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Uncovering a hidden black hole binary from secular eccentricity variations of a tertiary star

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We study the dynamics of a solar-type star orbiting around a black hole binary (BHB) in a nearly coplanar system. We present a novel effect that can prompt a growth and significant oscillations of the eccentricity of the stellar orbit when the system encounters an “apsidal precession resonance,” where the apsidal precession rate of the outer stellar orbit matches that of the inner BHB. The eccentricity excitation requires the inner binary to have a nonzero eccentricity and unequal masses, and can be created even in noncoplanar triples. We show that the secular variability of the stellar orbit’s apocenter, induced by the changing eccentricity, could be potentially detectable by Gaia. Detection is favorable for BHBs emitting gravitational waves in the frequency band of the Laser Interferometer Space Antenna, hence providing a distinctive, multimessenger probe of the existence of stellar-mass BHBs in the Milky Way.

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I. INTRODUCTION

About 90 double compact object merger events have been detected by the LIGO-Virgo-KAGRA Collaboration in their first three observing runs [1]. The avenues to produce stellar-mass black-hole binary (BHB) mergers include different formation channels and environments, including isolated binary evolution [2–10], chemically homogeneous evolution [11–14], and multiple-body evolution in the gas disks of active galactic nuclei [15–30]. Additionally, there are various flavors of dynamical channels that involve either strong gravitational scatterings in dense clusters [31–41], tertiary-induced mergers via von Zeipel–Lidov–Kozai (ZLK) oscillations [42–59], or flyby-induced mergers [60,61]. However, the relative contribution of each channel and the astrophysical origin of the detected mergers are still unclear.

BHB progenitors are expected to be numerous but remain undetected as an abundant population in our Universe. Searching for these inspiraling BHBs is of great importance to understand the origin of gravitational-wave (GW) sources. If the BHBs are not accreting, these quiescent sources can be detected via GWs. Since BHBs in the inspiral phase are still far from merger, the associated GWs are in the low-frequency band that can be explored by future spaceborne GW observatories, such as LISA [62], TianQin [63], Taiji [64], B-DECIGO [65], Decihertz Observatories [66], and TianGO [67]. Also, since a significant fraction of compact BHBs may be members of hierarchical systems [68–70], the motion of a nearby visible object (such as a star or a pulsar) can be used to search for BHBs. In this scenario, the inner BHB can perturb the outer orbit, either inducing short-term orbital oscillations (tertiary orbit becomes quasi-Keplerian), or causing long-term oscillations of the eccentricity and the orientation of the angular momentum when the tertiary orbit is highly inclined [71–73]. If the tertiary object is bright enough, radial velocity measurements could be used to determine the short- and long-term deviations from a Keplerian orbit [74–76].

Currently, observations show that most triple-star systems are less inclined or nearly coplanar [77–79]. Here, we consider a solar-type star orbiting around a BHB and study the secular evolution of the stellar orbit when the triple system is coplanar. We show that the outer binary may experience an eccentricity growth driven by the “apsidal precession resonance” [80,81]. Compared to the complex evolution of the orientation of the angular momentum (i.e., precession or nutation), the secular change of the eccentricity of the outer stellar orbit could provide distinctive evidence to reveal the presence of a BHB.

II. APSIDAL PRECESSION RESONANCE

We consider an inner BHB with masses $m_1$, $m_2$ and a solar-type star ($m_* = 1 \, M_\odot$) that moves around the center of mass of the inner bodies. The reduced mass for the inner binary is $\mu_{10} \equiv m_1 m_2 / m_{12}$, with $m_{12} \equiv m_1 + m_2$. Similarly, the outer binary has $\mu_* \equiv (m_1 m_2)/(m_{12} + m_*)$. The semimajor axes
and eccentricities are denoted by $a_{\infty}$, $a_*$, and $e_{\infty}$, $e_*$, respectively. The orbital angular momenta of two orbits are thus given by $L_{\infty} = \mu_{\infty} \sqrt{G m_{12} a_{\infty} (1 - e_{\infty}^2)}$ and $L_* = \mu_* \sqrt{G (m_{12} + m_*) a_* (1 - e_*^2)}$.

When the triple system is nearly coplanar, the ZLK oscillations are not allowed to occur, but a significant eccentricity excitation of the inner binary may still be induced [82,83]. A secular, “apsidal precession resonance” plays a dominant role if the total apsidal precession of the inner binary matches the precession rate of the outer binary [80,81]. The precession of both the inner and outer binaries is driven by Newtonian and general-relativistic (GR) effects. Such resonance allows efficient angular momentum exchange between the inner and outer binaries.

Here, we extend our previous studies to an “inverse” secular problem, and address the question of how the apsidal precession resonance modifies the eccentricity evolution of the tertiary for the first time. Since we are interested in the long-term orbital evolution, we adopt the single-averaged (SA; only averaging over the inner orbital period) secular equations of motion, taking into account the contributions from the Newtonian effect up to the octupole level of approximation and the leading-order GR effect in both the inner and outer orbits. The explicit SA equations were provided in Refs. [52,84].

In Fig. 1, the left panels show the evolution of the eccentricities of both the inner and outer orbits. Starting with the eccentric inner binary, we see that $e_*$ can be excited from the circular orbit and undergoes oscillations. In the middle panel, we find that a large fraction of systems can develop eccentricities (0.04 $\lesssim a_{\infty}/\text{AU} \lesssim 0.08$), and an evident peak, $\Delta e_*^{\text{max}} \approx 0.8$, can be resolved when the evolution is sufficiently long ($\gtrsim 10$ y). The right panel illustrates the level of $e_*$ excitation in the $m_2/m_1-a_{\infty}$ plane. The eccentricity of the stellar orbits can be excited for $a_{\infty} \gtrsim 0.04$ AU, and the systems with smaller mass ratios tend to have larger $\Delta e_*^{\text{max}}$ values. This is because the evolution of $e_*$ is determined by the octupole-order secular interactions, which can be quantified by terms proportional to [45]

$$e_{\text{oct}} \equiv \frac{m_1 - m_2 a_{\infty} e_*}{m_2 (1 - e_*^2)}.$$

We see that the eccentricities of some outer orbits reach significantly large $\Delta e_*^{\text{max}}$ values close to unity, leading to unbound orbits.

For coplanar ($\tilde{L} = \tilde{L}_*$), nondissipative (no gravitational radiation) systems, the secular dynamics can be understood analytically. When $e_{\infty}, e_* \ll 1$, the evolution of $e_{\infty}$ and $e_*$ is governed by the linear Laplace-Lagrange equations [86,87]. If we define the complex eccentricity variables as $\tilde{e}_{\infty} \equiv e_{\infty} \exp(i \sigma_{\infty})$ and $\tilde{e}_* \equiv e_* \exp(i \sigma_*)$, where $\sigma_{\infty}, \sigma_*$ are the longitude of the pericenter of the inner and outer orbits, then the evolution equations are reduced to

$$\frac{d}{dt} (\tilde{e}_{\infty} \tilde{e}_*) = i \left( \nu_{\infty} \nu_* \right) \left( \tilde{e}_{\infty} \tilde{e}_* \right),$$

with

![FIG. 1. Apsidal precession resonance in coplanar triple systems where the outer orbital period ($P_*$) is set to 15 days. All results are obtained by integrating the SA secular equations including GR effects (but without GW emission). Left: evolution examples of the orbital eccentricities in the inner (black) and outer (red) binaries, with $m_{12} = 50$ M$_\odot$ and initial $e_{\infty}^0 = 0.9$ and $e_*^0 = 0$. Middle: ratio of apsidal precession rates [Eqs. (3) and (4), including the dependence of finite eccentricities, i.e., $\Delta e_*/\omega_*$] and the maximum change in eccentricity $\Delta e_*^{\text{max}}$ of the outer stellar orbit as a function of the semimajor axis $a_{\infty}$. The cross-hatched region corresponds to dynamically unstable triple systems [85]. The parameters are the same as in the left panels, except that $a_{\infty}$ is relaxed to a range of values. The labeled GW frequency is the peak frequency at pericenter [47]. The numerical results are obtained by integrating the SA secular equations over several time scales (as labeled), and the analytical result is given by the energy and angular momentum conservation laws (dashed blue line). Right: $\Delta e_*^{\text{max}}$ induced by the apsidal precession resonance in the $m_2/m_1-a_{\infty}$ plane. We use the same parameters as in the middle panel, taking into account the full range of mass ratios of the BHB. The three black contours (solid, dashed, and dot-dashed) specify $\Delta e_*^{\text{max}} = 0.1$, 0.2, and 0.5, respectively. The gray crosses indicate the significant change of $e_*$ that leads to instability.](image-url)
then we have

\[ \Delta \epsilon_{\text{max}} = \left| \frac{\nu_{\infty} - \nu_{\ast}}{a_{\infty}} \right| \frac{\Delta e_{\ast}}{e_{\ast}} \]

where \( n_{\infty,\ast} = (Gm_{12}/a_{\infty,\ast}^3)^{1/2} \) and \( \omega_{\text{GR,\infty,\ast}} = 3G^{3/2}m_{12}^{3/2}/[e_1^2a_{\infty,\ast}^2(1-e_1^2)] \) are the mean motion and the GR-induced pericenter-precession frequency of the inner (outer) binary for \( m_{12} \gg m_{\ast} \), respectively.

Starting with \( e_{\infty} = e_{0\sin}^0, e_{\ast} = 0 \) at \( t = 0 \), Eq. (2) can be solved to determine the time evolution of \( e_{\ast}(t) \) (see Ref. [80]), which oscillates between 0 and \( e_{\ast,\text{max}} \), where

\[ e_{\ast,\text{max}} = \frac{e_{0\sin}^0}{\sqrt{(\omega_{\infty,\ast})^2 + 4\nu_{\ast,\text{in}}\nu_{\infty,\ast}}} \]

Clearly, \( e_{\ast,\text{max}} \) attains its peak value when \( \omega_{\infty,\ast} = \omega_{\ast} \), and then we have

\[ e_{\ast,\text{peak}} = e_{0\sin}^0 \left( \frac{a_{\infty,\ast}^{1/2}}{a_{\ast}^{1/4}} \right)^{1/4} \]

Note that the linear theory is valid for the low-\( e \) systems. For the example in Fig. 1, a nonzero \( e_{0\sin}^0 \) may lead to an unphysically large \( e_{\ast,\text{peak}} \); however, Eqs. (7) and (8) are useful in the sense that we can expect (i) an \( e_{\ast} \) excitation to appear when \( \omega_{\infty,\ast} \approx \omega_{\ast} \) (see the middle panel of Fig. 1; the resonance occurs for finite \( e_{\ast} \)) and (ii) the \( e_{\ast} \) excitation becomes stronger with increasing \( e_{0\sin}^0 \) (see also Fig. 2).

For finite eccentricities, Eq. (2) breaks down. However, in the case of exact coplanarity, the maximum eccentricity of a triple can still be calculated algebraically, using the conservation of energy and angular momentum [88]. This method works well for two orbits with arbitrary eccentricities, but it cannot show the time evolution and resonance features. A full derivation can be found in Ref. [81] and the solution is presented in Fig. 1.

Figure 2 shows the \( e_{\ast} \) excitation with arbitrary initial eccentricities for coplanar triples. We again consider the fiducial example in which the inner BHB has a total mass \( m_{12} = 50 M_\odot \) with a mass ratio \( m_2/m_1 = 0.2 \). We choose three values of the semimajor axis of the outer orbit (\( a_{\ast} \)) and consider a range of \( a_{\infty} \) that satisfies the stability criterion. To illustrate the role of the eccentricity, we start with the same initial configurations, namely, the argument of periapsis, the longitude of ascending nodes, and the true anomaly of the outer orbit are set to be the same at \( t = 0 \).

Each system is evolved over a long time scale (to achieve the highest value of \( e_{\ast} \)) and a short time scale (10 y). The maximum change of \( e_{\ast} \) is picked only for the system that remains stable.

In the upper left panel of Fig. 2, we see that all initial circular outer orbits can become eccentric when the resonance occurs, and the maximum change \( \Delta e_{\ast,\text{max}} \) grows as \( e_{0\sin}^0 \) increases. In the lower left panel, the \( e_{\ast} \) excitation can still occur for the initially eccentric outer orbits. However, due to the stability, only a fraction of systems (with a narrow range of \( a_{\infty} \), when \( e_{0\sin}^0 \approx 0.6 \)) may undergo
significant eccentricity oscillations. Note that for the wider stellar orbits ($P_\star = 50, 100$ days), as shown in the middle and right panels, the system has to be evolved for a sufficiently long time. This is because the time scale of the $e_\star$ excitation is of the order of [89]

$$T_{e_\star}|_{e_\star, e_\infty \ll 1} \simeq \frac{m_{12}}{m_{\infty}} \frac{e_\star}{e_\infty} \left(\frac{a_\star}{a_\infty}\right)^3 \frac{L_\star}{L_\infty}.$$  

When the inner and outer orbits are mutually inclined, no simple analytical result can be derived, and the long-term evolution of the outer orbits can only be studied numerically. Previous studies [71–73] showed that in inclined triple systems, the eccentricity of the outer orbit can oscillate moderately and the angular momentum ($L_\star$) undergoes nodal precession/nutation around the inner one ($L_\infty$). Moreover, $L_\star$ might experience a flip if the tertiary is a test particle.

Figure 3 presents the results of the triples with a series of initial inclinations. We see that in the upper panels, regardless of the values of the initial inclinations, $e_\star$ excitation due to resonance always occurs, and the resonance location shifts when $P_\infty$ changes ($P_\star$ is the initial inclination angle between $L_\infty$ and $L_\star$). In the lower panels, we find that the inclination varies for a wider range of $a_\infty$ compared to the change of $e_\star$. In particular, $\Delta I_\star$ always undergoes an additional excitation when $\Delta e_\star^{\text{max}}$ approaches the peak value for the inclined systems.

### III. RESONANCE IN STELLAR ORBITS AND DETECTABILITY

We now focus on the dependence of the change in eccentricity on the parameters of the outer stellar orbit, considering that the inner BHB is a LISA source. To explore the observability of this effect, we consider the detectability of a maximum eccentricity change, $\Delta e_\star^{\text{peak}}$, within a certain time scale.

We initialize systems with $e_\infty = 0.9$ and $e_\infty = 0$ in a coplanar configuration. For the inner BHB, we choose three values for the total mass ($m_{12}/M_\odot = 20, 50, 100$) and allow the mass-ratio range to take on all values such that both masses are consistent with being a BH, $m_1, m_2 \gtrsim 5M_\odot$. Since we are interested in the GW sources, we focus on BHBs that radiate GWs in the LISA frequency band. Thus, the semimajor axis $a_\infty$ is chosen from a uniform distribution that satisfies $f_{\text{GW}} \gtrsim 10^{-4}$ Hz and with a merger time (due to GW emission) larger than $10^3$ y [90]. Then, for the (outer) stellar orbits, we sample the semimajor axis $a_\star$ in the range $P_\star = 1–180$ days, considering only systems that are dynamically stable. Each system evolves for 10, 30, or 100 y, using the SA equations of motion. The maximum change of $e_\star$ is recorded if the star remains gravitationally bound and stable during the evolution. Finally, since the orbital evolution relies on the initial geometry of the triples, to cover all possibilities we randomly sample the longitude of the pericenter of the inner orbit and the true anomaly of the outer orbit. Each triple system is evolved with 100 different initial geometries.

For a given set of parameters, the criterion of apsidal precession resonance ($\omega_\infty = \omega_\star$) provides a good estimate for the resonance radius: resonance occurs at the location $a_\star = a_\text{res}^{\text{pre}}$ for a given $a_\infty$. In Fig. 4, the upper panel clarifies the resonance locations when $m_{12} = 50M_\odot$. The region of interest where the outer orbit potentially undergoes $e_\star$ excitation due to the apsidal precession resonance is located within a wide range of $a_\star$ (or $P_\star$).

The lower panels of Fig. 4 show the results for the averaged maximum changes of the outer eccentricity ($\Delta e_\star^{\text{peak}}$), over all 100 runs, as a function of $a_\star$ for different
BHB masses. A remarkable eccentricity excitation is achieved for all tested values of the BHB mass. For the $m_{12} = 20 \, M_\odot$ case, the maximum eccentricity growth is found for the smallest $a_*$, and decreases for larger $a_*$. For the BHBs ($m_{12}/M_\odot = 50, 100$), the perturbation becomes stronger, and the induced peak eccentricity can be so high (because of $e^*_{\text{peak}} \propto \mu_0$) that some of the systems with small $a_*$ can become unbound. The peak of $\Delta e^*_{\text{peak}}$ appears to shift to larger $a_*$ for larger BHB masses. The decrease of $\Delta e^*_{\text{peak}}$ with increasing $a_*$ is the result of the secular time scale of generating the eccentricity growth (see Fig. 3).

Note that, in principle, the resonance can occur as $a_* \leq a^*_{\text{Res}}$ (the vertical blue line; $P_\star \lesssim 160$ days). As shown, more systems can have larger $\Delta e^*_{\text{peak}}$ values when the evolution time is longer (see Fig. 2). We find that $e^*_{\text{peak}}$ excitation is mainly contributed by the inner BHBs with relatively small mass ratios ($m_i/m_1 \lesssim 0.5$).

The secular variability of the orbital eccentricity induces a change in the projected orbit that may be probed via astrometric monitoring with surveys such as Gaia [91]. To determine detectability with Gaia, we compute the signal-to-noise ratio (SNR) for astrometric detection, $\rho = \theta_{\text{signal}}/\theta_{\text{Gaia}}$. Assuming that the signal can be well approximated by the change in the apocenter, the maximum such signal for a system at distance $D$ is approximated by

$$\theta_{\text{signal}}(D) \approx \frac{a_* \Delta e^*_{\text{peak}}}{D}. \quad (10)$$

To compute the noise we follow Ref. [92], which drew upon Refs. [93–97] to evaluate the Gaia astrometric precision for a single scan. Here, we assume that our source is a solar-type star with an absolute $V$-band magnitude of $-26.8$, and $V - I_C = 0.688$ [98]. Following Ref. [96], the single-scan precision is computed from the end-of-mission, sky-averaged parallax uncertainty $\theta_{\text{com}}(D)$ as

$$\theta_{\text{Gaia}}(D) \equiv \frac{\sqrt{140}}{1.1 \times 2.15} \theta_{\text{com}}(D). \quad (11)$$

The prefactors account for an average $140$ Gaia visits over 10 y, a geometrical averaging factor of 2.15, and a contingency margin of 1.1 [96]. Note that the contingency margin is 1.1 instead of the value of 1.2 chosen in Ref. [96]. This is based on the newest information from Gaia EDR3 uncertainties, as given in Sec. 1 of Ref. [99]. To compute the end-of-mission astrometric precision, we use the most up-to-date fitting formula from the Gaia document [99],

$$\theta_{\text{com}}(D) = 0.527[40 + 800Z + 30Z^2]^{1/2} \mu\text{as}$$

$$Z \equiv \max \{10^{0.4[13.0–15.0]}, 10^{0.4[G–15.0]}\}$$

$$G = m_V(D) - 0.01746 + 0.008092(V - I_C) - 0.2810(V - I_C)^2 + 0.03655(V - I_C)^3. \quad (12)$$

Here the 0.527 prefactor is for a 10-year mission (referred to as Gaia DR5 in Ref. [99]), the conversion between Gaia $G$ and $V$ magnitudes (in the last line above) is given in Table A2 of Ref. [100], and $m_V(D) = -26.8 + 2.5\log_{10}[(D/\text{AU})^2]$ is the apparent magnitude of a Sun-like star at distance $D$ in AU.

Figure 5 summarizes the optimal-characteristic SNR as a function of distance to the source and outer orbital period,
Fig. 5. Detectability of the change of the outer stellar eccentricity in the \( P_\star - D \) plane with \textit{Gaia}, which is evaluated using Eqs. (10) and (11), and \( \Delta e_{\text{peak}}^{\star} \) is given by the data from Fig. 4 for 10 y. The top panel shows an example of detectability where the source is at \( D = 900 \) pc, and the shaded region corresponds to systems with \( \theta_{\text{signal}} \geq \theta_{\text{Gaia}} \). The white dashed lines specify the region with \( \rho > 2 \).

For three different inner binary masses. Here we use the data from Fig. 4 that gives the maximum change of eccentricity for a range of \( a_{\star} \) over 10 y (for \( m_{12} = 100 M_\odot \), we assume \( \Delta e_{\text{peak}}^{\star} \)), due to the long-term instability). We see that the overall SNR improves as the distance \( D \) decreases, and the boundary of detectability is marked at \( \sim 10^3 \) pc given by \( \rho = 2 \). Two peaks of high SNR are the results of the pure \( e_{\star} \) excitation (Fig. 4) and the enhancement of \( \theta_{\text{signal}} \) from wide binaries. Although the detectability here is evaluated based only on \( \Delta e_{\text{peak}}^{\star} \), the outer pericenter argument may change in time in the detection [75]. When the triple system is inclined, a combination of predicted changes in orbital inclination and line-of-sight orbital projection can also increase or decrease our estimate here. Our results are characteristic of the optimal astrometric signatures over the course of the \textit{Gaia} mission.

Note that the average time between visits is \( \sim 26 \) days, and hence the shorter-period systems may be sampled at suborbital frequencies. However, because this is a secular effect, even a longer-than-orbital sampling rate could probe the longer-time-scale secular change of the projected orbit. Followup analysis must simulate mock systems to determine the required orbital sampling rate and SNR needed to reliably detect this effect. Further work is also required to determine in which cases the current \textit{Gaia} pipeline would flag such secularly evolving systems as binaries with an unseen companion, or misidentify them due to difficulty in fitting to a Keplerian orbit.

IV. SUMMARY AND DISCUSSION

We have studied a novel secular dynamical effect of a solar-type star around a compact BHB in a nearly coplanar triple configuration. We pointed out that the stellar orbit may experience significant oscillations in the orbital eccentricity if the system satisfies an “apsidal precession resonance.” Starting with an eccentric inner BHB, the outer eccentricity can be excited due to the resonance and the enhancement becomes stronger as the inner eccentricity increases. This effect, which can drive the eccentricity of the outer orbits close to unity, was overlooked in all previous studies and may have applications for other types of systems, such as a planet around a binary star or a star/compact object around a supermassive BH binary with/without a gaseous disc.

Note that the apsidal precession resonance allows angular momentum exchange to occur efficiently between the inner and outer orbits, leading to a transfer of eccentricity. One case that we did not include in our study is the triple systems with \( e_{\odot} = 0 \) and \( e_{\odot} = 0.9 \). In this situation, the inner (outer) binary is expected to become more (less) eccentric as the resonance occurs.

Figure 6 shows the parameter space where the apsidal precession resonance can play a role, on the basis of \( \omega_{\odot}(e_{\odot}) = \omega_{\star}(e_{\star}) \). Compared to the fiducial cases (left panel), the resonance region for the initially stable systems in the right panel is shifted to larger \( a_{\star} \) (or \( P_{\star} \)). Therefore, the corresponding semimajor axis of the inner BHB (\( a_{\odot} \)) becomes larger, leading to a much lower GW frequency range (i.e., outside of the LISA band).

Figure 7 shows the change in eccentricities due to resonance for both the inner and outer binary, including the examples identified in Fig. 6. In the left panel (fiducial case) we see that the inner eccentricity decreases (i.e., \( \Delta e_{\odot} = 0.01 \)) when the outer eccentricity is excited. In the right panel we find that the eccentricities evolve in an opposite way. The inner binary can efficiently gain some eccentricity from the outer binary during the resonance.
system parameters are $m_2 = 50 M_\odot$, $m_1/m_2 = 0.2$, $e_i^0 = 0.9$, $P_i = 15$ days (left panel), and $e_i^0 = 0$, $P_i = 800$ days (right panel). Upper panels: ratio of apsidal precession rate. Lower panels: these results (black and red lines) are obtained by numerically integrating the SA equations for 25 y (left panel) and $6 \times 10^3$ y (right panel).

FIG. 7. Similar to the middle panel of Fig. 1, but we include the change in eccentricities of both the inner and outer binaries. The system parameters are $m_2 = 50 M_\odot$, $m_1/m_2 = 0.2$, $e_i^0 = 0.9$, $e_o^0 = 0$, $P_i = 15$ days (left panel), and $e_i^0 = 0$, $e_o^0 = 0.9$, $P_i = 800$ days (right panel). Upper panels: ratio of apsidal precession rate. Lower panels: these results (black and red lines) are obtained by numerically integrating the SA equations for 25 y (left panel) and $6 \times 10^3$ y (right panel).

(the peak value is about $\Delta e_{in}^{max} \sim 0.5$), while the outer eccentricity can decrease by a factor of $\lesssim 0.2$.

Since we are interested in the change of $e_i$ induced by the LISA source within $\sim 10$ y, we did not include this type of system (with $e_i^0 = 0$ and $e_o^0 = 0.9$) in our main study.

The formation of compact massive BHB + star systems may be challenging. The progenitor stars of these BHBs usually expand by hundreds or thousands of solar radii throughout their evolution, likely dynamically interacting with the tertiary star. However, some low-metallicity massive stellar binaries might remain compact throughout their evolution [12], allowing for dynamically stable compact triples [101]. Alternatively, a BHB can be formed first and eventually capture a long-lived low-mass star. Note that our analysis is not restricted to any specific formation scenarios, and can be adapted to other types of systems by applying scaling relations.

We found that the secular variability of the stellar orbit’s apocenter induced by the changing eccentricity is detectable by Gaia for inner BHBs emitting GWs in the LISA frequency range. Assuming that the formation and merger rates of BHBs are in equilibrium, we expect to have hundreds of BHBs in the LISA band in our Galaxy based on the LIGO detection rate [102–107]. Since our proposed secular variability can only be resolved by Gaia within several kpc, the expected number of sources that LISA and Gaia could see becomes $\sim$ a few. Although the actual number of LISA sources accompanied by a tertiary star in our Galaxy is quite uncertain, identifying the secular motion of stellar orbits in current (Gaia Data Release 3 [91]) and future Gaia data is timely.

Our proof-of-concept calculations demonstrate that the long-term evolution of the eccentricity of a nearby stellar orbit can serve as a distinctive imprint of such an unseen binary companion. Precise measurements of secular variability are therefore an independent approach to reveal hidden BHBs, in addition to GW detection. We emphasize that the inner binary systems that generate Gaia-detectable variations in the orbits of their stellar tertiary also emit GWs in the LISA band. Therefore, Gaia may provide candidate LISA sources before LISA is launched (planned for the 2030s). In this sense, a joint detection with Gaia and LISA [108–110] would be a unique multimessenger tool to understand the evolution, fate, and configurations of compact BHBs.

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