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Theory of the magnetoelectric effect in a lightly doped high-$T_c$ cuprate

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In a recent study, Viskadourakis et al. (arXiv:1111.0050) discovered that extremely underdoped La$_2$CuO$_{4+z}$ is a relaxor ferroelectric and a magnetoelectric material at low temperatures. It is further observed that the magnetoelectric response is anisotropic for different directions of electric polarization and applied magnetic field. By constructing an appropriate Landau theory, we show that a biquadratic magnetoelectric coupling can explain the experimentally observed polarization dependence on magnetic field. This coupling leads to several interesting low-temperature effects, including a feedback enhancement of the magnetization within the ferroelectric phase, and a predicted magnetocapacitive effect.

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The field of magnetoelectrics has witnessed intense theoretical and experimental progress in recent years, mainly driven by the discovery of the nonlinear magnetoelectric effect, i.e., the dominant magnetoelectric coupling is of higher order than a bilinear coupling between electric and magnetic fields. Among the materials discovered with such physical properties are the so-called birelaxors. These systems show both relaxor ferroelectric and relaxor magnetic properties and are associated with spin-charging coupling at a mesoscopic scale.

Focusing on the parent high-$T_c$ superconductor La$_2$CuO$_{4+z}$ (LCO) with an exceptionally low carrier concentration $n=10^{17}$ cm$^{-3}$, we have recently found that this material is in fact a ferroelectric at low temperatures. More specifically, LCO has been shown to be a relaxor ferroelectric where the dielectric mode behavior is caused by freezing of randomly oriented polarized regions. In addition, LCO exhibits a distinct magnetoelectric effect with a pronounced dependence of the polarization curves reported in Ref. 5.

Below approximately 530 K the crystal structure of LCO is LTO with space group $Cmca$ ($D_{2h}^8$). If $(\hat{x}, \hat{y}, \hat{z})$ denote unit vectors along the crystal axes, then we define fractional translations by

$$\tau = \frac{1}{2}(a\hat{x} + c\hat{z})\tau' = \frac{1}{2}(a\hat{x} + b\hat{y}),$$

where $a, b, c$ are the lattice constants. The symmetry elements of this crystal structure are then written as $G = G_0 + \tau G_0$, where $G_0$ contains the eight elements

$$E, I, \sigma_a, \sigma'_a, \sigma_c, C_{2a}, C_{2b}, C_{2c}.$$ (2)

Here $E$ denotes the identity, $I$ inversion about a Cu site, $\sigma_a, \sigma'_a, \sigma_c$ reflections about the planes $x = a/2, y = b/2, z = c/2$, and $C_{2a}, C_{2b}, C_{2c}$ are 180° rotations about the axes that emanate from the center of the unit cell. Primed elements must be complemented by translation $\tau'$ that is itself not a symmetry operation.

Taking into account the above-mentioned symmetry properties of the $Cmca$ space group, the free energy can be expressed as a sum of three contributions

$$F = F_M + F_{MP} + F_P.$$ (3)

Here, $F_M$ is the purely magnetic free energy, $F_{MP}$ is the magnetoelectric contribution, and $F_P$ is the polarization free energy. The magnetic free energy that accounts for the crystal structure of the LTO phase has been studied previously by,
e.g., Thio et al.,16 and is given by

$$F_M = \frac{1}{2} \sum_{i=1}^{3} \left[ \frac{\gamma_{a}}{2} L_{i}^{2} + \frac{1}{4} AL_{i}^{4} + \frac{1}{6} BL_{i}^{6} - CL_{i} M_{i} \right] + \frac{\gamma_{a}}{2} M_{i}^{2} - H_{i} M_{i} - M_{ab} L_{i} \right] + \frac{1}{2} J_{z} L_{i} L_{2}. \quad (4)$$

Here, the out-of-plane (c direction) [in-plane (a-b plane)] applied magnetic field is represented by $H_{c} [H_{ab}]$. The coefficients $A$, $B$, and $C$ would in general be temperature dependent. The order parameter $M_{i} = (S_{x i} + S_{y i})/2$ is the ferromagnetic moment per spin with $S_{x i}, S_{y i}$ being the sublattice spins in the ith plane, and $L_{i} = (S_{x i} - S_{y i})/2$ is the antiferromagnetic order parameter ($L_{i}||a$). The spins are slightly canted due to the DM interaction term $-CM_{i} L_{i}$, which causes them to lie in the $a$-$c$ plane of the magnetic unit cell. The coupling between the different planes is included by the $J_{z}$ term.

The presence of an inversion symmetry in the space group of the crystal forbids any linear magnetoelastic effect17 and the physics is dominated by nonlinear coupling terms. We can focus on the largest nonlinear terms by further noting that the physics is dominated by nonlinear coupling terms. We can focus on the largest nonlinear terms by further noting that the free energy should also contain gradient terms since we are dealing with a relaxor system20 as well as higher-order terms. However, since we are interested in the magnetoelectric effect close to the ferroelectric transition, it is reasonable to restrict our analysis to the above terms.

The solutions that determine $\mathbf{P}(H)$ are obtained by minimizing $F$ with respect to the electric polarization and magnetic order parameters. In the case of LCO studied experimentally, the Néel temperature is $T_{N} \sim 320$ K, which is much higher than the temperature at which the ferroelectric order sets in ($T_{p} \sim 4.5$ K). Therefore, we evaluate $F_{M}$ for the high-temperature phase with $\mathbf{P} = 0$, providing the following set of equations:

$$M_{i} = \chi_{0}(H_{c} + CL_{i}), \quad (8)$$

$$\chi_{2D}^{-1} L_{1} + AL_{1}^{3} + BL_{1}^{5} + \frac{1}{2} J_{z} L_{2} = CM_{i} + H_{ab}, \quad (9)$$

$$\chi_{2D}^{-1} L_{2} + AL_{2}^{3} + BL_{2}^{5} + \frac{1}{2} J_{z} L_{1} = CM_{i} + H_{ab}, \quad (10)$$

$$\left[ \chi_{ea}^{-1} + \sum_{i=1}^{2} \left( \gamma_{aa} L_{i}^{2} + \gamma_{aa} M_{i}^{2} + \gamma_{ba} M_{i} L_{i} \right) \right] P_{a} = -\beta P_{a}. \quad (11)$$

The magnetization curves at low temperatures ($\lesssim 30$ K) have a glassy contribution that can be observed in Fig. 1(a) as a hump feature at low magnetic fields and a broadened spin-flop transition for out-of-plane magnetic fields $H_{c}$.24 Such glassy behavior is absent in the magnetization response for in-plane applied magnetic fields $H_{ab}$, as seen from Fig. 1(b). These features cannot be obtained from the above equations, and hence to include them to the lowest order we simply take the experimental magnetization curves in Fig. 1 as input. This approximation, along with the temperature range at which we evaluate the magnetoelectric effect, leads to deviations from the parameters of the magnetic free energy from those used, e.g., by Thio et al.16,23

In terms of the following rescaled quantities $l_{+} = \chi_{0} C(L_{1} + L_{2})/2$, $l_{-} = \chi_{0} C(L_{1} - L_{2})/2$, $M = (M_{1} + M_{2})/2$, $\gamma_{1a} = 2\gamma_{1a}(\chi_{0} C)^{-1}$, $\gamma_{2a} = 2\gamma_{2a}$, $\gamma_{ba} = 2\gamma_{ba}(\chi_{0} C)^{-1}$, the polarization dependence on the applied magnetic field can be expressed as

$$P_{a}(H_{ab})/P_{a}(0) = \left\{ 1 + \frac{s_{a}}{L_{a}^{2}} \left[ l_{+}^{2}(H_{ab}) - l_{-}^{2}(0) + g_{a} M(H_{c}) \right] \right\}^{1/2}, \quad (12)$$

$$P_{a}(H_{c})/P_{a}(0) = \left\{ 1 + \frac{s_{a}}{L_{a}^{2}} \left[ l_{+}^{2}(H_{c}) - l_{-}^{2}(0) + g_{a} M(H_{c}) \right] + (1 - g_{a}) l_{+}^{2}(H_{c}) + q_{a} M(H_{c}) l_{+}(H_{c}) \right\}^{1/2}, \quad (13)$$

where $s_{a} = \lambda_{a} l_{+}^{2}(0)/[\chi_{ea}^{-1} + \lambda_{a} l_{+}^{2}(0)]$, $g_{a} = \gamma_{ba}/\lambda_{a}$, and $q_{a} = \gamma_{ba}/\lambda_{a}$, with $\lambda_{a} = \gamma_{1a} + \gamma_{2a} + \gamma_{ba}$. In general, all three

![FIG. 1. (Color online) Experimental values of (a) out-of-plane magnetization and (b) in-plane magnetization at $T = 5$ K.](140405-2)
parameters $s_a$, $g_a$, and $q_a$ will be temperature dependent. The temperature dependence of $s_a$ primarily results from its relation to the electric susceptibility; hence an estimation of the amplitude of $s_a$ can reveal the magnitude of anisotropy in the electric polarization.

In the case of an out-of-plane magnetic field $H_c$, the measured $P_c(H_c)$ increases with field and exhibits a pronounced hump at the spin-flip transition at $H_{sf}$, as seen from Fig. 2(a). By contrast, $P_{ab}(H_c)$ decreases with increasing $H_c$ but also exhibits a hump feature at $H_{sf}$, as seen from Fig. 2(c). This behavior indicates a scenario where the coupling between the magnetic order and out-of-plane polarization $P_c$ is attractive whereas the coupling with $P_{ab}$ is repulsive. However, we find that the theoretical picture is more complex due to the presence of two competing magnetic orders $L$ and $M$ coupling to the electric polarization. For the out-of-plane magnetic field, we calculate the $P_c(H_c)$ response using the magnetization data shown in Fig. 1(a). As seen from Figs. 2(b) and 2(d), we obtain qualitative agreement with both experimental polarization curves including the hump feature at $H_{sf}$. Note that for the coupling to the magnetization we have set $g_a = g_b = g_c = -0.2$. Therefore, the source of anisotropy between $P_c(H_c)$ and $P_{ab}(H_c)$ is the DM-induced coupling term $q_a P_{ab} M_i L_i$ with $q_a = q_b = 0$ and $q_c = -6.58$.

In the case of an in-plane magnetic field $H_{ab}$, $P_c(H_{ab})$ depends on only a single fitting parameter $s_a$ that controls the magnitude of the polarization ratio, whereas the shapes of the theoretical curves are governed by the magnetic order parameter of the system. Further, we can deduce from Eq. (12) that the polarization primarily couples to the 2D antiferromagnetic order through a magnetoelectric interaction term $P_{ab} \sim \lambda_a P_{ab}^2 L_i^2$. The anisotropy in polarization through the parameter $\lambda_a$ for in-plane magnetic fields is primarily controlled by the DM-induced magnetoelectric coupling term $q_a P_{ab}^2 M_i L_i$, since $q_a$ undergoes the largest variation between in-plane and out-of-plane directions. The DM physics therefore plays an important role in generating an anisotropy between $P_c(H)$ and $P_{ab}(H)$ in La$_2$CuO$_{4+x}$.

Using the magnetization curve from Fig. 1(b), the solutions of $P_c(H_{ab})$ are presented in Figs. 3(b) and 3(d). Though the theoretical curves have similar shapes, the scales are different in the two figures due to the difference in $s_a$ values. Note that all theoretical curves have been plotted using magnetization data available at $T = 5$ K while the experimental curves correspond to $T = 2.5$ K, which accounts for the smaller scale of the theoretical curves. As seen from the plots, we find again qualitative agreement with the experimental data shown in Figs. 3(a) and 3(c), though the experimental plot in Fig. 3(a) has a steeper slope than theory. This steeper curve in the experimental curve could be the result of some history effect in these relaxor systems, a feature that has not been taken into account in our analysis. As in Fig. 2, the plots correspond to $s_a = 0.1$, $s_a = 0.074$, which leads to a small anisotropy in the electric susceptibilities $\chi_{\alpha\alpha}^{-1}$ and therefore between the zero magnetic field values of in-plane polarization $P_{ab}$ and the out-of-plane component $P_c$. This small anisotropy has been observed in experiments and implies a much weaker anisotropy of the electric polarization compared to the magnetic order. This result lends support to a scenario where the nonstoichiometric oxygen dopants (charge carrier doping) play an important role in generating the relaxor ferroelectricity in La$_2$CuO$_{4+x}$.

We have observed experimentally that the magnetization shows a small enhancement below the temperatures where the ferroelectric order sets in. This effect is in addition to the typical upturn in magnetization near the spin-glass freezing temperature. We can study such a feedback effect of a finite polarization on the magnetization by minimizing $F$.
A weak magnetocapacitive effect is therefore predicted in experiments at low temperatures. Note that in the above expression we would expect a small suppression in the permittivity for magnetic fields in the $a$-$b$ plane.

The observation of relaxor ferroelectricity in underdoped LCO has been argued to originate from the formation of polar nanoregions (PNRs) around the nonstoichiometric oxygen dopants. The formation of PNRs and the mechanism by which they condense into a ferroelectric phase is a well studied topic. Though the relaxor physics in LCO naturally relates to the presence of dopants, the extremely low concentration of excess oxygen in the samples used in Ref. 5 may imply the presence of additional mechanisms for the PNRs to couple and undergo a spontaneous transition to long-range ferroelectric order. One may speculate that such mechanisms include subtle noncentrosymmetric structural distortions in the host lattice and/or a tendency for the dopants to cluster and thereby reduce the inter-PNR distance. As shown in Fig. 4, in magnetic materials such as LCO the PNRs may also cause a distorted spin structure that could lead to a magnetoelectric effect through, e.g., geometric frustrations in the presence of a DM interaction and/or indirectly through coupling to strains. This physics has similarities to the observation of magnetoelectric behavior in a number of other relaxor ferroelectrics.

In summary, we have shown that the magnetoelectric effect in extremely underdoped La$_2$CuO$_{4+x}$ can be explained by biquadratic terms in the free energy. It is proposed that the microscopic origin of the ferroelectricity is caused by polar nanoregions generated by dopant ions. The discovery of ferroelectricity and a magnetoelectric effect in the cuprate materials due to charge carrier doping has sparked many questions for future studies. In particular, what happens at higher doping levels and what is the fate of the PNRs in the regime where the pseudogap and superconducting phases emerge?

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25The coefficients in $F_M$ are $\chi_0 = 5.625 \times 10^{-4} \text{ cm}^3/\text{mol}$, $C\chi_0 = 1.88 \times 10^{-3}$, $\chi_0^2 - C^2\chi_0 - J_c = -4.4 \mu \text{eV}$, $a = 2.4 \times 10^{-3}/(C\chi_0)^2 \text{ eV}/(\text{emu})^2$, $b = 10^{-3}/(C\chi_0)^4 \text{ eV}/(\text{emu})^2$.