Study of flavor dependence of the baryon-to-meson ratio in proton-proton collisions at \( s=13 \) TeV

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Study of flavor dependence of the baryon-to-meson ratio in proton-proton collisions at $\sqrt{s} = 13$ TeV

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The production cross sections of $D^0$ and $\Lambda_c^+ \Lambda_c^-$ baryons originating from beauty-hadron decays (i.e., nonprompt) were measured for the first time at midrapidity ($|y| < 0.5$) by the ALICE Collaboration in proton-proton collisions at a center-of-mass energy $\sqrt{s} = 13$ TeV. They are described within uncertainties by perturbative QCD calculations employing the fragmentation fractions of charm quarks into baryons measured at forward rapidity by the LHCb Collaboration. The $b\bar{b}$ production cross section per unit of rapidity at midrapidity, estimated from these measurements, is $d\sigma_{b\bar{b}}/dy|_{|y|<0.5} = 83.1 \pm 3.5(\text{stat}) \pm 5.4(\text{syst})^{+1.3}_{-1.2}(\text{extrap}) \mu b$. The baryon-to-meson ratios are computed to investigate the hadronization mechanism of beauty quarks. The nonprompt $\Lambda_c^+/D^0$ production ratio has a similar trend to the one measured for the promptly produced charmed particles and to the $p/\pi^+$ and $\Lambda/K^0_S$ ratios, suggesting a similar baryon-formation mechanism among light, strange, charm, and beauty hadrons. The $p_T$-integrated nonprompt $\Lambda_c^+/D^0$ ratio is found to be significantly higher than the one measured in $e^+e^-$ collisions.

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I. INTRODUCTION

Measurements of open charm- and beauty-meson production in proton-proton (pp) collisions are successfully described by quantum chromodynamics (QCD) calculations based on the factorization of soft (nonperturbative) and hard (perturbative) processes [1–12]. Within the collinear factorization approach, the production cross sections of heavy-flavor hadrons are computed as the convolution of (i) the parton distribution functions (PDFs) of the incoming protons, (ii) the perturbative partonic cross section, and (iii) the fragmentation functions (FFs) describing the transition from the heavy quark to the hadron. The partonic cross section in these calculations is typically computed at next-to-leading order accuracy with all-order resummation of next-to-leading logarithms (e.g., FONLL [13–15] and GM-VFNS [16–21]), but recently calculations at next-to-next-to-leading order (NNLO) also became available [22]. The FFs are instead parametrized from measurements performed in $e^+e^-$ or ep collisions [23], assuming that the hadronization process of charm and beauty quarks is independent of the collision system.

Recent measurements of charm baryon-to-meson production ratios and fragmentation fractions (i.e., the probability of charm quark to fragment into a specific hadron) at midrapidity in pp collisions at LHC energies showed significant deviations from the values measured at $e^+e^-$ and ep colliders [24–32], demonstrating that the assumption of universality of the hadronization process across the collision systems has to be reconsidered. As reported in Ref. [30], the observed baryon-to-meson enhancement also leads to an increase of the derived $c\bar{c}$ production cross section at midrapidity compared to previous measurements, where prompt D-meson cross sections and fragmentation fractions from $e^+e^-$ were used. Models based on the hadronization via coalescence, i.e., recombination of heavy and light quarks close in space and with similar velocity, are able to reproduce the magnitude as well as the $p_T$ dependence of the measured $\Lambda_c^+/D^0$ ratio [33,34]. An alternative explanation is provided by statistical hadronization models, if an augmented set of yet unobserved charm-baryon states predicted by the relativistic-quark model [35] and lattice QCD [36] is considered. Moreover, string fragmentation models including color-reconnection mechanisms beyond the leading-color (CLR-BLC) approximation introduce new topologies through the contributions of “junctions” that fragment into baryons, thus providing an augmented baryon production [37]. In the beauty sector, the measurements of $\Lambda_b^0$-baryon production relative to that of $B$ mesons at forward rapidity by the LHCb Collaboration show a modification of the fragmentation fractions among collision systems similar
to that observed for charm quarks at midrapidity [38,39]. However, the rapidity-dependent baryon-to-meson enhancement with respect to values measured at e⁺e⁻ and ep colliders is still not fully understood and explored. Different enhancement was observed for the charm baryonto-meson ratio between midrapidity and forward rapidity for p_T < 8 GeV/c and for different colliding systems (i.e., pp, p–Pb) [27,40,41]. Beauty measurements at midrapidity are available only at high transverse momentum (p_T > 7 GeV/c) [5,42–48], hence a firm conclusion cannot be drawn.

In this article, the first measurements of the p_T-differential and p_T-integrated production cross sections of D⁰ mesons and Λ_c⁺ baryons at midrapidity (|y| < 0.5) originating from beauty-hadron decays (denoted as nonprompt) in pp collisions at a center-of-mass energy of √s = 13 TeV are reported. The differential measurements performed in 1 < p_T < 24 GeV/c and 2 < p_T < 44 GeV/c for D⁰ and Λ_c⁺ hadrons, respectively, are extrapolated down to p_T = 0 to compute the p_T-integrated production cross sections and compute the bb production cross section at midrapidity. Finally, the nonprompt Λ_c⁺/D⁰ production ratio is compared with the production ratio of prompt Λ_c⁺ and D⁰, with the p/π⁺ and Λ/K⁺ ratios, as well as with predictions based on the statistical hadronization model TAMU [49] or the PYTHIA8 Monte Carlo (MC) generator [50] to investigate the hadronization mechanisms of beauty quarks into baryons and mesons.

II. EXPERIMENTAL APPARATUS AND DATA SAMPLE

The description of the ALICE apparatus and of its performance is presented in detail in Refs. [51,52]. The detectors used for the reconstruction of nonprompt charm-hadron decays are the inner tracking system (ITS), the time projection chamber (TPC), and the time-of-flight detector (TOF). These are located in the central barrel, which covers the pseudorapidity interval |η| < 0.9 inside a solenoid magnet of field strength B = 0.5 T. The ITS and the TPC are used for tracking charged particles and reconstructing particle decay vertices. Particle identification (PID) is performed via the measurement of the specific energy loss dE/dx in the TPC and of the flight time with the TOF detector.

The data used for this analysis were collected during pp collisions at √s = 13 TeV, with a minimum bias (MB) trigger. The latter requires coincident signals in the two scintillator arrays covering the intervals 2.8 < η < 5.1 (V0A) and −3.7 < η < −1.7 (V0C). Offline selections were applied to remove background from beam–gas collisions, as described in Ref. [27]. Only events with a primary vertex reconstructed within ±10 cm from the nominal interaction point along the beam line were analyzed. Events with multiple primary vertices were rejected in order to remove collision pileup in the same bunch crossing. The remaining undetected pileup is negligible. The selected events correspond to an integrated luminosity L_int = 31.9 ± 0.5 nb⁻¹ [53].

III. DATA ANALYSIS

A. D⁰ and Λ_c⁺ raw yields

The D⁰ meson, Λ_c⁺ baryon, and their charge conjugates were reconstructed via the hadronic decay channels D⁰ → K⁻π⁺ (branching ratio BR = 3.95 ± 0.03%), Λ_c⁺ → pK⁰ (BR = 1.59 ± 0.08%, followed by K⁰ → π⁺π⁻ with a BR of 69.20 ± 0.05%), and Λ_c⁺ → pK⁻π⁺ (BR = 6.28 ± 0.32%) [54]. The D⁰ -meson and Λ_c⁺ -baryon candidates were reconstructed by combining pairs or triplets of tracks reconstructed with the proper charge, while for the Λ_c⁺ → pK⁰ channel the V-shaped decay of the K⁰ meson into two pion-track candidates was combined with a proton-track candidate, using a Kalman-Filter vertexing algorithm [55]. All daughter tracks were required to be reconstructed within |η| < 0.8 and to have at least 70 reconstructed space points in the TPC. For all decay products, at least one cluster was required in either of the two SPD layers. As a consequence of these track-quality selections, the detector acceptance for the candidates falls steeply to zero for |y| > 0.5 at p_T ≈ 0 and at |y| ≈ 0.8 for p_T > 5 GeV/c. Thus, a fiducial-acceptance selection |y| < yfid(p_T) was applied, increasing from 0.5 at p_T = 0 to the maximum value of 0.8 at p_T ≥ 5 GeV/c.

A multi-class classification approach based on Boosted Decision Trees (BDT) algorithms provided by the XGBoost [56,57] library, was used to simultaneously reduce the combinatorial background, and to separate the prompt and nonprompt components for D⁰ mesons and Λ_c⁺ baryons. Indeed, the inclusive sample of D⁰ and Λ_c⁺ is dominated by the prompt hadrons and the nonprompt ones are a small fraction which can be enhanced exploiting the larger displacement due to the beauty-hadron decay topology. Signal samples of prompt and nonprompt candidates for the BDT training were obtained from MC simulations produced with the PYTHIA8.243 [50] event generator with the Monash 2013 tune [58]. The generated particles were propagated through the ALICE apparatus using the GEANT3 transport code [59]. Background samples were extracted from the candidate invariant-mass distributions inside the window of 5σ < |ΔM| < 9σ in data, where ΔM is the difference between the candidate invariant mass and the D⁰ (Λ_c⁺) mass, and σ is the invariant-mass resolution. Loose selections on the decay kinematics, the decay topology, and the PID of the decay particles were applied to the candidates before the training. The BDTs were trained in each p_T interval using different variables related to the displaced decay-vertex topology and the PID of the decay tracks, similarly as described in Refs. [2,60]. The BDT outputs are related to the candidate’s probability to be either prompt or nonprompt D⁰ (Λ_c⁺) meson (baryon) or...
combinatorial background. Selections on the BDT output probabilities of being background and nonprompt were optimized to obtain a high nonprompt D⁰ and Λ⁺ₘ fractions (i.e., ≥60% in each p_T interval) while maintaining a reliable signal extraction. The sample of candidates passing the BDT selection is denoted in the following as nonprompt enhanced sample. Based on the selections on the BDT outputs, samples dominated by nonprompt (prompt) candidates were selected by requiring low BDT probability for a candidate to be combinatorial background and a high BDT probability to be nonprompt (prompt).

The D⁰ -meson and Λ⁺ₘ -baryon raw yields were extracted via binned maximum-likelihood fits to the candidate invariant-mass distributions. The fitting function was composed of a Gaussian term to model the signal and an exponential or polynomial function to model the background. In the case of D⁰ mesons, an additional term was added for the contribution of signal candidates with the wrong K − π mass assignment (reflections), parametrized from simulated candidates [1]. To improve the stability of the fits, the widths of the signal peaks were fixed to the values extracted from the fits of the invariant-mass distributions in the prompt enhanced sample, given the naturally larger abundance of prompt compared to nonprompt contributions in the prompt enhanced sample, given the value extracted from the fits of the invariant-mass distributions. The fitting function was minimized to obtain the corrected yields of prompt and nonprompt D⁰ or Λ⁺ₘ hadrons as follows

\[
\begin{align*}
\frac{f_{\text{corrected}}}{f_{\text{raw}}} & = \frac{N_{\text{prompt}}}{N_{\text{nonprompt}}} \left( \frac{0.9}{\epsilon_{\text{prompt}}} \right) \\
& \times \left( \frac{\chi^2_{\text{prompt}}}{\chi^2_{\text{nonprompt}}} \right) \times \left( \frac{\epsilon_{\text{prompt}}}{\epsilon_{\text{nonprompt}}} \right) \times \left( \frac{N_{\text{corrected}}}{N_{\text{raw}}} \right) \\
\end{align*}
\]

where δ represents a residual that accounts for the equation not holding exactly due to the uncertainties of \( Y_i \), \( (\text{Acc} \times e)_{i}^{\text{prompt}} \), and \( (\text{Acc} \times e)_{i}^{\text{nonprompt}} \). In the case of \( n \geq 2 \) sets, a \( \chi^2 \) function can be defined based on Eq. (2), which can be minimized to obtain the corrected yields of prompt \( (N_{\text{prompt}}) \) and nonprompt \( (N_{\text{nonprompt}}) \) Λ⁺ₘ (D⁰) hadrons as explained in Ref. [2]. One of the \( n \) sets with a high nonprompt component (larger than 50%) was selected as a working point (default), and the corresponding \( f_{\text{non-prompt, default}} \) fraction (more details in Ref. [2]) can be calculated as

\[
\begin{align*}
\frac{f_{\text{non-prompt, default}}}{f_{\text{prompt, default}}} & = \left( \frac{(\text{Acc} \times e)_{i}^{\text{nonprompt}}}{(\text{Acc} \times e)_{i}^{\text{default}}} \right) \times \left( \frac{N_{\text{corrected}}}{N_{\text{raw}}} \right) \times \left( \frac{\chi^2_{\text{corrected}}}{\chi^2_{\text{raw}}} \right) \\
& \times \left( \frac{\epsilon_{\text{corrected}}}{\epsilon_{\text{raw}}} \right) \times \left( \frac{N_{\text{corrected}}}{N_{\text{raw}}} \right) \times \left( \frac{\chi^2_{\text{corrected}}}{\chi^2_{\text{raw}}} \right) \times \left( \frac{\epsilon_{\text{corrected}}}{\epsilon_{\text{raw}}} \right) \\
\end{align*}
\]

Figure 2 shows an example of raw-yield distribution as a function of the BDT-based selection employed in the minimization procedure for D⁰ in \( 2 < p_T < 4 \text{ GeV}/c \) (top left panel), Λ⁺ₘ → pK⁺π⁻ in \( 4 < p_T < 6 \text{ GeV}/c \) (top right panel), and Λ⁺ₘ → pK₀S in \( 6 < p_T < 8 \text{ GeV}/c \) (bottom panel). The black markers are the measured raw yields corresponding to a selection on the BDT output related to the candidate’s probability of being a nonprompt D⁰ (Λ⁺ₘ) meson (baryon). The leftmost data point of each distribution corresponds to the loosest applied selection, while the rightmost one corresponds to the tightest selection, which preferentially selects nonprompt candidates. The prompt and nonprompt components, obtained for each
BDT-based selection from the minimization procedure as $(\text{Acc} \times e)_{i}^{\text{prompt}} \times N_{\text{prompt}}$ and $(\text{Acc} \times e)_{i}^{\text{nonprompt}} \times N_{\text{nonprompt}}$, are represented by the red and blue filled histograms, respectively, while their sum is reported by the green histogram. The $f_{\text{nonprompt}}$ fractions obtained for $D^{0}$, $\Lambda^{+} \to pK^{-}\pi^{+}$, and $\bar{\Lambda}^{0} \to pK^{0}S$, computed for the default selections with the formula in Eq. (3) are reported as a function of $p_{T}$ in the bottom right panel of Fig. 2.

**FIG. 1.** Invariant-mass distributions of the $D^{0}$- and $\Lambda^{+}$-hadron candidates and their charge conjugates produced in pp collisions at $\sqrt{s} = 13$ TeV and reconstructed at midrapidity, shown in a selected $p_{T}$ range. The values for the Gaussian mean $\mu$, width $\sigma$, and raw yield $S$ are reported. Top row: $D^{0} \to K^{-}\pi^{+}$ meson candidates measured in the $2 < p_{T} < 4$ GeV/$c$ interval. Middle row: $\Lambda^{+} \to pK^{0}$ baryon candidates measured in the $2 < p_{T} < 4$ GeV/$c$ interval. Bottom row: $\bar{\Lambda}^{0} \to pK^{0}\pi^{+}$ baryon candidates measured in the $2 < p_{T} < 4$ GeV/$c$ interval. The corresponding BDT probability minimum threshold for the candidate selection is reported. The left (right) column corresponds to the prompt (nonprompt) $D^{0}$- and $\Lambda^{+}$-hadron candidates enriched sample.
IV. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties of the nonprompt $\Lambda^+_c$ and $D^0$ cross sections were studied for the different decay channels, which depend on $p_T$. The contributions from the raw-yield extraction were evaluated by repeating the invariant-mass fits, varying the fit interval, the functional form of the background fit function, and the width of the Gaussian function used to model the signal peaks. The latter was varied within the uncertainties obtained from the fits of the invariant-mass distributions of the prompt enhanced sample. The relative uncertainty from this contribution varies in the range 1%–3% for $D^0$ and 4%–11% for $\Lambda^+_c$. The uncertainties of the track reconstruction efficiency were estimated by considering the uncertainty due to track quality selections and the uncertainty due to the TPC–ITS track matching efficiency as discussed in Ref. [2]. It ranges from 3.5% to 5% for $D^0$ and from 4% to 7% for $\Lambda^+_c$. The systematic uncertainties of the nonprompt fractions were evaluated by varying the configuration and the number of BDT selections employed in the data-driven method and amounts to 2%–3% for $D^0$ and 5%–9% for $\Lambda^+_c$. The selection efficiency uncertainties, ranging from 2% to 4% for $D^0$ and 4% to 10% for $\Lambda^+_c$, were studied by repeating the analyses using different BDT working points. The systematic uncertainties of the PID selection efficiency were found to be negligible, similar to what observed for prompt charm hadrons [60]. The systematic effects due to a possible difference between the real and simulated charm and beauty hadron $p_T$ spectra, were estimated by evaluating the selection efficiency after reweighting the $p_T$ shape from the PYTHIA8.243 event generator to match the one from FONLL calculations [13–15] for prompt and nonprompt $D^0$. For the $\Lambda^+_c$ the reweighting was defined to match the $p_T$ shape of $D^0$ and B

FIG. 2. Raw-yield distribution as a function of the BDT-based selection employed in the $\chi^2$-minimization procedure adopted for the determination of $f_{\text{nonprompt}}$ of $D^0$ in $2 < p_T < 4$ GeV/c (top left panel), $\Lambda^+_c \rightarrow pK^-\pi^+$ in $4 < p_T < 6$ GeV/c (top right panel), and $\Lambda^+_c \rightarrow pK^0_S$ in $6 < p_T < 8$ GeV/c (bottom left panel). Bottom right panel: $f_{\text{nonprompt}}$ fraction as function as $p_T$ obtained for the set of selection criteria adopted in the analysis of for nonprompt $D^0$, $\Lambda^+_c \rightarrow pK^-\pi^+$, and $\Lambda^+_c \rightarrow pK^0_S$ hadrons.
mesons from FONLL multiplied by the $\Lambda^+_c/D^0$ yield ratio from ALICE [27] and the $\Lambda^0_c/B$ yield ratio from LHCb [39], respectively. The weights were applied to the $p_T$ distributions for prompt hadrons and to the mother beauty-hadron particles in the case of nonprompt hadrons. The systematic uncertainty from this contribution varies in the range 1%–4% for $D^0$ and 4–5% for $\Lambda^+_c$. In addition, the imperfect apparatus material budget description in the MC simulation, particularly relevant for the effects of the absorption of protons, might result in a bias in the estimation of the $\Lambda^+_c$ efficiencies. It was evaluated by comparing the corrected yields of charged pions, kaons, and protons using a standard MC production and one with the material budget increased artificially by 10%. The assigned systematic uncertainty is 2%. Further $p_T$-independent uncertainties from the BR [61] and the luminosity [53] were considered. The total uncertainties, 5%–8% for $D^0$ and 12%–17% for $\Lambda^+_c$, were calculated as the quadratic sum of the contributions of the different sources.

V. RESULTS

A. Production cross sections

The $p_T$-differential production cross sections of nonprompt $\Lambda^+_c$ baryons and $D^0$ mesons are shown in Fig. 3. The nonprompt $\Lambda^+_c$ cross section was obtained by computing a weighted average of the results from the analyses of the $\Lambda^+_c \rightarrow pK^0_S$ and $\Lambda^+_c \rightarrow pK^-\pi^+$ decay channels, using the inverse of the quadratic sum of the relative statistical and uncorrelated systematic uncertainties as weights. The systematic uncertainties related to the tracking, luminosity, and generated $p_T$ spectrum in the MC simulations are treated as correlated between the two decay channels, the uncertainty of the branching ratios as partially correlated as described in Ref. [54], while all the other sources of systematic uncertainties are considered uncorrelated. The data points are compared with theoretical models based on the B-meson cross section predicted by FONLL calculations in the left panel and to the TAMU statistical hadronization model [49] in the right panel. In the FONLL-based predictions, the beauty-quark fragmentation fraction to $B$ mesons, $f(b \rightarrow B)$, was taken from $e^+e^-$ collisions [54]. For the $\Lambda^0_c$ baryon, $f(b \rightarrow B)_{e^+e^-} \times (f(b \rightarrow \Lambda^0_c)/f(b \rightarrow B))_{LHCb}$ was used, where the $p_T$-differential ratio $\Lambda^0_c/B$ was measured by the LHCb Collaboration in pp collisions [39]. It has to be noted that the usage of the $p_T$-differential fragmentation fractions ratio $(f(b \rightarrow \Lambda^0_c)/f(b \rightarrow B))_{LHCb}$ combined with the $f(b \rightarrow B)$ from $e^+e^-$ collisions enlarges the total beauty production cross section compared to the one predicted by FONLL calculations. In the TAMU model instead, the branching fractions of beauty quarks to the different hadron species are assumed to follow the relative thermal densities calculated.

FIG. 3. $p_T$-differential production cross sections of nonprompt $D^0$ and $\Lambda^+_c$ hadrons in pp collisions at $\sqrt{s} = 13$ TeV compared with predictions obtained with FONLL calculations [13–15] adopting $f(b \rightarrow B)$ and $f(b \rightarrow \Lambda^0_c)$ fragmentation fractions measured in $e^+e^-$ collisions [61] and LHCb Collaboration [39] (left panel) and the TAMU model [49] (right panel) combined with PYTHIA8 [50,58] for the $h_b \rightarrow h_c + X$ decay kinematics.
with the statistical hadronization model and an enriched set of heavy-flavor hadron states is obtained from the relativistic-quark model [35]. The $p_T$ distribution is obtained from the one of beauty quarks, convoluted to the fragmentation functions as implemented in FONLL calculations. In this case, the $b\bar{b}$ production cross section at midrapidity is a parameter of the model, fixed to $d\sigma_{b\bar{b}}/dy|_{y}=0=85.3$ mb.

The resulting beauty-hadron cross sections of both models were then folded with the $h_b \to h_c + X$ decay kinematics (where $h_c$ and $h_b$ denote a generic hadron species containing either a charm or beauty quark) and branching ratios provided by the PYTHIA8 decayer, in order to obtain the nonprompt $D^0$ and $\Lambda^+_c$ cross sections. In the left panel, the uncertainties in the model are those of the FONLL calculation, which arise from the choice of the normalization and factorization scales, and the mass of the beauty quark, combined with the uncertainties of the cTEQ6.6 PDFs. The nonprompt $D^0$ cross section is in agreement with FONLL + PYTHIA8 and TAMU + PYTHIA8 predictions over the whole $p_T$ range, while the nonprompt $\Lambda^+_c$ cross section shows a hint of underestimation at low $p_T$ ($2 < p_T < 4$ GeV/c) by both models.

The measured visible cross sections of nonprompt $\Lambda^+_c$ and $D^0$ hadrons were computed by integrating the measured $p_T$-differential cross sections in the measured $p_T$ range. All the systematic uncertainties were propagated as fully correlated among the measured $p_T$ intervals, except for the raw-yield extraction uncertainty. As the $p_T$-differential cross sections predicted by FONLL + PYTHIA8 were found to be compatible with the measurements, they were assumed to provide an accurate description of the $p_T$ shape also outside of the measured $p_T$ range. Therefore, the visible cross section was then extrapolated to the full $p_T$ range, using an extrapolation factor computed as the ratio of the $p_T$-integrated cross sections predicted by FONLL + PYTHIA8 integrated over $p_T > 0$ and that in the measured $p_T$ interval. The systematic uncertainty of the extrapolation factors was computed considering (i) the FONLL uncertainties, (ii) the $f(b \to h_b)$ fragmentation fractions uncertainties, and (iii) the branching ratios uncertainties of the $h_b \to h_c + X$ decays. The second source was estimated by using different sets of beauty fragmentation fractions (from $e^+e^-$, $p\bar{p}$ collisions [54], or those measured by LHCb [39]), while for the third one the branching ratios implemented in PYTHIA8 were reweighted in order to reproduce the measured values reported in Ref. [54].

Extrapolation factors are $\alpha_{\text{extrap}}^{D^0} = 1.241_{-0.037}^{+0.009}$ and $\alpha_{\text{extrap}}^{\Lambda^+_c} = 1.847_{-0.152}^{+0.108}$ for $D^0$ mesons and $\Lambda^+_c$ baryons, respectively. The $p_T$-integrated cross sections are reported in Table I and compared to FONLL + PYTHIA8 calculations, which describe the measurements within the uncertainties.

Similarly, the $b\bar{b}$ production cross section per unit of rapidity at midrapidity was obtained summing the visible cross sections previously computed and then using an extrapolation factor to account for the unmeasured $p_T$ regions and hadrons. This factor was computed as the ratio of the beauty cross section and the visible cross section of a nonprompt charm hadron, estimated with FONLL + PYTHIA8 as follows

$$\alpha_{b\bar{b}}^\text{extrap} = \frac{d\sigma_{b\bar{b}}^\text{FONLL}/dy|_{|y|<0.5}}{d\sigma_{h_b\to h_c}^{\text{PYTHIA8}}/dy|_{|y|<0.5}(p_T^{\text{min}}<p_T<p_T^{\text{max}})}.$$  \hspace{1cm} (4)

The extrapolation factor for the $D^0$ meson was found to be $\alpha_{b\bar{b}}^{D^0} = 2.106_{-0.014}^{+0.366}$, while the one for $\Lambda^+_c$ baryons $\alpha_{b\bar{b}}^{\Lambda^+_c} = 10.98_{-1.34}^{+0.87}$. The systematic uncertainty of the extrapolation factor includes the same sources considered for the extrapolation of the single-hadron production cross sections. In addition, a correction due to the difference between the rapidity distributions of beauty quarks and beauty hadrons, and between the $b\bar{b}$ pairs and beauty quarks, was applied. The first factor was evaluated to be unity in the relevant rapidity range based on FONLL calculations with 1% uncertainties evaluated from the difference between FONLL and PYTHIA8. The second correction factor is the ratio $(d\sigma_{b\bar{b}}/dy)/(d\sigma_{b\bar{b}}/dy) = 1.06 \pm 0.01$ in $|y| < 0.5$, which was estimated from POWHEG simulations [62].

The uncertainty was assigned by varying the factorization and renormalization scales in the POWHEG calculation and using the CT10NLO [63] and CT14NLO [64] PDFs, alternatively to the default one (cTEQ6.6). The $d\sigma_{b\bar{b}}/dy$ was computed separately from the measurements of nonprompt $D^0$ and $\Lambda^+_c$ hadrons were then averaged using the inverse of the quadratic sum of the absolute statistical and uncorrelated systematic uncertainties as weights. The systematic uncertainties related to the tracking uncertainty and the extrapolation uncertainties related to FONLL and the beauty fragmentation fractions were treated as fully correlated among the two hadron species, while all the

### Table I. Production cross sections at midrapidity per unit of rapidity $(d\sigma/dy)_{|y|<0.5}$ in pp collisions at $\sqrt{s} = 13$ TeV of nonprompt $\Lambda^+_c$ and $D^0$ hadrons and $b\bar{b}$ pairs $(d\sigma_{b\bar{b}}/dy)_{|y|<0.5}$ compared to pQCD calculations [13–15,22].

<table>
<thead>
<tr>
<th>Measurement (mb)</th>
<th>FONLL (mb) [13–15]</th>
<th>NNLO (mb) [22]</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D^0$</td>
<td>$41.3 \pm 1.5$ (stat) $\pm 2.9$ (syst) $^{+0.3}_{-0.2}$ (extrap)</td>
<td>$34 \pm 14$</td>
</tr>
<tr>
<td>$\Lambda^+_c$</td>
<td>$19.1 \pm 2.3$ (stat) $\pm 1.7$ (syst) $^{+1.0}_{-1.5}$ (extrap)</td>
<td>$11^{+7}_{-5}$</td>
</tr>
<tr>
<td>$b\bar{b}$</td>
<td>$83.1 \pm 3.5$ (stat) $\pm 5.4$ (syst) $^{+12.3}_{-3.2}$ (extrap)</td>
<td>$65^{+28}<em>{-26}$ $72^{+22}</em>{-20}$</td>
</tr>
</tbody>
</table>
other sources as uncorrelated. The resulting $b\bar{b}$ production cross section per unit of rapidity at midrapidity is compatible with the predictions from FONLL and NNLO calculations, as reported in Table I. The NNLO predictions are however closer to the measurement and have smaller uncertainties than the FONLL ones, as expected by the higher perturbative accuracy. The measurement is also compatible with previous estimates based on the measurements of dielectrons [65,66] and nonprompt $J/\psi$-mesons [3].

Figure 4 shows the $b\bar{b}$ production cross section per unit rapidity at midrapidity estimated from the production cross sections of nonprompt $D^0$ and $\Lambda^+_c$ hadrons in pp collisions at $\sqrt{s} = 13$ TeV compared to the previous values based on dielectron and nonprompt $J/\psi$-meson measurements. The experimental results are also compared with the predictions provided by FONLL and NNLO perturbative QCD calculations.

### B. Baryon-to-meson ratios

The ratio of the $p_T$-differential production cross sections of nonprompt $\Lambda^+_c$ and $D^0$ hadrons is shown in Fig. 5. In the left panel, the data are compared with theoretical predictions obtained with FONLL calculations [13–15] and PYTHIA8 [50,58] for the description of the decay kinematics and branching ratios. They are obtained using fragmentation fractions from $e^+e^-$ collisions [61] for the $B$ mesons and the $f(b \to \Lambda^+_c)/f(b \to B)$ fragmentation fraction ratio measured by the LHCb Collaboration [39]. The contributions of nonprompt $\Lambda^+_c$ baryons originating from $B$ mesons and $\Lambda^+_0$ baryons are reported separately to show that the largest contribution is represented by the beauty baryons, while the $B$ mesons contribute only marginally to the nonprompt $\Lambda^+_c$ production cross section. Hence, it is possible to inquire the hadronization of beauty quarks into $\Lambda^+_0$ baryons through the nonprompt $\Lambda^+_c$. In the right panel of the same figure the data are compared with the $p_T$-differential ratio between prompt $\Lambda^+_c$ and $D^0$ hadrons. The two measurements are compatible in their common $p_T$ range, with a tension of less than two standard deviations in $2 < p_T < 4$ GeV/$c$, where the ratio of nonprompt hadrons

![Figure 4](image1.png)

**FIG. 4.** Beauty production cross section per rapidity unit at midrapidity obtained from from dielectron [66] and nonprompt $J/\psi$ [3], $D^0$, and $\Lambda^+_c$ hadrons measured in pp collisions at $\sqrt{s} = 13$ TeV compared to FONLL [13–15] and NNLO [22] predictions. The average $d\sigma_{b\bar{b}}/dy$ of the estimates from the $D^0$ and $\Lambda^+_c$ hadrons is also reported.

![Figure 5](image2.png)

**FIG. 5.** Left: $p_T$-differential ratios of nonprompt $\Lambda^+_c$- and $D^0$-hadron cross sections compared with predictions obtained with FONLL calculations [13–15] and PYTHIA8 [50,58] for the $b \to h_c + X$ decay kinematics. The contributions from beauty mesons and from the $\Lambda^+_0$ baryon are depicted separately. Right: $p_T$-differential ratios of prompt [27] and nonprompt $\Lambda^+_c$- and $D^0$-hadron cross sections compared with predictions obtained with the TAMU model [36,49] and PYTHIA8 for the $b \to h_c + X$ decay kinematics.
is higher than the one of promptly produced hadrons. The experimental data are also compared to the predictions obtained with the TAMU model combined with PYTHIA8 to describe the $h_b \rightarrow h_c + X$ decay kinematics, in the case of nonprompt production. The prediction for prompt charm hadrons has an error band representing the uncertainty on the BR of excited charm baryons decaying into $\Lambda^+_c$, not included in the one for nonprompt hadrons. The measured nonprompt $\Lambda^+_c/D^0$ ratio is rather well described for $p_T > 4$ GeV/$c$ given the current uncertainties, while it is underestimated for $2 < p_T < 4$ GeV/$c$. The prompt charm and beauty ratios are described by the TAMU calculations within the uncertainties for the whole measured $p_T$ interval.

Figure 6 shows the $p_T$-differential nonprompt $\Lambda^+_c/D^0$ yield ratio at midrapidity ($|y| < 0.5$) in pp collisions at $\sqrt{s} = 13$ TeV compared with the measurements of prompt $\Lambda^+_c/D^0$ [27], $\Lambda/\Lambda^0$ [67], and $p/\pi^+$ [67] ratios at the same energy and rapidity interval, and with the $\Lambda^0_\psi/(B^0 + B^+)$ yield ratio measured by LHCb at forward rapidity ($2.5 < y < 4$). The $\Lambda^0_\psi/(B^0 + B^+)$ ratio is a bit lower than the one between nonprompt $\Lambda^+_c$ and $D^0$ mesons, however it has to be considered that the normalization is slightly different. In the LHCb result the production cross sections of $B^0$ and $B^+$ mesons, i.e., the total yield of nonstrange $B$ mesons is used, while the nonprompt $D^0$, used in this ratio, accounts for about 70% of the nonstrange $D$ mesons. Also the fraction of $B^0$ and $B^+$ mesons decaying to $\Lambda^+_c$ and $D^+_c$, as well as the $\Lambda^0_b$ and $B^0$ hadrons decaying to $D^0$ mesons influence the ratio. In addition, in the nonprompt $\Lambda^+_c/D^0$ ratio, the $h_b \rightarrow h_c + X$ decay kinematics is expected to slightly modify the $p_T$ dependence compared to the one of the ratio between beauty hadrons. Interestingly, all the measurements for beauty, charm, and strange hadrons show a similar trend as a function of $p_T$ and are compatible within the uncertainties. The $p/\pi^+$ production ratio also features a similar $p_T$ dependence, however it is lower in absolute terms. The experimental values are compared with the corresponding predictions obtained with PYTHIA8 simulations, using different tunes and the same rapidity ranges.

FIG. 6. Non-prompt $\Lambda^+_c/D^0$, prompt $\Lambda^+_c/D^0$ [27], $\Lambda/\Lambda^0$ [67], and $p/\pi^+$ [67] ratios measured in pp collisions at $\sqrt{s} = 13$ TeV at midrapidity ($|y| < 0.5$) compared with the $\Lambda^0_\psi/(B^0 + B^+)$ ratio measured by the LHCb Collaboration at forward rapidity ($2.5 < y < 4$) [39] and with predictions obtained with the PYTHIA8 MC generator with the Monash 2013 tune [50,58] and the CLR-BLC modes 0, 2, and 3 [37] in the corresponding rapidity range with respect to data.
of the experimental results. In the top-left panel, the results obtained with the Monash 2013 tune [58], which implements a fragmentation process tuned to reproduce the measurements in e⁺e⁻ collisions, is reported. Here, all the baryon-to-meson ratios are underestimated by PYTHIA8 except for the p/π⁺ ratio for which the model prediction is rather good at low p_T. A better agreement is instead obtained with the CLR-BLC tunes (i.e., Mode 0, 2, and 3), shown in the other three panels of Fig. 6. These three tunes are characterized by different constraints on the time dilation and causality, as defined in Ref. [37]. The time parameters are relevant in this model, because two strings can reconnect if they are able to resolve each other during the time between their formation and hadronization, taking also into account time-dilation effects caused by relative boosts. The Mode 0 and 2 settings, reported in the top-right and bottom-left panels of Fig. 6 respectively, predict a similar baryon-to-meson ratio for the strange, charm, and beauty flavors for p_T > 2 GeV/c and a significantly higher ratio for heavy-flavor hadrons than strange hadrons for lower p_T (e.g., a factor three is predicted at p_T ≈ 400 MeV/c). Despite the agreement with the data is significantly improved compared to the Monash tune, the measurements of beauty hadrons are overestimated for p_T ≤ 10 GeV/c. Instead, the Mode 3 (bottom-right panel of Fig. 6) underestimates the ratio for charm hadrons for p_T ≤ 12 GeV/c and overestimates that of beauty hadrons in the same p_T interval, quantitatively more than the other two CLR-BLC modes. The features, observed in all comparisons with PYTHIA8 tunes, indicate that more precise measurements of the baryon-to-meson ratios, especially those including beauty-hadron measurements at very low p_T (p_T < 2 GeV/c) are crucial for tuning the model parameters involving the reconnection of quarks via junction topologies and to possibly validate this as the mechanism responsible of the baryon enhancement observed in hadron collisions compared to e⁺e⁻ collisions. It is worth pointing out that other theoretical models are proposed to describe the enhancement, based on different hadronization mechanisms (e.g., recombination).

The p_T-integrated nonprompt Λ⁺/D⁰ ratio was computed by dividing the p_T-integrated cross sections reported in Table I. All the systematic uncertainties, except for those related to the tracking efficiency, were propagated as uncorrelated in the ratio. The resulting value is compatible with the one measured for promptly produced particles and significantly higher than that measured in e⁺e⁻ collisions at LEP [68]. All the values are reported in Table II.

VI. CONCLUSIONS

In summary, the p_T-differential and p_T-integrated production cross sections of nonprompt Λ⁺ and D⁰ hadrons were measured for the first time at midrapidity in pp collisions at √s = 13 TeV. The results are compatible with the theoretical models based on FONLL calculations with the f(b → Λ_c) and f(b → B) fragmentation fractions measured by LHCb and at e⁺e⁻, respectively, suggesting a similar beauty-baryon enhancement at forward and midrapidity in pp collisions. Furthermore, the results are in agreement with the TAMU statistical hadronization model for the relative abundances of different beauty hadron species. The extrapolated bb production cross section at midrapidity per unit of rapidity is found to be compatible with pQCD calculations with FONLL and NNLO accuracy. The measured baryon-to-meson ratios of light flavor, strange, charm, and beauty hadrons show a similar p_T trend. In addition, all ratios, except the p/π⁺, are significantly higher than the values measured in e⁺e⁻ collisions. The p_T-differential baryon-to-meson ratios have been compared to predictions of the TAMU statistical hadronization model and to the PYTHIA8 simulations, that include the color-reconnection mechanism in the string fragmentation and indicate that all the flavors have to be considered simultaneously in order to obtain the best tuning of the model parameters involving the reconnection of quarks via junction topologies. This feature asks for more precise results, including a direct measurement of beauty hadrons especially in the same p_T and rapidity range and the p_T < 4 GeV/c region, which can be reached with the data collected in the LHC Run 3 data taking period.

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<table>
<thead>
<tr>
<th>ALICE</th>
<th>LEP average [68]</th>
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<tr>
<td>Prompt Λ⁺/D⁰</td>
<td>0.49 ± 0.02(stat)±0.05(sys) [60]</td>
</tr>
<tr>
<td>Nonprompt Λ⁺/D⁰</td>
<td>0.47 ± 0.06(stat)±0.04(sys) [60]</td>
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