Charged-particle multiplicity fluctuations in Pb-Pb collisions at root $s(\text{NN})=2.76$ TeV

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Charged-particle multiplicity fluctuations in Pb–Pb collisions at \( \sqrt{s_{NN}} = 2.76 \) TeV

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Abstract Measurements of event-by-event fluctuations of charged-particle multiplicities in Pb–Pb collisions at \( \sqrt{s_{NN}} = 2.76 \) TeV using the ALICE detector at the CERN Large Hadron Collider (LHC) are presented in the pseudorapidity range \( |\eta| < 0.8 \) and transverse momentum \( 0.2 < p_T < 2.0 \) GeV/c. The amplitude of the fluctuations is expressed in terms of the variance normalized by the mean of the multiplicity distribution. The \( \eta \) and \( p_T \) dependences of the fluctuations and their evolution with respect to collision centrality are investigated. The multiplicity fluctuations tend to decrease from peripheral to central collisions. The results are compared to those obtained from HIJING and AMPT Monte Carlo event generators as well as to experimental data at lower collision energies. Additionally, the measured multiplicity fluctuations are discussed in the context of the isothermal compressibility of the high-density strongly-interacting system formed in central Pb–Pb collisions.

1 Introduction

According to quantum chromodynamics (QCD), at high temperatures and high energy densities, nuclear matter undergoes a phase transition to a deconfined state of quarks and gluons, the quark–gluon plasma (QGP) [1–5]. Heavy-ion collisions at ultra-relativistic energies make it possible to create and study such strongly-interacting matter under extreme conditions. The QGP formed in high-energy heavy-ion collisions has been characterised as a strongly-coupled system with very low shear viscosity. The primary goal of the heavy-ion program at the CERN Large Hadron Collider (LHC) is to study the QCD phase structure by measuring the properties of QGP matter. One of the important methods for this study is the measurement of event-by-event fluctuations of experimental observables. These fluctuations are sensitive to the proximity of the phase transition and thus provide information on the nature and dynamics of the system formed in the collisions [6–12]. Fluctuation measurements provide a powerful tool to investigate the response of a system to external perturbations. Theoretical developments suggest that it is possible to extract quantities related to the thermodynamic properties of the system, such as entropy, chemical potential, viscosity, specific heat, and isothermal compressibility [6,13–21]. In particular, isothermal compressibility expresses how a system’s volume responds to a change in the applied pressure. In the case of heavy-ion collisions, it has been shown that the isothermal compressibility can be calculated from the event-by-event fluctuation of charged-particle multiplicity distributions [17].

The measured multiplicity scales with the collision centrality in heavy-ion collisions. The distribution of particle multiplicities in a given class of centrality and its fluctuations on an event-by-event basis provide information on particle production mechanisms [22–24]. In this work, the magnitude of the fluctuations is quantified in terms of the scaled variance,

\[
\omega_{\text{ch}} = \frac{\sigma_{\text{ch}}^2}{\langle N_{\text{ch}} \rangle},
\]

where \( \langle N_{\text{ch}} \rangle \) and \( \sigma_{\text{ch}}^2 \) denote the mean and variance of the charged-particle multiplicity distribution, respectively. Event-by-event multiplicity fluctuations in heavy-ion collisions have been studied earlier at the BNL-AGS by E802 [25], the CERN-SPS by the WA98 [26], NA49 [27,28], and CERES [29] experiments, and at the Relativistic Heavy Ion Collider (RHIC) by the PHOBOS [30] and PHENIX [31] experiments. A compilation of available experimental data and comparison to predictions of the event generators are presented elsewhere [19]. In this work, measurements of the scaled variance of multiplicity fluctuations are presented as a function of collision centrality in Pb–Pb collisions at \( \sqrt{s_{NN}} = 2.76 \) TeV using the ALICE detector at the LHC.

In thermodynamics, the isothermal compressibility (\( k_T \)) is defined as the fractional change in the volume of a system with change of pressure at a constant temperature,

\[
k_T = -\frac{1}{V} \left. \frac{\partial V}{\partial P} \right|_T,
\]
where $V$, $T$, $P$ are the volume, temperature, and pressure of the system, respectively. In general, an increase in the applied pressure leads to a decrease in volume, so the negative sign makes the value of $kT$ positive. In the context of a description in terms of the grand canonical ensemble, which is approximately applicable for the description of particle production in heavy-ion collisions [5], the scaled variance of the multiplicity distribution can be expressed as [17],

$$\omega_{\text{ch}} = \frac{k_B T \langle N_{\text{ch}} \rangle}{V} k_T,$$

(3)

where $k_B$ is the Boltzmann’s constant, and $\langle N_{\text{ch}} \rangle$ is the average number of charged particles. Measurements of fluctuations in terms of $\omega_{\text{ch}}$ can be exploited to determine $k_T$ and associated thermodynamic quantities such as the speed of sound within the system [17,32].

Measurements of the multiplicity of produced particles in relativistic heavy-ion collisions are basic to most of the studies as a majority of the experimentally observed quantities are directly related to the multiplicity. The variation of the multiplicity depends on the fluctuations in the collision impact parameter or the number of participant nucleons. Thus, the measured multiplicity fluctuations contain contributions from event-by-event fluctuations in the number of participant nucleons, which forms the main background towards the evaluation of any thermodynamic quantity [33,34]. This has been partly addressed by selecting narrow intervals in centrality and accounting for the multiplicity variation within the centrality of the measurement. The remainder of participant fluctuations is estimated in the context of an MC Glauber model in which nucleus–nucleus collisions are considered to be a superposition of nucleon–nucleon interactions.

Thus, the background fluctuations contain contributions from independent particle production and correlations corresponding to different physical origins. The background-subtracted fluctuations can be used in Eq. (3) to estimate $k_T$ with the knowledge of the temperature and volume from complementary analyses of hadron yields, calculated at the chemical freeze-out [35,36].

In addition to fluctuations in the number of participant nucleons, several other processes contribute to fluctuations of the charged particles multiplicity on an event-by-event basis [17,37]. These include long-range particle correlations, charge conservation, resonance production, radial flow, as well as Bose–Einstein correlations. Since these contributions can not be evaluated directly, the value of $k_T$ extracted and reported in this work amounts to an upper limit.

The article is organized as follows. In Sect. 2, the experimental setup and details of the data analysis method, including event selection, centrality selection, corrections for finite width of the centrality intervals, and particle losses are presented. In Sect. 3, the measurements of the variances of multiplicity distributions are presented as a function of collision centrality. Additionally, the dependence of the fluctuations on the $\eta$ and $p_T$ ranges of the measured charged hadrons are studied. The results are compared with calculations from selected event generators. In Sect. 4, methods used to estimate multiplicity fluctuations resulting from the fluctuations of the number of participants are discussed. An estimation of the isothermal compressibility for central collisions is made in Sect. 5.

2 Experimental setup and analysis details

The ALICE experiment [38] is a multi-purpose detector designed to measure and identify particles produced in heavy-ion collisions at the LHC. The experiment consists of several central barrel detectors positioned inside a solenoidal magnet operated at 0.5 T field parallel to the beam direction and a set of detectors placed at forward rapidities. The central barrel of the ALICE detector provides full azimuthal coverage for track reconstruction within a pseudorapidity ($\eta$) range of $|\eta| < 0.8$. The Time Projection Chamber (TPC) is the main tracking detector of the central barrel, consisting of 159 pad rows grouped into 18 sectors that cover the full azimuth. The Inner Tracking System (ITS) consists of six layers of silicon detectors employing three different technologies. The two innermost layers are Silicon Pixel Detectors (SPD), followed by two layers of Silicon Drift Detectors (SDD), and finally, the two outermost layers are double-sided Silicon Strip Detectors (SSD). The V0 detector consists of two arrays of scintillators located on opposite sides of the interaction point (IP). It features full azimuthal coverage in the forward and backward rapidity ranges, $2.8 < \eta < 5.1$ (VOA) and $-3.7 < \eta < -1.7$ (VOC). The V0 detectors are used for event triggering purposes as well as to evaluate the collision centrality on an event-by-event basis [39].

The impact of the detector response on the measurement of charged-particle multiplicity based on Monte Carlo simulations is studied with the GEANT3 framework [40].

This analysis is based on Pb–Pb collision data recorded in 2010 at $\sqrt{s_{NN}} = 2.76$ TeV with a minimum-bias trigger comprising of a combination of hits in the V0 detector and the two innermost (pixel) layers of the ITS. In total, 13.8 million minimum-bias events satisfy the event selection criteria. The primary interaction vertex of a collision is obtained by extending correlated hits in the two SPD layers to the beam axis. The longitudinal position of the interaction vertex in the beam ($z$) direction ($V_z$) is restricted to $|V_z| < 10$ cm to ensure a uniform acceptance in the central $\eta$ region. The interaction vertex is also obtained from TPC tracks. The event selection includes an additional vertex selection criterion, where the difference between the vertex using TPC tracks and the vertex using the SPD is less than 5 mm in the $z$-direction. This
selection criterion greatly suppresses the contamination of the primary tracks by secondary tracks resulting from weak decays and spurious interactions of particles within the apparatus.

Charged particles are reconstructed using the combined information of the TPC and ITS [38]. In the TPC, tracks are reconstructed from a collection of space points (clusters). The selected tracks are required to have at least 80 reconstructed space points. Different combinations of tracks in the TPC and SPD hits are utilized to correct for detector acceptances and efficiency losses. To suppress contributions from secondary tracks (i.e., charged particles produced by weak decays and interactions of particles with materials of the detector), the analysis is restricted to charged-particle tracks featuring a distance of closest approach (DCA) to the interaction vertex, \( DCA_{xy} < 2.4 \text{ cm} \) in the transverse plane and of \( DCA_z < 3.2 \text{ cm} \) along the beam direction. The tracks are additionally restricted to the kinematic range, \(|\eta| < 0.8 \) and \( 0.2 < p_T < 2.0 \text{ GeV}/c \).

### 2.1 Centrality selection and the effect of finite width of the centrality intervals

The collision centrality is estimated based on the sum of the amplitudes of the V0A and V0C signals (known as the V0M collision centrality estimator) [39]. Events are classified in percentiles of the hadronic cross section using this estimator. The average number of participants in a centrality class, denoted by \( N_{\text{part}} \), is obtained by comparing the V0M multiplicity to a geometrical Glauber model [41]. Thus, the centrality of the collision is measured based on the V0M centrality estimator, whereas the measurement of multiplicity fluctuations is based on charged particles measured within the acceptance of the TPC.

A given centrality class is a collection of events of measured multiplicity distributions within a range in V0M corresponding to a mean number of participants, \( \langle N_{\text{part}} \rangle \). This results in additional fluctuations in the number of particles within each centrality class. To account for these fluctuations, a centrality interval width correction is employed. The procedure involves dividing a broad centrality class into several narrow intervals and correcting for the finite interval using weighted moments according to [42,43],

\[
X = \sum_{i} n_i X_i \frac{1}{\sum_{i} n_i}.
\]

Here, the index \( i \) runs over the narrow centrality intervals. \( X_i \) and \( n_i \) are the corresponding moments of the distribution and number of events in the \( i \)th interval, respectively. With this, one obtains, \( N = \sum n_i \) as the total number of events in the broad centrality interval.

The centrality resolution of the combined V0A and V0C signals ranges from 0.5% in central to 2% in the most peripheral collisions [39]. A correction for the finite width of centrality intervals has been made with Eq. 4 using 0.5% centrality intervals from central to 40% cross-section and 1% intervals for the rest of the centrality classes.

### 2.2 Efficiency correction

The detector efficiency factors \( \varepsilon \) were evaluated in bins of pseudorapidity \( \eta \), azimuthal angle \( \varphi \), and \( p_T \). By defining \( N_{\text{ch}}(x) \) as the number of produced particles in a phase-space bin at \( x \), \( n(x) \) as the number of observed particles at \( x \), and \( \varepsilon(x) \) as the detection efficiency, the first and second factorial moments of the multiplicity distributions can be corrected for particle losses according to the procedure outlined in Refs. [44,45]:

\[
F_1 = \langle N_{\text{ch}} \rangle = \sum_{i=1}^{m} \langle N_{\text{ch}}(x_i) \rangle = \sum_{i=1}^{m} \frac{n(x_i)}{\varepsilon(x_i)},
\]

\[
F_2 = \sum_{i=1}^{m} \sum_{j=1}^{m} \frac{n(x_i)n(x_j) - \delta_{x_i x_j}}{\varepsilon(x_i)\varepsilon(x_j)},
\]

respectively. Here, \( m \) denotes the index of the phase-space bins and \( i, j \) are the bin indexes. \( \delta_{x_i x_j} = 1 \) if \( x_i = x_j \) and zero otherwise. The variance of the charged-particle multiplicity is then calculated as:

\[
\sigma_{\text{ch}}^2 = F_2 + F_1 - F_1^2.
\]

The correction procedure is validated by a Monte Carlo study employing two million Pb–Pb events at \( \sqrt{s_{NN}} = 2.76 \text{ TeV} \) generated using the HIJING event generator [46], and passed through GEANT3 simulations of the experimental setup, taking care of the acceptances of the detectors. The efficiency dependencies on \( \eta \), \( \varphi \), and \( p_T \) are calculated from the ratio of the number of reconstructed charged particles by the number of produced particles. In order to account for the \( p_T \) dependence of efficiency, the full \( p_T \) range (0.2 < \( p_T < 2.0 \text{ GeV}/c \)) was divided to nine bins (0.2–0.3, 0.3–0.4, 0.4–0.5, 0.5–0.6, 0.6–0.8, 0.8–1.0, 1.0–1.2, 1.2–1.6, 1.6–2.0) with larger number of bins in low \( p_T \) ranges. In the Monte Carlo closure test, the values of \( \langle N_{\text{ch}} \rangle \), \( \sigma_{\text{ch}} \), and \( \omega_{\text{ch}} \) of the efficiency corrected results from the simulated events are compared to those of HIJING at the generator level to obtain the corrections. By construction, the efficiency corrected values for \( \langle N_{\text{ch}} \rangle \) match with those from the generator, whereas \( \sigma_{\text{ch}} \) and \( \omega_{\text{ch}} \) values differ by \( \sim 0.7 \) and \( \sim 1.4\% \), respectively. These differences are included in the systematic uncertainties.

### 2.3 Statistical and systematic uncertainties

The statistical uncertainties of the moments of multiplicity distributions are calculated based on the method of error
Table 1 Systematic uncertainties on the mean, standard deviation, and scaled variance of charged-particle multiplicity distributions from different sources. The ranges of uncertainties quoted correspond to central to peripheral collisions.

<table>
<thead>
<tr>
<th>Source</th>
<th>$\langle N_{ch} \rangle$</th>
<th>$\sigma_{ch}$</th>
<th>$\omega_{ch}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Track selection</td>
<td>3.5–4.8%</td>
<td>3.8–6.0%</td>
<td>4.0–7.5%</td>
</tr>
<tr>
<td>Variation of $DC A_{xy}$</td>
<td>0.5–0.9%</td>
<td>0.8–1.2%</td>
<td>1.3–1.6%</td>
</tr>
<tr>
<td>Variation of $DC A_{z}$</td>
<td>0.4–0.9%</td>
<td>0.7–1.0%</td>
<td>1.2–1.7%</td>
</tr>
<tr>
<td>Vertex ($V_z$) selection</td>
<td>0.1–0.5%</td>
<td>0.5%</td>
<td>0.1–0.8%</td>
</tr>
<tr>
<td>Removal of $V_x$, $V_y$ selections</td>
<td>0.1%</td>
<td>0.2%</td>
<td>0.5%</td>
</tr>
<tr>
<td>Efficiency correction</td>
<td>&lt; 0.1%</td>
<td>0.7%</td>
<td>1.4%</td>
</tr>
<tr>
<td>Magnetic polarity</td>
<td>0.2–1.0%</td>
<td>0.5–1.5%</td>
<td>0.8–1.7%</td>
</tr>
<tr>
<td>Total</td>
<td>3.5–5.1%</td>
<td>4.1–6.4%</td>
<td>4.8–8.3%</td>
</tr>
</tbody>
</table>

Propagation derived from the delta theorem [47]. The systematic uncertainties have been evaluated by considering the effects of various criteria in track selection, vertex determination, and efficiency corrections.

The systematic uncertainties related to the track selection criteria were obtained by varying the track reconstruction method and track quality cuts. The nominal analysis was carried out with charged particles reconstructed within the TPC and ITS. For systematic checks, the full analysis is repeated for tracks reconstructed using only the TPC information. The differences in the values of $\langle N_{ch} \rangle$, $\sigma_{ch}$, and $\omega_{ch}$ resulting from the track selections using the two methods are listed in Table 1 as a part of the systematic uncertainties. The $DC A_{xy}$ and $DC A_{z}$ of the tracks are varied by ±25% to obtain the systematic uncertainties caused by variations in the track quality selections. The effect of the selection of events based on the vertex position is studied by restricting the $z$-position of the vertex to ±5 cm from the nominal ±10 cm, and additionally by removing restrictions on $V_x$ and $V_y$. The efficiency correction introduces additional systematic uncertainty as discussed earlier. The experimental data were recorded for two different magnetic field polarities. The two data sets are analyzed separately and the differences are taken as a source of systematic uncertainties.

The individual sources of systematic uncertainties discussed above are considered uncorrelated and summed in quadrature to obtain the total systematic errors reported in this work. Table 1 lists the systematic uncertainties associated with the values of $\langle N_{ch} \rangle$, $\sigma_{ch}$, and $\omega_{ch}$.

3 Results and discussions

Figure 1 shows the corrected mean ($\langle N_{ch} \rangle$), standard deviation ($\sigma_{ch}$), and scaled variance ($\omega_{ch}$) of charged-particle multiplicity distributions as a function of the number of participating nucleons for experimental data along with HIJING and AMPT (string melting) models for Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV, shown in panels a, b, and c, respectively. For panel a, $\langle N_{part} \rangle$ for the two models are shifted for better visibility. The statistical uncertainties are smaller than the size of the markers. The systematic uncertainties are presented as filled boxes.

3.1 Comparison with models

The measured $\omega_{ch}$ values are compared with the results of simulations with the HIJING and the string melting option of the AMPT models. HIJING [46] is a Monte Carlo event generator for parton and particle production in high-energy hadronic and nuclear collisions and is based on QCD-inspired models which incorporate mechanisms such as multiple minijet production, soft excitation, nuclear shadowing of parton distribution functions, and jet interactions in the participants, $\langle N_{part} \rangle$, obtained from Ref. [38], are smaller than the width of the solid red circles used to present the data in the centrality range considered in this measurement. It is observed that the values of $\langle N_{ch} \rangle$ and $\sigma_{ch}$ increase with increasing $\langle N_{part} \rangle$. The value of $\omega_{ch}$ decreases monotonically by ~29% from peripheral to central collisions.
dense hadronic matter. The HIJING model treats a nucleon-nucleus collision as a superposition of many binary nucleon-nucleon collisions. In the AMPT model [48], the initial parton momentum distribution is generated from the HIJING model. In the default mode of AMPT, energetic partons recombine and hadrons are produced via string fragmentation. The string melting mode of the model includes a fully partonic phase and hadrons are produced via string fragmentation. The string melting model is useful in extrapolating fluctuations to different coverages.

In order to enable a proper comparison with data obtained in this work, Monte Carlo events produced with HIJING and AMPT are grouped in collision centrality classes based on generator level charged-particle multiplicities computed in Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV, shown in panels a, and b, respectively. The estimated $\omega_{ch}$ for $|\eta| < 0.3$ and $|\eta| < 0.5$ are obtained from the experimental data of $|\eta| < 0.8$ by using Eq. 8. The estimated $\omega_{ch}$ for $0.2 < p_T < 1.5$ GeV/c and $0.2 < p_T < 1.0$ GeV/c are obtained from the experimental data of $0.2 < p_T < 2.0$ GeV/c, also by using Eq. 8. The statistical uncertainties are smaller than the size of the markers. The systematic uncertainties are presented as filled boxes.

Charged-particle multiplicity distributions depend on the acceptance of the detection region. Starting with the measured multiplicity fluctuations within $|\eta| < 0.8$ and $0.2 < p_T < 2.0$ GeV/c with a mean $(N_{ch})$ and scaled variance of $\omega_{ch}$, the scaled variance ($\omega_{ch}^{acc}$) for a fractional acceptance in $\eta$ or for a limited $p_T$ range with mean of $(N_{ch}^{acc})$ can be expressed as [31].

$$\omega_{ch}^{acc} = 1 + f^{acc}(\omega_{ch} - 1),$$

where

$$f^{acc} = \frac{N_{ch}^{acc}}{N_{ch}}.$$  

This empirical estimation for the acceptance dependence of the scaled variance is valid assuming that there are no significant correlations present over the acceptance range being studied. The validity of this dependence has been checked by comparing the experimental data of scaled variances at reduced acceptances along with the results from the above calculations. This is shown in Fig. 2 for different $\eta$ or $p_T$ ranges. In the top panel, the scaled variances are shown, as a function of $(N_{part})$, for three $\eta$ ranges. The solid symbols show the results of measured scaled variances, whereas open symbols show the estimated values for the two reduced $\eta$ windows. The calculated values yield a good description of the measured data points. The choice of the $p_T$ range also affects the multiplicity of an event. In the bottom panel of Fig. 2, the scaled variances are shown, as a function of $(N_{part})$, for three $p_T$ ranges keeping $|\eta| < 0.8$. A decrease in the value of $\omega_{ch}$ is observed with the decrease of the $p_T$ window. The results from the calculations of scaled variances are compared to the measured data points. The calculated values are close to those of the measurement. This estimation of the scaled variances of multiplicity distributions is particularly useful in extrapolating fluctuations to different coverages.
3.3 Comparison to scaled variances at lower collision energies

Scaled variances of charged-particle multiplicity distributions were earlier reported by the PHENIX Collaboration at RHIC for Au–Au collisions at \( \sqrt{s_{NN}} = 62.4 \) and 200 GeV [31]. The beam–beam counters (BBC) in PHENIX covering the full azimuthal angle in the pseudorapidity range \( 3.0 < |\eta| < 3.9 \) provided the minimum-bias trigger and were used for centrality selection. The pseudorapidity acceptance of the PHENIX experiment amounted to \( |\eta| < 0.26 \) with an effective average azimuthal active area of 2.1 radian and \( 0.2 < p_T < 2.0 \text{ GeV}/c \) for charged particle measurements. The published results of mean and scaled variances of charged-particles were corrected for fluctuations of the collision geometry within a centrality bin. This was performed by comparing fluctuations from simulated HIJING events with a fixed impact parameter to events with a range of impact parameters covering the width of the centrality bin, as determined from Glauber model simulations. The corrected results are reproduced in Fig. 3 for the two collision energies. To enable an appropriate comparison with results reported by PHENIX, the ALICE data are reanalyzed by imposing the same kinematic ranges as in PHENIX, and the resulting mean and scaled variances are presented in Fig. 3. It is observed that for the same acceptance and kinematic cuts, the mean values and the scaled variances are larger at the LHC energy compared to those obtained at RHIC energies.

It is also of interest to study \( \frac{\sigma^2}{\langle N_{ch} \rangle^2} \), the ratio of the variance by the square of the average multiplicity as a function of collision centrality. At lower beam energies, these distributions obey a power-law relative to the number of participants [49]. In the lower panel of Fig. 3, the values of \( \frac{\sigma^2}{\langle N_{ch} \rangle^2} \) are presented as a function of \( \langle N_{\text{part}} \rangle \) for the ALICE data, for the common coverage of ALICE and PHENIX data, as well as PHENIX data at two collision energies. The data points are fitted by a scaling curve, \( \frac{\sigma^2}{\langle N_{ch} \rangle^2} = A \cdot N_{\text{part}}^{-\alpha} \). The exponent \( \alpha = -1.25 \pm 0.03 \) fits the four sets of experimental data well with \( \chi^2/\text{ndf} \) (where ndf is the number of degrees of freedom) as 0.88, 1.1, 0.95, 0.84 for Pb–Pb collisions at \( \sqrt{s_{NN}} = 2.76 \text{ TeV} \) with the ALICE acceptance, the PHENIX detector acceptance and Au–Au collisions at \( \sqrt{s_{NN}} = 200 \text{ GeV} \) and 62.4 GeV, respectively. The scaling, first described by the PHENIX Collaboration [49], also holds for the ALICE data. The corresponding values of \( \frac{\sigma^2}{\langle N_{ch} \rangle^2} \) for HIJING and AMPT models for Pb–Pb collisions at \( \sqrt{s_{NN}} = 2.76 \text{ TeV} \) are also displayed in Fig. 3. The trends as a function of centrality are observed to be similar to those of the experimental data. Fits with a similar scaling curve yield power-law exponents as \( -1.1 \) and \( -1.05 \) for HIJING and AMPT models, respectively. These exponents for the models are lower compared to those of the experimental data.

4 Background to the measured multiplicity fluctuations

The background to the measured multiplicity fluctuations contains contributions from several sources. In this section, the background fluctuations are presented first from a par-
the detector. Within the context of this framework, the scaled fluctuations are also strongly dependent on the acceptance of each nucleon–source within the detector acceptance, calculated. The V0 detector coverage (2) arises in part from fluctuations in Pb–Pb collisions are considered to be a superposition of participant model calculation and then the expectations from a Poisson distribution of particle multiplicity are discussed. In the wounded nucleon model, nucleus–nucleus (such as Pb–Pb) collisions are considered to be a superposition of individual nucleon–nucleon interactions. In this context, the fluctuations in multiplicity within a given centrality window arise in part from fluctuations in $N_{\text{part}}$ and from fluctuations in the number of particles ($n$) produced by each nucleon–nucleon interaction [22,26,31]. The values of $n$ and their fluctuations are also strongly dependent on the acceptance of the detector. Within the context of this framework, the scaled variance of the background, $\omega_{\text{ch}}^{\text{back}}$, amounts to

$$\omega_{\text{ch}}^{\text{back}} = \omega_n + \langle n \rangle \omega_{N_{\text{part}}}, \quad (10)$$

where $\langle n \rangle$ is the average number of particles produced by each nucleon–source within the detector acceptance, $\omega_n$ is the scaled variance of the fluctuations in $n$, and $\omega_{N_{\text{part}}}$ denotes the fluctuations in $N_{\text{part}}$. The variance, $\omega_{N_{\text{part}}}$ is calculated using event-by-event $N_{\text{part}}$ from the HIJING model. The distribution of $N_{\text{part}}$ corresponds to the centrality obtained within the V0 detector coverage (2.8 < $\eta$ < 5.1 and −3.7 < $\eta$ < −1.7). The extracted values of $\omega_{N_{\text{part}}}$ are corrected for the effects of the finite width of the centrality intervals.

For the central rapidity range ($|\eta| < 0.5$), the measured number of charged particles produced in pp collisions within $0.2 < p_T < 2.0$ GeV/c at $\sqrt{s} = 2.76$ TeV [50] yields $\langle n \rangle = 1.45 \pm 0.07$, which is half of the measured value. In order to calculate $\omega_n$, an extrapolation of the measured $\omega_{\text{ch}}$ is made to $N_{\text{part}} = 2$ using a polynomial fit function of the form $a + bx + cx^2 + dx^3$, which is shown in Fig. 4. In order to calculate $\omega_n$, an extrapolation of the measured $\omega_{\text{ch}}$ is made to $N_{\text{part}} = 2$ using a polynomial fit function of the form $a + bx + cx^2 + dx^3$, which is shown in Fig. 4. Since both the nucleon sources contributing to $N_{\text{part}} = 2$ are correlated, $\omega_n$ becomes half of the extrapolated value, yielding $\omega_n = 1.445 \pm 0.12$. This result is also consistent with the value of $\omega_n = 1.51 \pm 0.16$ obtained from the parameterization given by the PHENIX Collaboration [31].

Using the above numbers, $\omega_{\text{ch}}^{\text{back}}$ are calculated and plotted as a function of $\langle N_{\text{part}} \rangle$ as in Fig. 4. The obtained trend in $\omega_{\text{ch}}^{\text{back}}$ mainly arises from the centrality dependence of $\omega_{N_{\text{part}}}$. For most central collisions, the difference between the measured and background $\omega_{\text{ch}}$ is 0.02±0.18, which is consistent with zero within the uncertainties. Except for most central collisions, $\omega_{\text{ch}}^{\text{back}}$ is observed to be larger than $\omega_{\text{ch}}$. Thus, it seems likely that the background estimated in this way from the participant model is overestimated.

For an ideal gas, the number fluctuations are described by the Poisson distribution. So, if the emitted particles are uncorrelated, then the multiplicity distributions become Poissonian, the magnitude of $\omega_{\text{ch}}$ reduces to unity, which is independent of the multiplicity and thus independent of the centrality of the collision. As seen from Fig. 4, the observed multiplicity fluctuations are significantly above the Poisson expectation for all centralities.

5 Estimation of isothermal compressibility

Equation (3) relates the magnitude of the charged-particle multiplicity fluctuations to the isothermal compressibility. The calculation of $k_T$ requires knowledge of the temperature and volume of the system. After the collision, as the system cools down, the hadronic yields are fixed when the rate of inelastic collisions becomes negligible (chemical freeze-out), but the transverse-momentum distributions continue to change until elastic interactions also cease (kinetic freeze-out). The number of charged particles gets fixed at the time of chemical freeze-out (except for long-lived resonances). As the calculation of $k_T$ depends on the fluctuations in the number of particles, the chemical freeze-out conditions are considered as input. The ALICE Collaboration has published the identified particle yields of pions, kaons, protons, light nuclei, and resonances [36,51,52]. The statistical hadronization models have been successful in describing these yields and their ratios [5,35,53], using temperature and volume as parameters at the chemical freeze-out. For most central Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV, the ALICE data on yields of particles in one unit of rapidity at mid-rapidity are in good agreement with $0.156 \pm 0.002$ GeV and $5330 \pm 505$ fm$^3$, for temperature and volume, respectively [52]. In addition, the charged-particle multiplicity within $|\eta| < 0.5$ in this centrality range is $\langle N_{\text{ch}} \rangle = 1410 \pm 47$ (syst).
Here, an attempt is made to estimate $k_T$ for Pb–Pb collisions using the charged-particle multiplicity fluctuations along with the temperature, volume, and mean number of charged particles from above. The measured multiplicity fluctuation for central collisions is $\omega_{ch} = 2.15 \pm 0.1$. In the absence of any background where the full fluctuation is attributed to have a thermal origin, one would obtain $k_T = 52.1 \pm 5.81 \text{fm}^3/\text{GeV}$. As the measured $\omega_{ch}$ contains background fluctuations from different sources, this value of $k_T$ can be only be considered as an absolute upper limit.

In the previous section, the background fluctuations have been estimated from the participant model calculation as shown in Fig. 4. For central collisions, the value of the measured fluctuation above that of the participant model fluctuation is $\omega_{ch} = 0.02 \pm 0.18$. This leads to $k_T = 0.48 \pm 4.32 \text{fm}^3/\text{GeV}$. On the other hand, the background fluctuations from the participant model for other centralities are larger compared to the measured ones making the background-subtracted fluctuations negative. So it is not possible to obtain estimates of $k_T$ for these centrality ranges based on the present model of participant fluctuations.

The measured multiplicity fluctuations can be viewed as combinations of correlated and uncorrelated fluctuations. If the particle production is completely uncorrelated, the system effectively behaves as an ideal gas, and the multiplicity distribution is expected to follow a Poisson distribution ($\omega_{ch} = 1$). For central collisions, fluctuations above the Poisson estimation gives, $\omega_{ch} = 1.15 \pm 0.06$, which in turn implies a value of $k_T = 27.9 \pm 3.18 \text{fm}^3/\text{GeV}$.

It may be noted that other sources likely also contribute to the background of the measured multiplicity fluctuations. A quantitative determination of these effects requires further studies and theoretical modeling, which is beyond the scope of this work. In view of this, the estimation of $k_T$ from the background-subtracted event-by-event multiplicity fluctuation provides an upper limit of its value.

It is imperative to put the extracted values of $k_T$ in perspective with respect to that of normal nuclear matter. The incompressibility constant of normal nuclear matter at pressure $P$, expressed as $K_0 = 9(\partial P/\partial \rho)$ at zero temperature and normal nuclear density, $\rho = \rho_0$, has been determined to be $K_0 = 240 \pm 20 \text{MeV}$ [54–56]. Using the relation, $k_T = (9/\rho K_0)$, one obtains the isothermal compressibility of nuclear matter to be $k_T \simeq 234 \pm 20 \text{fm}^3/\text{GeV}$. This is consistent with the expectation that normal nuclear matter at low temperature is more compressible than the high temperature matter produced at LHC energies (as of Eq. 3). From the above estimation, the value of $k_T = 27.9 \pm 3.18 \text{fm}^3/\text{GeV}$, which corresponds to multiplicity fluctuations above the Poisson expectation, serves as a conservative upper limit, and is even significantly below the normal nuclear matter at low temperature.

6 Summary

Measurements of event-by-event fluctuations of charged-particle multiplicities are reported as a function of centrality in Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76 \text{TeV}$. The mean, standard deviation, and scaled variances of charged-particle multiplicities are presented for $|\eta| < 0.8$ and $0.2 < p_T < 2.0 \text{GeV/c}$ as a function of centrality. A monotonically decreasing trend for the scaled variance is observed from peripheral to central collisions. Corresponding results from HIJING and AMPT event generators show a mismatch with the experimental results. The scaled variance of the multiplicity decreases with the reduction of the $\eta$ acceptance of the detector as well as with the decrease of the $p_T$ range. The multiplicity fluctuations are compared to the results from lower beam energies as reported by the PHENIX experiment. For the same acceptance, the observed scaled variances at RHIC energies are smaller compared to those observed at the LHC.

As multiplicity fluctuations are related to the isothermal compressibility of the system, the measured fluctuations are used to estimate $k_T$ in central Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76 \text{TeV}$. The multiplicity fluctuations above the Poisson expectation case yields $k_T = 27.9 \pm 3.18 \text{fm}^3/\text{GeV}$, which may still contain contributions from additional uncorrelated particle production as well as from several non-thermal sources as discussed in Sect. 5. Proper modeling of background subtraction needs to be developed by accounting for all possible contributions from different physics origins, which is beyond the scope of the present work. This result serves as a conservative upper limit of $k_T$ until various contributions to the background are properly understood and evaluated. The estimation of $k_T$ at lower collision energies and for different system-sizes is an interesting way to explore the QCD phase diagram from thermodynamics point of view.

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