‘field galaxies’ in less dense regions which remain neutral for longer (see also Hutter et al. 2017, 2021; Qin et al. 2022) This figure demonstrates that UV-faint galaxies will have very significant

3Note that, our characteristic scale is at least an order of magnitude higher than that presented by Furlanetto & Oh (2005) due to our use of the mean free path approximation, which captures the sizes of overlapping bubbles (Lin et al. 2016)
sightline variance in their Ly α optical depth, and highlights the importance of using realistic bubble size distributions for inference of the IGM neutral fraction (see also e.g. Mesinger & Furlanetto 2008a; Mason et al. 2018b).

3.2 Bubble size distribution as a function of galaxy overdensity

In this section, we investigate the distribution of bubble sizes as a function of galaxy overdensity, \(N/(\langle N \rangle)\). This distribution should directly reflect how structure formation affects reionization.

As described in Section 2.3, an observed galaxy overdensity, \(N/(\langle N \rangle)\), depends on the survey depth and volume. For our investigation here, we explore expected overdensities within a medium-deep JWST observation within 1 NIRISS pointing (or 1/2 of the NIRCam field-of-view), aiming to simulate observations similar to those obtained by the JWST/NIRISS pure-parallel PASSAGE survey (Malkan et al. 2021). We thus use a survey limiting depth of \(m_{AB} = 28\) and area 4.84 sq. arcmin with a redshift window of \(\Delta z = 0.2\). This corresponds to [\(M_{UV,\lim}, V_{\text{survey}}\] ] = [−19, 2014 cMpc] at \(z = 8 ± 0.1\). We follow the procedure described in Section 2.3 to create a cube of \(N/(\langle N \rangle)\) using these survey parameters, and then select 200 000 cells\(^4\) to measure the bubble size distribution as a function of overdensity.

Fig. 4 shows the bubble size distributions for \(N/(\langle N \rangle) \approx 5\), \(N/(\langle N \rangle) \approx 10\), and \(N/(\langle N \rangle) \gtrsim 15\), along with the bubble size distribution in the full volume as a function of \(\tau_{\text{HI}}\), for the Gradual model. As in Section 3.1, we see the clear trend that the bubble size distributions increase to higher values as the universe reionizes, but we can now identify where the reionization process begins. We can see that the most overdense regions reionize first and inhabit the largest ionized bubbles. As in Section 3.1, we investigate three clear trends in the bubble size distribution as a function of galaxy overdensity.

First, overdense regions start and finish carving out ionized bubbles earlier compared to regions at the mean density. We see a much larger proportion of overdense regions already in \(R_{\text{ion}} > 1\) cMpc bubbles early in reionization. We find at \(\tau_{\text{HI}} = 0.9\), when only 10 per cent of the total IGM volume is ionized, \(\gtrsim 30\) per cent of the \(N/(\langle N \rangle) \geq 10\) regions are already in \(R_{\text{ion}} > 1\) cMpc bubbles. By \(\tau_{\text{HI}} = 0.5\), all of the \(N/(\langle N \rangle) \geq 10\) regions are in \(R_{\text{ion}} > 1\) cMpc bubble. This demonstrates that early in reionization, we expect only the strongest overdensities to trace large ionized regions.

Second, ionized bubbles around overdense regions are larger than the characteristic bubble size in the full volume, particularly in the early stages of reionization. At \(\tau_{\text{HI}} = 0.8\), the characteristic bubble size around \(N/(\langle N \rangle) \geq 10\) regions is \(R_{\text{ion}} \sim 10\) cMpc, which is \(\sim 2 \times\) larger than the mean bubble size in the full volume at that time, and large enough for significant Ly α transmission (e.g. Miralda-Escude 1998; Mason & Gronke 2020; Qin et al. 2022). Detection of Ly α in a highly neutral universe is thus not unexpected if the LAEs are in highly overdense regions.

The mean bubble size of overdense regions grows more slowly than that of less overdense regions. In the early stage of reionization, bubbles around the most overdense regions grow in isolation and
do not merge with similarly sized bubbles because most overdense regions are far away from each other. By contrast, bubbles created by less overdense regions are more likely to grow rapidly by merging with other bubbles.

Finally, again, we see the bubble size distributions are broad, but that the strong overdensities have the narrowest distribution of bubble sizes because they are guaranteed to trace ionized environments, whereas less dense regions can be isolated, and therefore in smaller bubbles, or contained within large scale overdensities in large bubbles.

**3.3 Bubble size distribution as a function of reionizing source model**

In the previous sections, we have shown the bubble size distribution using only our fiducial Gradual faint-galaxies driven reionization model. Here, we demonstrate how the bubble size distribution changes if instead reionization is driven by rarer brighter galaxies in our Rapid model. We show the bubble size distributions for the two models as a function of the IGM neutral fraction in Figs 5 and 6 for galaxies of given $M_{UV}$ and galaxy overdensities.

Both models have qualitatively similar bubble size distributions but the Rapid model predicts much larger bubble sizes at fixed neutral fraction, particularly at the earliest stages of reionization. A key prediction of the Rapid model is the existence of large ($\sim 30$–100 cMpc) bubbles at the earliest stages of reionization, $\tau_{\text{HI}} \sim 0.9$, in order to fill the same volume with ionized hydrogen around the more biased ionizing sources.

First, galaxies in the Gradual model are more likely to reside in neutral IGM at the beginning of reionization, compared to galaxies in the Rapid model. At $\tau_{\text{HI}} = 0.9$, $\sim 80$ per cent of the $M_{UV} = -16$ galaxies have bubble sizes no greater than 1 cMpc in the Gradual model. By contrast, in the Rapid model, only $\sim 60$ per cent of $M_{UV} = -16$ galaxies are in such neutral regions at the same $\tau_{\text{HI}}$.

At the mid-point of reionization ($\tau_{\text{HI}} = 0.5$), UV-faint galaxies ($M_{UV} = -16$) in the Gradual model ($\sim 9$ per cent) are half as likely to be in small ionized/neutrally regions compared to UV-faint galaxies in the Rapid model ($\sim 20$ per cent). This is because the early ionized regions in the Rapid model are concentrated around the most overdense regions, compared to a more uniform coverage of bubbles seen in the Gradual model (see Fig. 1). In the Rapid model, isolated faint galaxies cannot create $R_{\text{ion}} > 1$ cMpc bubbles around themselves, because reionization is dominated by $M_{UV} \lesssim 19.5$ galaxies in this model. Therefore, isolated faint galaxies remain in $R_{\text{ion}} < 1$ cMpc bubbles even at the mid-point of the reionization.

Second, galaxies in the Rapid model blow out big ionized bubbles early in the reionization. However, the bubble sizes do not grow as rapidly as those in the Gradual model. At the beginning of reionization, the characteristic bubble size in the Rapid model is $R_{\text{char}} \approx 10$ cMpc. In the Gradual model, the characteristic bubble size is $\sim 3 \times$ smaller: no more than 3 cMpc. By the latest stages of reionization ($\tau_{\text{HI}} = 0.1$), the mean bubble sizes in the Rapid model...
are $\sim 300$ cMpc. However, in the Gradual model, the mean bubble size has grown twice as rapidly, reaching $\sim 200$ cMpc. The different evolutionary trends reflect the different bubble-merging histories of the two models. In the Gradual scenario, many faint galaxies create small ionized bubbles and soon merge together to form big bubbles. In the Rapid model, big bubbles form early, but due to the rarity of bright ionizing galaxies, bubbles are less likely to merge and immediately double in size compared to those in the Gradual model.

We can see from this comparison that there can be a degeneracy between the Gradual and Rapid model. If we find evidence of a large (>10 cMpc) bubble at high redshift, it could be explained by a bright-galaxies-driven reionization at a high-neutral fraction, or by the faint-galaxies-driven reionization but with a lower neutral fraction. However, independent information on the reionization history and/or information from the dispersion of bubble sizes along multiple sightlines could break this degeneracy. We discuss this in Section 4.2.

3.4 Interpretation of current observations

In this section, we use our simulations to interpret some recent observations of Ly $\alpha$ emission at $z \gtrsim 7$ in candidate overdensities. Here, we aim to establish if the enhanced Ly $\alpha$ visibility in these regions can be explained by the sources tracing an ionized overdensity, and how likely that scenario is given our consensus timeline of reionization and either of our two reionization models.

We focus on observations of $z \gtrsim 7$ Ly $\alpha$ emission from galaxies in 6 regions in the sky, in candidate overdensities: the COSMOS field at $z \approx 6.8$ (Endsley & Stark 2022), BDF field at $z \approx 7.0$ (Vanzella et al. 2011; Castellano et al. 2016, 2018; Castellano et al. 2022), EGS field with two regions at $z \approx 7.7$ and 8.7 (Oesch et al. 2015; Roberts-Borsani et al. 2016; Tilvi et al. 2020; Jung et al. 2022; Larson et al. 2022; Leonova et al. 2022; Tang et al. 2023), the field behind the galaxy cluster Abell 2744 at $z \approx 7.9$ (Morishita et al. 2023) and the area around the $z = 10.6$ galaxy GNz11 (Oesch et al. 2016; Bunker et al. 2023; Tacchella et al. 2023).

To compare with observations at known redshifts, we will switch from comoving to proper distance units. Due to the incompleteness of the observations, here we aim to create bubble size distributions for regions in our simulations that are approximately similar to those observed. Our simulations are coeval boxes at $z = 7, 8, 9, 10$, so in the following, we use the box closest in redshift to the observations, but use the observed redshift to fix assumed IGM neutral fractions and to calculate physical distances. We demonstrate in Appendix B that our bubble size distributions do not depend significantly on redshift.

We create mock observations assuming the same area as the observed overdensities. For the regions which only have photometric overdensities, due to the large redshift uncertainties in the photometric overdensities, but motivated by the $\Delta z \approx 0.2$ redshift separation of Ly $\alpha$ emitters in all of these regions, we assume a redshift window of $\Delta z = 0.2$ for our mock observations. This corresponds to $\sim 5-8$ Mpc at $z \sim 7-10$. In all cases, we will assume the observed overdensity of Lyman-break galaxies to be the same as in that smaller volume as in the true observed volume. This means we are likely overestimating the true overdensity, in that case our estimated probabilities can be seen as upper limits.

Using these assumed volumes, we then use the method described in Section 2.3.1 to convolve our galaxy field with the volume and depth kernel of the observations to create a cube of overdensity.
matched to each observation set-up. We then select regions in the overdensity cube which match the observed overdensity estimates.

We assess the probability of the observed overdensities lying in ionized regions >1 pMpc in radius, which would allow ≥30 per cent of Ly α flux to be transmitted at the rest-frame Ly α line centre (up to ~50 per cent transmission for emission 500 km s⁻¹ redward of linecentre, e.g. Mason & Gronke 2020; Endsley & Stark 2022; Qin et al. 2022; Prieto-Lyon et al. 2023), with a ~10 per cent variation in transmission over the redshift range of interest. While the true Ly α detection rate will depend on the flux limit of the survey and the Ly α flux emitted by the galaxies – which has a broad spread, as captured by the Ly α equivalent width distribution (EW; e.g. Pentericci et al. 2014; Mason et al. 2018a; Jung et al. 2020; Endsley et al. 2021a), due to a number of internal factors, e.g. star formation rate, dust attenuation, and viewing angle (e.g. Yajima et al. 2012; Smith et al. 2019) – before attenuation in the IGM, this threshold gives us a qualitative approach with which to interpret the observations.

Assuming the ‘pre-IGM’ Ly α EW distribution model by Mason et al. (2018a) (where Ly α EW is a function of M_Ly), the increase in Ly α EW with decreasing UV magnitude is roughly balanced by decrease in continuum flux, thus the Ly α detection rate for M_Ly ~ -19 Lyman break galaxies is roughly constant as a function of UV magnitude, given a fixed flux limit of the observations. Thus, our constant bubble size/transmission threshold of >1 pMpc should indicate regions where M_Ly ~ -19 galaxies can be detected with Ly α emission, regardless of individual galaxy properties. We defer full forward-modelling of Ly α observations to a future work.

At the redshift of each observation, we assume a non-parametric estimate of the IGM neutral fraction, f_HI, inferred by Mason et al. (2019b) described in Section 2.1. We then calculate the final bubble size distribution by marginalizing the bubble size distribution at each f_HI over the inferred f_HI distribution. We also measure the characteristic bubble sizes, R_bubble, for the observed overdensities, which indicates the mean size of ionized regions above our resolution limit around the overdensities.

We present a summary of our simulation set-ups to compare to these observations in Table 1, the resulting probability of each region residing in a large ionized region in Fig. 7, and R_bubble. The full bubble size distributions are described in Appendix C.

3.4.1 z ~ 7 overdensities in COSMOS and BDF fields

In the COSMOS field, Endsley & Stark (2022) detected Ly α in 9/10 M_Ly ~ -20.4, z ~ 6.8 galaxies in a 140 pMpc³ volume. Using these spectroscopic confirmations, they estimate the lower limit of the overdensity of this region is ≥3. They estimate that individual galaxies in this field can create ionized bubbles R_bubble ~ 0.69–1.13 pMpc. Taking into account the N(H/α) ~ 3 overdensity and the ionizing contribution from M_Ly ~ -17 galaxies, they estimate an ionized bubble radius of R_bubble ~ 3 pMpc in this volume.

We predict that almost 100 per cent of regions this overdense at f_HI ~ 0.5 are in >1 pMpc bubbles and the characteristic bubble size is R_bubble = 6.4 pMpc at f_HI ~ 0.4. The high LAE fraction detected by Endsley & Stark (2022) is thus consistent with being a typical ionized region in our Gradual model. In the Rapid model, we predict even larger bubble sizes around this overdensity: the characteristic bubble size is R_bubble = 11.2 pMpc, thus high-Ly α transmission would also be expected. In both cases, we would expect an excess of Ly α detections in neighbouring UV-faint galaxies.
In the BDF field, Vanzella et al. (2011) and Castellano et al. (2018) detected $z \sim 7$ LAEs with $M_{B_V} \sim [-21.1, -20.4, -20.4]$. Two of the galaxies have a projected separation of only 91.3 kpc, and the third is 1.9 pMpc away (Castellano et al. 2018). The photometric overdensity of $z \sim 7$ Lyman-break galaxies within $\sim 3.86$ arcmin$^2$ around these galaxies is $3-4 \times$ times higher than expected (Castellano et al. 2016). Based on the star formation rate and age of the galaxies, and assuming a uniform IGM $\tau_{HI} = 0.5$ surrounding the sources, Castellano et al. (2018) estimated individual bubble sizes of the two galaxies at $\sim 2$ pMpc separation to be $R_{b_{\text{HI}}} < 0.8$ pMpc. We use a 56 arcmin$^2$ survey area (corresponding to the BDF field, where the sources have an angular separation of 6 arcmin; Vanzella et al. 2011) at $z = 7 \pm 0.1$, which is $>3 \times$ overdense (Castellano et al. 2016). We see in Fig. 7 that we expect nearly all regions ($\sim 84$ per cent in our fiducial Gradual model) with this galaxy overdensity to be inside $>1$ pMpc ionized bubbles, enabling significant Ly$\alpha$ escape.

The non-detection of Ly$\alpha$ with equivalent width $>25$ Å in 12 surrounding UV-faint galaxies in this region may thus be surprising, but could be explained by a number of reasons, as discussed by Castellano et al. (2018). For example, even given the predicted most likely bubble size of 4 pMpc, the fraction of transmitted Ly$\alpha$ flux may be only $\sim 60$ per cent for galaxies at the centre of the bubble (Mason & Gronke 2020), thus with deeper spectroscopy Ly$\alpha$ may be detected. It could also be possible that infalling neutral gas in this region resonantly scatters Ly$\alpha$ photons emitted redward of systemic (which look blue in the rest frame of the infalling gas, e.g. Santos 2004; Weinberger et al. 2018; Park et al. 2021). As UV-faint galaxies are likely to be low mass, and thus have a lower H$\text{I}$ column density in the ISM compared to UV-bright galaxies, they may emit more of their Ly$\alpha$ close to systemic redshift, making it more easily susceptible to scattering by infalling gas. Measurements of systemic redshifts for the galaxies in this region may help explain the complex Ly$\alpha$ visibility. Furthermore, given the large photometric redshift uncertainties of the Castellano et al. (2016) sample, it could...
also be possible that the actual galaxy overdensity associated with the three LAEs is smaller, thus the expected bubble size is smaller and the faint galaxies may not lie in the same bubble as the detected LAEs.

### 3.4.2 $\sim$ 8 overdensities in EGS and Abell 2744 fields

The EGS field contains the majority of $z > 7$ LAEs that have been detected to-date (Oesch et al. 2015; Zitrin et al. 2015a; Roberts-Borsani et al. 2016; Tilvi et al. 2020; Jung et al. 2022; Larson et al. 2022; Tang et al. 2023). Among these LAEs, Tilvi et al. (2020), Jung et al. (2022), and Tang et al. (2023) have reported a total of $8 \lesssim M_{\text{UV}} < -20 \approx 7.7$ LAEs, including the $M_{\text{UV}} = -22$ LAE detected by Oesch et al. (2015), within a circle of radius $\approx 1$ pMpc. Jung et al. (2022) estimates the $R_{\text{ion}} < 1.1$ pMpc for the individual galaxies based on the model of Yajima et al. (2018) which relates Ly $\alpha$ luminosity and bubble size. The photometric overdensity around these LAEs has been estimated to be $N/N(\sim) \sim 3.5$ (Leonova et al. 2022).

We calculate the bubble size distributions using a set-up similar to the results of Leonova et al. (2022): an area of 4.5 arcmin$^2$ at $z = 7.7 \pm 0.1$, with a limiting UV magnitude $M_{\text{UV}} > -19.5$. The result is shown in Fig. 7, assuming the neutral fraction $\tau_{\text{HI}}(z = 7.7) = 0.76 \pm 0.09$ (Mason et al. 2019b). We find $\sim 40$ per cent of regions this overdense are in large ionized bubbles in the Gradual model and 70 per cent of regions in the Rapid model. We conclude this region is likely consistent with our consensus picture of reionization. In the Abell 2744 field, Morishita et al. (2023) found no Ly $\alpha$ detections of $\tau_{\text{HI}} \approx 7.89, M_{\text{UV}} > -20$ galaxies. These galaxies are within a circle of radius $\sim 60$ pkpc. This area is $N/N(\sim) \sim 130$ overdense for galaxies with $M_{\text{UV}} > -17.5$ (Ishigaki et al. 2016). Morishita et al. (2023) estimated bubble sizes of $R_{\text{ion}} \approx 0.07-0.76$ pMpc for individual galaxies, based on their ionizing properties derived from rest-frame optical spectroscopy with NIRSpec. We generate the bubble size distributions for a region of $M_{\text{UV}} > -17.5$ galaxies within a volume of $(0.9 \text{cMpc})^3$. A bubble size of $R_{\text{ion}} \approx 1$ pMpc or larger is unexpected for regions as overdense as this in our Gradual model at $\tau_{\text{HI}} \approx 0.8$: we find $p(R > 1 \text{pMpc}) = 0.27$.

The redshifts of sources in the EGS and Abell2744 fields are very similar. However, Ly $\alpha$ has only been detected in the EGS field. We can see in Fig. 7 and Table 1 that our predicted bubble size distributions for EGS are shifted towards higher bubble sizes than in Abell 2744. Although the Abell 2744 region is overdense in UV-faint galaxies, the volume of this region is very small, thus there may not be sufficient ionizing emissivity to produce a large-scale ionized region. Thus non-detection of Ly $\alpha$ in this overdensity is not surprising.

### 3.4.3 $\sim$ 9–11 overdensities in EGS and GOODS-N fields

The highest redshift association of LAEs in the EGS field is a pair at $z \approx 8.7$ (Zitrin et al. 2015b; Larson et al. 2022), which lies $\sim 4$ pMpc apart. The photometric overdensity around these LAEs has been estimated to be $N/N(\sim) \sim 3.5$ (Leonova et al. 2022). We calculate the bubble size distributions using a set-up similar to the results of Leonova et al. (2022): an area of 27 arcmin$^2$ (corresponding to $\sim 6$ HST/WFC3 pointings between the two sources) with $\Delta z = 0.2$, with a limiting UV magnitude $M_{\text{UV}} > -19.5$.

At $z = 8.7$ the inferred IGM neutral fraction is $\tau_{\text{HI}} = 0.93^{+0.02}_{-0.15}$. We predict the probability of finding LAEs at $\tau_{\text{HI}} = 0.9$ should be extremely low: in the full simulation volume in our fiducial Gradual model, we obtain $p(R > 1 \text{pMpc}) = 0.01$ and there is $<0.2$ per cent probability of finding a bubble with $R_{\text{ion}} > 4$ pMpc. Around regions as overdense as that observed we find $p(R > 1 \text{pMpc}) = 0.11$. Thus in our fiducial model, we find it is extremely unlikely that the $z \approx 8.7$ LAE pair in the EGS field are in one large ionized region.

The visibility of Ly $\alpha$ therefore implies some missing aspect in our understanding of this system. First, if $\tau_{\text{HI}}$ is lower, there will be a higher chance to find LAEs: we obtain $p(R > 1 \text{pMpc}) = 0.17$ in regions this overdense if $\tau_{\text{HI}} = 0.8$, so $\tau_{\text{HI}}$ will need to be substantially lower to find a high probability of large ionized regions. Second, in the Rapid model, $p(R > 1 \text{pMpc}) = 0.42$ for such an overdensity, and the bubble size distributions at $\tau_{\text{HI}} = 0.8 - 0.6$ peak at $R_{\text{ion}} \gtrsim 3$ pMpc: the two LAEs could be in one large ionized bubble. Alternatively, the Ly $\alpha$ visibility of these galaxies could be boosted by high intrinsic Ly $\alpha$ production as suggested by their other strong emission lines, and potential contribution of AGN (Stark et al. 2017; Larson et al. 2023; Tang et al. 2023), and facilitated transmission in the IGM if the Ly $\alpha$ flux is emitted redward of systemic (e.g. Dijkstra, Mesinger & Wyithe 2011; Mason et al. 2018b). Additionally, strong ionizing radiation from AGN could potentially boost bubble sizes (Cen & Haiman 2000; Madau & Rees 2000). An AGN with $M_{\text{UV}} \approx -22$ can create a $< 0.8$ pMpc ionized proximity zone using the correlation between $M_{\text{UV}}$ and AGN proximity zone size derived from radiative transfer simulations (Eilers et al. 2017) or from observations (Ishimoto et al. 2020). Thus, a faint AGN in this field could potentially boost the ionized bubble size and enhance Ly $\alpha$ transmission, but evidence for an AGN in this field is still tentative and requires deeper spectroscopy (Larson et al. 2023).

Finally, Bunker et al. (2023) have detected Ly $\alpha$ in GN-z11 at $z = 10.6$, in the GOODS-N field (Oesch et al. 2016). 9 fainter galaxy candidates ($m_{AB} \approx 29$) at similar redshift are found within a $(10 \text{cMpc})^2$ square centred at GN-z11 (Tacchella et al. 2023). We estimate the overdensity of $m_{AB} < 29$ ($M_{\text{UV}} < -18.6$), $z = 10 \pm 0.1$ galaxies in this field using our $z = 10$ UV LF, finding that this region is $\sim 23 \times$ overdense. We obtain $p(R > 1 \text{pMpc}) = 0.07$ and 0.48 in the Gradual and the Rapid model, respectively. It is thus extremely unlikely that all of the $z \sim 11$ galaxies are in one $R > 1$ pMpc ionized region that allows significant Ly $\alpha$ transmission, in our fiducial Gradual model.

We find $R_{\text{ion}} = 0.5$ and 1.1 p.m.p.c in the Gradual and the Rapid model, respectively. The characteristic bubble size is slightly smaller than the largest distance of galaxies from GN-z11 in this field ($\sim 0.6$ pMpc) estimated by Tacchella et al. (2023) from photometric redshifts, implying that most of these galaxies could reside in the same (small) ionized region. If GN-z11 is an AGN (e.g. Bunker et al. 2023; Maiolino et al. 2023), the Ly $\alpha$ visibility in the field could also be enhanced by the AGN-related physics discussed above.

In summary, our simulations demonstrate that the regions discussed above at $z \sim 7$ are extremely likely (> 90 per cent) to be in large ionized bubbles, given their large estimated overdensities. We also find it likely (> 40 per cent) that the EGS region at $z \approx 7.7$ is in a large ionized bubble. However, at higher redshifts we find it very unlikely that the $z \approx 8.7$ Ly $\alpha$ emitters in EGS and the $z \approx 10.6$ galaxies in GOODS-N, including GNz11, are in large ionized regions ($\sim 11$ and $\sim 7$ per cent, respectively) in our fiducial Gradual model.

If the actual overdensities of these regions are smaller than the photometrically estimated values, we will find it even more unlikely for these galaxies to reside in large ionized bubbles, strengthening our result. These results clearly demonstrate the importance of measuring the IGM neutral fraction at $z \gtrsim 8$ and distinguishing between
reionizing source models (e.g. Bruton et al. 2023), of understanding intrinsic Ly α production and escape in the ISM in these galaxies (Roberts-Borsani et al. 2023; Tang et al. 2023), and of understanding the prevalence of AGN at $z > 8$ and their contribution to ionizing their surroundings.

3.5 Forecasts for future observations

Anticipating upcoming large area surveys at $z \geq 7$, we make forecasts for the expected number of large bubbles in the JWST COSMOS-Web survey (Casey et al. 2022), the Euclid Deep survey (Euclid Collaboration et al. 2022; van Mierlo et al. 2022), and the Roman High-Latitude Survey (Wang et al. 2022). These surveys will detect tens of thousands of UV-bright $z > 7$ galaxy candidates which could be used to constrain the underlying density field and pinpoint early nodes of reionization.

The identification and size measurement of ionized regions in these large surveys has the potential to distinguish between reionization models. We sample simulated volumes equivalent to the survey areas (0.6 sq. deg for COSMOS-Web, 53 sq. deg for Euclid-Deep) at $z = 8 \pm 0.1$ and use the watershed algorithm (Section 2.3.2) to identify individual bubbles in these volumes. As we describe below, the bubble size distribution in a Euclid-like survey volume will suffer minimal cosmic variance, thus our Euclid forecast can be rescaled to forecast for the Roman High-Latitude Survey (2000 sq. deg). We show in Appendix B that the expected bubble sizes, in comoving units, do not depend strongly on redshift at fixed neutral fraction, so our results can be easily shifted to other redshifts without expecting significant differences. As discussed above, to reduce oversegmentation, we use the H-minima threshold when calculating the bubble sizes using the watershed algorithm, this sets an effective resolution of 3 cMpc.

In Fig. 8, we plot our predicted ‘bubble size function’ down to this resolution limit: the number density of ionized bubbles as a function of bubble size, for our Gradual and Rapid model at $\tau_{\text{HI}} = [0.5, 0.7, 0.9]$. As the neutral fraction decreases, as above, we expect to find an increasing number of large ionized regions, and the number of small ionized regions decreases as bubbles overlap. Fig. 8 again shows the clear difference in the predicted number and size of ionized regions for the different reionization models, as discussed in Section 3.3. We mark the survey volume of COSMOS-Web and Euclid Deep, $(120 \text{cMpc})^3$ and $(530 \text{cMpc})^3$ at $z = 8$, respectively, as horizontal lines. The survey volume of the Roman High-Latitude survey (not shown) is $(1816 \text{cMpc})^3$. We note that when $\tau_{\text{HI}} \lesssim 0.7$ we expect a significant fraction of bubbles with $R \gtrsim 50$ cMpc (see Figs 3 and 4). COSMOS-Web is thus unlikely to capture the full extent of large ionized bubbles during the majority of reionization. Kaur, Gillet & Mesinger (2020) demonstrated that a simulated volume of $(>250 \text{cMpc})^3$ is required for convergence of the 21-cm power spectrum during reionization, so it is likely that this volume must be observed to be able to robustly measure the bubble size distribution, thus we expect the Euclid Deep and Roman High Latitude surveys can robustly sample the full bubble size distribution.

The number of bubbles with $R \gtrsim 10$ cMpc can be considered a proxy for a cluster of Ly α-emitting galaxies as $\sim 30$–35 per cent of Ly α flux should be transmitted through regions this large (Mason & Gronke 2020) (see Section 3.4). Ly α emission from galaxies inside such large ionized regions is more likely to be detected therefore the number density of Ly α-emitting galaxies and the strength of their clustering will significantly increase relative to galaxies in the whole observed volume (e.g. McQuinn et al. 2007b; Mesinger & Furlanetto 2008b; Sobacchi & Mesinger 2015; Hutter et al. 2023). Our results indicate that counting the number of overdensities of LAEs in a volume could be a useful estimate of the bubble size distribution, as they will probe ionized regions $\gtrsim 1$ cMpc, and thus $\tau_{\text{HI}}$ (especially, at $\tau_{\text{HI}} > 0.5$, before the bubble overlap stage). For example, in our fiducial Gradual model, we expect no $R > 10$ cMpc bubbles in the COSMOS-Web volume when $\tau_{\text{HI}} = 0.9$. This implies detection of clusters of LAEs in this volume at a given redshift would indicate $\tau_{\text{HI}} < 0.9$ (or a reionization morphology similar to our Rapid model). We expect tens of large bubbles in this volume when $\tau_{\text{HI}} < 0.7$. In future work, we will present quantitative methods to infer the sizes of ionized bubbles in single fields using Ly α emission from galaxies (Lu et al., in preparation; Nikolić et al., in preparation), which requires comparison to expected Ly α emission from galaxies pre-IGM absorption (e.g. using empirical models based on $z \sim 6$ observations; Schenker et al. 2012; Pentericci et al. 2014; Mason et al. 2018a; Endsley et al. 2021b). For simplicity, here, we assume $R > 10$ cMpc bubbles could be roughly identified by clusters of Ly α-emitters, as discussed in Section 3.4, as bubbles smaller than this will be very unlikely to transmit substantial Ly α.

However, to detect $R > 10$ cMpc ionized bubbles, requires not only a large survey volume, but sufficient survey depth to detect the high redshift UV-bright galaxies which signpost large ionized regions. Only the Roman Space Telescope (RST) (Akeson et al. 2019) is likely to be able to carry out bubble counting. Zackrisson et al. (2020) study the number of galaxies within a $V_{\text{lim}} = 1000$ cMpc$^3$ bubble that can be detected with upcoming photometric surveys with instruments such as Euclid, JWST, and RST. They found that the Euclid Deep survey can barely detect one $M_{\odot} \approx -21$ galaxy in that volume at $z > 7$ given its detection limit, meaning that identifying large overdensities will be challenging. By contrast, a 20 deg$^2$ deep field observation by RST could detect $\sim 10 M_{\odot} \lesssim 18.5$ galaxies at $z = 7$–10 in a $V_{\text{lim}} = 1000$ cMpc$^3$ volume. The wide survey area ($\approx (400 \text{cMpc})^3$ at $z \sim 8 \pm 0.2$) and survey depth of an
4 DISCUSSION

In the following section, we compare our results to those obtained from other simulations (Section 4.1) and discuss the implications of our results for the reionization history and identifying the primary sources of reionization (Section 4.2).

4.1 Comparison to other simulations

In this work, we characterize the bubble size distributions around typically observed reionization-era galaxies for the first time over the full timeline of reionization. Previously, only the total bubble size distribution has been modelled as a function of the neutral fraction (e.g. Furlanetto & Oh 2005; Mesinger & Furlanetto 2007; McQuinn et al. 2007a; Seiler et al. 2019).

In principle, the full bubble size distribution measured in this work should agree with previous works of similar reionization set-ups. However, as seen in Fig. 10, our mean bubble size is significantly larger than the characteristic bubble size modelled by Furlanetto & Oh (2005). Our bigger size comes from our use of the mean-free-path (MFP) method which is capable of taking into account the size of overlapped bubbles. The Furlanetto & Oh (2005) model underestimates the typical bubble size because they calculate bubbles via the excursion set formalism: as found by Lin et al. (2016), this method can underestimate bubble sizes by an order of magnitude. Our mean bubble size is comparable to those in works which use the mean free path approximation (e.g. Mesinger & Furlanetto 2007; Seiler et al. 2019), modulo minor differences due to different assumptions for the ionizing source population, as expected looking at the difference between our Gradual and Rapid models.

Other works have explored the correlation between ionized bubble size and galaxy luminosity. For example, Geil et al. (2017) and Qin et al. (2022) presented results from the DRAGONS simulation (Poole et al. 2016), finding more luminous galaxies are more likely to reside in large ionized bubbles, and that UV-faint galaxies have a large scatter in their host bubble size, consistent with our results in Section 3.1. However, these works only investigated a single redshift,
IGM neutral fraction and reionizing source model. Furthermore, the DRAGONS simulation is only (100 cMpc)$^3$, meaning that it does not contain large numbers of rare overdensities and UV-bright galaxies (it contains only 2 galaxies as bright as GNZ11; Mutch et al. 2016) and thus, their predicted bubble sizes around UV-bright galaxies were subject to substantial Poisson noise. Yajima et al. (2018) presented a model for the sizes of ionized bubbles around galaxies by modelling cosmological Stronggren spheres around each galaxy (e.g. Shapiro & Giroux 1987; Cen & Haiman 2000), finding more massive and highly star-forming galaxies (and therefore more luminous) lie in larger ionized bubbles than low-mass galaxies. However, this model does not take into account the overlapping of ionized regions, which can happen very early during reionization (e.g. Lin et al. 2016) and thus their bubble sizes will be underestimated.

Our results in Section 3.1 highlight the importance of considering the expected ionized bubble size as a function of $M_{UV}$ calculated using the MFP method. Previous works which used the characteristic bubble size predicted by Furlanetto & Oh (2005) will thus be underestimating the size of ionized bubbles around observed galaxies at fixed neutral fraction. Jung et al. (2020) estimated the ionized bubble size required to explain the drop in Ly $\alpha$ transmission in the GOODS-N field at $z \sim 7.6$, and compared this bubble size to the Furlanetto & Oh (2005) characteristic bubble size as a function of neutral fraction to estimate $\tau_{\text{HI}} = 0.49 \pm 0.19$. Our results in Fig. 10 imply that this approach will lead to an underestimate in $\tau_{\text{HI}}$. This likely explains the discrepancy between the neutral fraction estimated by Jung et al. (2020) and that inferred by Bolan et al. (2022) ($\tau_{\text{HI}} = 0.83^{+0.08}_{-0.11}$) at a similar redshift, which was obtained by sampling sightlines in inhomogeneous IGM simulations.

4.2 Implications for the reionization history and identification of primary ionizing sources

Our results demonstrate that the visibility of Ly $\alpha$ emission at $z > 8$ is unexpected given our consensus timeline for reionization. The visibility of Ly $\alpha$ therefore implies some missing aspect in our understanding of reionization.

As discussed in Section 3.4, there are three possibilities: (1) $\tau_{\text{HI}}$ is lower than previously inferred; (2) reionization is dominated by rarer sources providing larger, rarer bubbles; (3) these galaxies have high-intrinsic Ly $\alpha$ production (Stark et al. 2017; Tang et al. 2023) and facilitated transmission in the IGM if the Ly $\alpha$ flux is emitted redward of systemic (e.g. Dijkstra et al. 2011; Mason et al. 2018b). These scenarios should be testable with spectroscopic observations in the field of high redshift Ly $\alpha$-emitters. The most important first step is confirming if the large regions really are ionized. As the Ly $\alpha$ damping wing due to nearby neutral gas strongly attenuates Ly $\alpha$ close to systemic velocity, detecting Ly $\alpha$ with high escape fraction (estimated from Balmer lines) and very low velocity offset would be a key test to infer if the sources lie in large ionized regions. The $z > 8$ LAEs that have been detected so far have Ly $\alpha$ velocity offset $>300$ km s$^{-1}$ (Bunker et al. 2023; Tang et al. 2023), thus the large ionized regions cannot be confirmed, but spectroscopy of the fainter galaxies (which are more likely to emit Ly $\alpha$ closer to systemic velocity; Prieto-Lyon et al. 2023) in these overdensities could be used to confirm large bubbles. These observations are now possible with JWST/NIRSpec, which can also importantly spectroscopically confirm overdensities. Excitingly, recent observations have discovered strong Ly $\alpha$ at low velocity offsets at $z > 7$, implying large ionized regions (Saxena et al. 2023; Tang et al. 2023), and we will discuss quantitative constraints on the sizes of ionized regions in a future work.

We have also shown that the bubble size distribution around observable galaxies depends on both the average IGM neutral fraction $\tau_{\text{HI}}$ and the reionizing source model. As the characteristic bubble size evolves strongly with $\tau_{\text{HI}}$ (Fig. 10), we may be able to constrain the reionization history by simply counting overdensities of LAEs as a function of redshift. Trapp, Furlanetto & Davies (2023) recently used observed overdensities of LAEs to place joint constraints on the IGM neutral fraction and underlying matter density of those regions. That work is complementary to our approach in that it demonstrates a strong link between the overdensity of a region and the expected size of the ionized region around an overdensity.

In Sections 3.3 and 3.5, we show that the reionizing source models have a strong impact on the predicted number of galaxies in large ionized bubbles early in reionization. Finding evidence for a high-number density of large ionized regions ($>10$ cMpc) at high redshift would thus provide evidence for reionization driven by rare bright sources. However, it is clear from our work that characteristic bubble sizes in different reionization models at different $\tau_{\text{HI}}$ can be degenerate, so focusing purely on observing overdensities likely to reside ionized regions will not be able to break this degeneracy.

As seen clearly in Fig. 1, the Rapid model is characterized by biased, isolated large bubbles, thus it is much more likely that galaxies outside of overdensities will still be in mostly neutral regions early in reionization in this scenario (see Fig. 6). Thus to measure $\tau_{\text{HI}}$ and fully break the degeneracy between reionization morphologies requires observing a range of environments over time during reionization. For example, observing the Ly $\alpha$ transmission from multiple sightlines to galaxies at different redshifts (e.g. Mesinger & Furlanetto 2008b; Mason et al. 2018b; Whitler et al. 2020; Bolan et al. 2022) and the 21-cm power spectrum as a function of redshift (e.g. Furlanetto, Hernquist & Zaldarriaga 2004a; Geil et al. 2016).

5 CONCLUSIONS

We have produced large-scale (1.6 Gpc)$^3$ simulations of the reionizing IGM using 21cmFAST and explored the size distribution of ionized bubbles around observable galaxies. Our conclusions are as follows:

(i) Observable galaxies ($M_{UV} < -16$) and galaxy overdensities are much less likely to reside in neutral regions compared to regions at the mean density. This is because galaxies are the source of reionization.

(ii) The bubble size distribution around UV-bright ($M_{UV} < -20$) galaxies and strong galaxy overdensities is biased to larger characteristic sizes compared to those in the full volume.

(iii) At all stages of reionization, we find a trend of increasing characteristic host bubble size and decreasing bubble size scatter with increasing UV luminosity and increasing overdensity.

(iv) As shown by prior works, we find the bubble size distribution strongly depends on both the IGM neutral fraction and the reionizing source model. The difference between these models is most apparent in the early stages of reionization, $\tau_{\text{HI}} > 0.5$: if numerous faint galaxies drive reionization, we expect a gradual reionization with numerous small bubbles, whereas if bright galaxies drive reionization, we expect a more rapid process characterized by larger bubbles biased around only the most overdense regions, with sizes $>30$ cMpc even in a 90 per cent neutral IGM.

(v) We use our simulations to interpret recent observations of galaxy overdensities detected with and without Ly $\alpha$ emission at $z > 7$. We find the probability of finding a large ionized region with $R_{\text{ion}} > 1$ pMpc, capable of transmitting significant Ly $\alpha$ flux, at $z \approx$...
7–8 is high (≥40–93 per cent) for large-scale galaxy overdensities, implying that Lyα-emitting galaxies detected at these redshifts are very likely in large ionized regions.

(vi) We find a very low probability of the $z \approx 8.7$ association of Lyα emitters in the EGS field and the $z = 10.6$ galaxy GNz11, also detected with Lyα emission, to be in a large ionized bubble ($\sim 11$ and $\sim 7$ per cent, respectively). The Lyα detections at such a high redshift could be explained by either: a lower neutral fraction ($\tau_{\HI} < 0.8$) than previously inferred; or if UV bright galaxies drive reionization or if bubble sizes are enhanced by potential AGNs in the fields, which would produce larger bubbles; or if the intrinsic Lyα production in these galaxies is unusually high.

(vii) We make forecasts for the number density of ionized bubbles as a function of bubble size expected in the JWST COSMOS-Web survey and the Euclid Deep survey. Our fiducial model predicts no ionized regions >10 cMpc in the COSMOS-Web volume unless $\tau_{\HI} < 0.9$, with tens of large bubbles expected by $\tau_{\HI} < 0.7$, though with large cosmic variance. We find Euclid and Roman wide-area surveys will have sufficient volume to cover the size distribution of ionized regions with minimal cosmic variance and should be able to detect the UV-bright galaxies which signpost overdensities. Deeper photometric and spectroscopic follow-up around UV-bright galaxies in these surveys to confirm overdensities and Lyα emission could be used to infer $\tau_{\HI}$ and discriminate between reionization models.

Our simulations show that in interpreting observations of $z > 6$ galaxies, it is important to consider the galaxy environment. We showed the bubble size distribution around observable galaxies and galaxy overdensities can be significantly shifted from the bubble size distribution over the whole cosmic volume. This motivates using realistic inhomogeneous reionization simulations, or at least tailored bubble size distributions to interpret observations.

Our results imply that the early stages of reionization are still very uncertain. Identifying and confirming large ionized regions at very high redshift is a first step to understanding these early stages, and thus the onset of star formation. This is now possible with deep JWST/NIRSpec observations which could map the regions around $z > 8$ Lyα emitters. The detection of Lyα with high escape fraction and low velocity offset from other galaxies in the observed $z > 8$ overdensities could confirm whether the Lyα emitters at $z > 8$ are tracing unexpectedly large ionized regions (e.g. Saxena et al. 2023; Tang et al. 2023).

ACKNOWLEDGEMENTS

The authors thank the anonymous referee for insightful comments. TYL, CAM, and AH acknowledge support by the VILLUM FONDEN under grant 37459. The Cosmic Dawn Center (DAWN) is funded by the Danish National Research Foundation under grant DNRF140. This work has been performed using the Danish National Life Science Supercomputing Center, Computerne. Part of this research was supported by the Australian Research Council Centre of Excellence for All Sky Astrophysics in 3 Dimensions (ASTRO 3D), through project #CE170100013.

DATA AVAILABILITY

Tables of bubble sizes as a function of $\tau_{\HI}$, $M_{15}$, and galaxy overdensity (using the same volume as in Section 3.2) are publicly available here: https://github.com/ting-ji-ju/bubble_size_overdensities_paper.

Bubble size distributions around other overdensities can be distributed upon reasonable request to the authors.

REFERENCES


Bouwens R. J. et al., 2021, AJ, 162, 47


Castellano M. et al., 2018, APL, 863, L3


Dijkstra M., 2014, PASA, 31, e040


Hu W. et al., 2021, Nat. Astron., 5, 485


Figure A1. UV luminosity functions from our model at $z \sim 7, 8, 9$ (solid lines) in comparison to HST measurements of the UV LF by Bouwens et al. (2021) ($z = 7-9$) and Oesch et al. (2018) ($z = 10$).

APPENDIX B: BUBBLE SIZE DISTRIBUTIONS AT DIFFERENT REDSHIFTS

Here, we compare the bubble size distributions at $z = 7-9$. We show the bubble size distributions at $\tau_{\text{HI}} = 0.5$ for each redshift in Fig. B1. We see negligible differences as a function of redshift, but that bubble sizes are slightly larger at fixed neutral fraction at higher redshift. This is because we use a fixed halo mass cut-off to calculate the ionizing emissivity (as described in Section 2.1), and at higher redshifts, the same mass halo will be more biased, resulting in rarer larger bubbles at fixed $\tau_{\text{HI}}$ as in our Rapid model. However, the difference between the bias of haloes of fixed mass and different redshifts is much lower than the difference between the bias due to our two mass thresholds for the Gradual and Rapid model, so this redshift effect is minimal.

APPENDIX C: BUBBLE SIZE DISTRIBUTION MODELS FOR OBSERVED OVERDENSITIES

In Fig. C1, we show the bubble size distribution for the observed overdensities described in Section 3.4. In all plots, we show the bubble size distribution in the full volume in the neutral fraction range expected given current constraints on reionization (Mason et al. 2019b), and the bubble size distribution in regions as overdense as those observed.
Figure C1. Bubble size distributions for the same overdensity observation set-ups as the COSMOS (top panel), BDF (second panel), EGS,z8 (third panel), Abell2744 (fourth panel), EGS,z9 (fifth panel), and GOODS-N (bottom panel), at the IGM neutral fractions expected at these redshifts (Mason et al. 2019b), from the Gradual (solid) and Rapid (dashed) models. The bubble size estimated by previous works (Castellano et al. 2016; Endsley et al. 2023; Jung et al. 2022; Leonova et al. 2022; Morishita et al. 2023; Tacchella et al. 2023) are marked with purple vertical lines. A summary of our simulation set-up is given in Table 1.

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