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Published in:
Monthly Notices of the Royal Astronomical Society

DOI:
10.1093/mnras/stab844

Publication date:
2021

Document version
Publisher's PDF, also known as Version of record

Document license:
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Citation for published version (APA):
From the CMF to the IMF: beyond the core-collapse model

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Accepted 2021 March 19. Received 2021 March 14; in original form 2020 August 5

ABSTRACT
Observations have indicated that the pre-stellar core mass function (CMF) is similar to the stellar initial mass function (IMF), except for an offset towards larger masses. This has led to the idea that there is a one-to-one relation between cores and stars, such that the whole stellar mass reservoir is contained in a gravitationally bound pre-stellar core, as postulated by the core-collapse model, and assumed in recent theoretical models of the stellar IMF. We test the validity of this assumption by comparing the final mass of stars with the mass of their progenitor cores in a high-resolution star formation simulation that generates a realistic IMF under physical condition characteristic of observed molecular clouds. Using a definition of bound cores similar to previous works we obtain a CMF that converges with increasing numerical resolution. We find that the CMF and the IMF are closely related in a statistical sense only; for any individual star there is only a weak correlation between the progenitor core mass and the final stellar mass. In particular, for high-mass stars only a small fraction of the final stellar mass comes from the progenitor core, and even for low-mass stars the fraction is highly variable, with a median fraction of only about 50 per cent. We conclude that the core-collapse scenario and related models for the origin of the IMF are incomplete. We also show that competitive accretion is not a viable alternative.

Key words: stars: formation – MHD – stars: luminosity function, mass function.

1 INTRODUCTION
The origin of the stellar initial mass function (IMF) is still considered an open problem, partly due to a lack of observational constraints. While the overall shape of the IMF is well documented in stellar clusters, its possible dependence on environmental parameters is still unclear. The turbulent nature of star-forming gas compounds the problem, although it may also be viewed as a key to solve it (e.g. Padoan & Nordlund 2002; Hennebelle & Chabrier 2008; Hopkins 2012).

The similarities of the stellar IMF (Kroupa 2001; Chabrier 2005) with the pre-stellar core mass function (CMF) derived from simulations (e.g. Klessen 2001; Tilley & Pudritz 2004, 2007; Padoan et al. 2007; Chabrier & Hennebelle 2010; Schmidt et al. 2010) and observations (e.g. Motte, Andre & Neri 1998; Alves, Lombardi & Lada 2007; Enoch et al. 2007; Nutter & Ward-Thompson 2007; Könyves et al. 2010, 2015; Marsh et al. 2016; Sokol et al. 2019; Könyves et al. 2020; Ladegjlate et al. 2020) has led to the suggestion that pre-stellar cores are true progenitors of stars, meaning that the mass reservoir of a star is fully contained in the progenitor core. The final mass of a star, $M_{\text{star}}$, is then given by that of its progenitor core, $M_{\text{prog}}$, multiplied by an efficiency factor, $\epsilon_{\text{prog}} = \epsilon_{\text{prog}} M_{\text{prog}}$, and the IMF is interpreted as a CMF offset in mass by the factor $\epsilon_{\text{prog}}$ (e.g. Alves et al. 2007; André et al. 2010, 2014).

The idea that in the pre-stellar phase the stellar mass reservoir is fully contained in a bound overdensity is a fundamental assumption in the IMF models of Hennebelle & Chabrier (2008) and Hopkins (2012). A bound overdensity collapses when it becomes gravitationally unstable, and some form of thermal, magnetic, or kinetic support is needed before the start of the collapse, if the overdensity is to accumulate all the stellar mass reservoir. Given the very broad mass range of stars, and the relatively small temperature variations in the dense molecular gas, magnetic and/or kinetic energy support are needed, particularly in the case of the most massive stars that would require the most massive pre-stellar cores (McKee & Tan 2002, 2003). This scenario for the origin of the IMF and massive stars, often referred to as core collapse, has been called into question by results of numerical simulations and observations.

Simulations of star formation in turbulent clouds result in relatively long star-formation time-scales: high-mass protostars acquire their mass on a time-scale comparable to the dynamical time-scale of the star-forming cloud (Bate 2009, 2012; Padoan, Haugbølle & Nordlund 2014; Padoan et al. 2020), which is much longer than the characteristic free-fall time of pre-stellar cores. In the case of the formation of intermediate- and high-mass stars, using SPH simulations or tracer particles in grid simulations, it has been shown that the mass reservoir of sink particles extends far beyond the pre-stellar cores (Bonnell, Vine & Bate 2004; Smith, Longmore & Bonnell 2009b; Padoan et al. 2020). Both results seem to be at odds with the core-collapse idea.

Recent interferometric observations of regions of massive star formation have revealed a scarcity of massive pre-stellar cores that could serve as the mass reservoir for high-mass stars (e.g. Sanhueza et al. 2017, 2019; Kong 2019; Li et al. 2019; Pillai et al. 2019; Servajean et al. 2019), implying that such a mass
reservoir is spread over larger scales. This is also suggested by the
evidence of parsec-scale filamentary accretion on to massive
protostellar cores (e.g. Peretto et al. 2013), as well as in smaller
scale observations of a flow originating from outside the dense core
of a protostar (Pineda et al. 2020), which has also been seen in
simulations (Kuffmeier, Haugbølle & Nordlund 2017) and studied
in semi-analytical models (Dib et al. 2010). Chen et al. (2019) report
observations of non-gravitationally bound cores potentially formed
by pressure compression and turbulent processes, which by definition
involves accretion from outside of a gravitationally bound core.
Furthermore, while the pre-stellar CMFs in the Aquila and Orion
regions are found to peak at a mass a few times larger than that of
the stellar IMF, corresponding to a progenitor core efficiency \(\epsilon_{\text{prog}} \sim 0.2 \sim 0.4\) (André et al. 2010; Könyves et al. 2015, 2020), the peak
mass of the CMFs in Taurus and Ophiucus is very close to that of
the stellar IMF, or even smaller if candidate cores are included (Marsh
et al. 2016; Ladjevak et al. 2020). This would imply that \(\epsilon_{\text{prog}} \geq 1\) in Taurus and Ophiucus, contrary to the core-collapse scenario.
Protostellar jets and outflows remove a significant fraction of the
accreting mass (e.g. Matzner & McKee 2000; Tanaka, Tan & Zhang
2017), so a core-collapse model requires \(\epsilon_{\text{prog}} \leq 0.5\).

Some of the alternatives to the core-collapse models are the
competitive accretion model (e.g. Zinnecker 1982; Bonnell et al.
2001a, b; Bonnell & Bate 2006) and the inertial-inflow model
(Padoan et al. 2020). In the competitive accretion model, all stars
have initially low mass, and most of their final mass is accreted
after the initial collapse and may originate far away from the initial
core. The accretion is due to the stellar gravity, so the accretion
rate is expected to grow with the stellar mass. However, the Bondi-
Hoyle accretion rate in turbulent clouds is too low for this model
to explain the stellar IMF, unless the star-forming region has a
very low virial parameter, with a high density and comparatively
low-velocity dispersion (Krumholz, McKee & Klein 2005). Thus,
although this model is quite different from the core-collapse model,
it still requires that the feeding region of a star is gravitationally
bound and essentially in free-fall collapse.

In the inertial-inflow model (Padoan et al. 2020), stars are fed by
mass inflows that are not driven primarily by gravity, as they are an
intrinsic feature of supersonic turbulence. The scenario is inspired
by the IMF model of Padoan & Nordlund (2002), where pre-stellar
cores are formed by shocks in converging flows. The characteristic
time of the compression is the turnover time of the turbulence on a
given scale, which is generally larger than the free-fall time in the
post-shock gas, so a pre-stellar core may collapse into a protostar well
before the full stellar mass reservoir has reached the core (Padoan &
Nordlund 2011). After the initial collapse, the star can continue to
grow, as the converging flows that were feeding the pre-stellar core
continue to feed the star, through the mediation of a disc. Thus, the
stellar mass reservoir can extend over a turbulent and unbound region
much larger than the pre-stellar core. Because converging flows occur
spontaneously in supersonic turbulence and can assemble the stellar
mass without relying on a global collapse or on the gravity of the
growing star (Padoan et al. 2014, 2020), the inertial-inflow scenario
is fundamentally different from competitive-accretion.

\[\text{prog} \leq 0.5\text{ and approximately independent of mass},\]
To more realistically investigate the relation between the masses of stars and their progenitor cores we use one of the adaptive-mesh-refinement (AMR), magnetohydrodynamic (MHD) simulations of Haugbølle et al. (2018). While other simulations have reproduced the stellar IMF including different combinations of physical processes (see review by Lee et al. 2020), this was the first work to demonstrate that isothermal, supersonic, MHD turbulence alone can produce a numerically converged IMF. The high dynamic range, the inclusion of magnetic fields, a sub-grid model of the effects of outflows, and the long integration time overcome the limitations of previous studies, and result in a mass distribution of star particles that is consistent with the observed stellar IMF, from brown dwarfs to massive stars. By the end of this simulation, a large fraction of star particles has stopped accreting, so final masses are well defined. Stars stop accreting when their converging mass inflows are terminated, when pressure forces decouple the gas from the stars, or when they are dynamically ejected from multiple systems while still accreting.

The paper is structured as follows. Section 2 briefly summarizes the simulation and the numerical methods, and Section 3 describes the selection of bound progenitor cores around newly formed star particles from the simulation. Section 4 describes the physical properties of the progenitor cores, including their masses, sizes and sonic Mach numbers, and verifies that the progenitors are supercritical with respect to their magnetic support. The final star particle masses are compared with their progenitor core masses in Section 5, and tracer particles are used to identify the fractions of mass accreted from the progenitor and from farther away. The results are discussed in Section 6 in the context of the core-collapse model and the observations of the core mass function. Section 7 summarizes the conclusions.

2 SIMULATION

The simulation used in this study is the high reference simulation from Haugbølle et al. (2018; see their Table 1). Details of the numerical methods and the simulation set-up are in that paper, and are only briefly summarized in the following.

The MHD code used for the simulation is a version, developed in Copenhagen, of the public AMR code RAMSES (Teyssier 2007). It includes random turbulence driving and a robust algorithm for star particles. Periodic boundaries and an isothermal equation of state are adopted for the simulation. The grid refinement is based on overdensity, first at ten times the mean density and then at each factor of four in density. With a root grid of $256^3$ cells and six levels of refinement, the highest effective resolution is $16384^3$, corresponding to a smallest cell size of 50 AU for the assumed box size of 4 pc. The initial turbulent state is achieved by running the simulation without self-gravity for ~20 dynamical times, with a random solenoidal acceleration giving an rms sonic Mach number of approximately 10. Then self-gravity is switched on while maintaining the random driving, and the simulation is run for another ~2.6 Myr, with snapshots saved every 22 kyr.

The physical parameters of the simulation are as follows. The temperature is set at 10 K and the mean molecular weight $\mu = 2.37$, appropriate for cold molecular clouds, resulting in an isothermal sound speed of 0.18 $\text{km s}^{-1}$. Assuming a box size $L_{\text{box}} = 4$ pc, the total mass, mean density and mean magnetic field strength are $M_{\text{box}} = 3000 M_\odot$, $\bar{n} = 795 \text{ cm}^{-3}$, and $B_{\text{box}} = 7.2 \mu \text{G}$. The corresponding free-fall time and dynamical time are 1.18 Myr and 1.08 Myr, respectively.

At the end of the simulation, 413 star particles have been created, with a mass distribution consistent with the observed stellar IMF (Haugbølle et al. 2018). As discussed in Haugbølle et al. (2018) and further demonstrated in Appendix A, the peak of the IMF converges to a well-defined value. Star particles are created at a local gravitational potential minimum when the gas density in the cell is above a critical density, set at $1.7 \times 10^5 \text{ cm}^{-3}$. They are created without mass, but start accreting from their surroundings.

The mass-loss from winds and outflows and their feedback on the surrounding gas is not modelled in detail in the current simulation. However, the protostellar feedback processes are accounted for through an accretion efficiency factor, $\epsilon_{\text{acc}} = 0.5$, meaning that only half of the accreting mass is added to the stellar mass. This is consistent with the reduction in stellar masses found in the small-scale simulations by Federrath et al. (2014), where outflows are included. Their outflow subgrid model assigns 30 percent of the accreting mass to the outflows. In addition, the outflows disperse part of the surrounding gas, which further reduces the global star formation rate by another 20 percent. Thus, the inclusion of $\epsilon_{\text{acc}}$ in our simulation functions as a subgrid model for protostellar feedback that effectively includes both the direct mass-loss from the outflows and the reduction in the accretion rate due to the feedback on the surrounding gas.

Despite the 50 percent of the accreting mass being removed rather than launched back into the simulation in our subgrid model, the star formation time-scales are on average of the order of the observational estimates. As shown in Fig. 11 of Haugbølle et al. (2018), the stars in our simulation accrete 95 percent of their final mass in a time of $0.51(M_{\text{acc}}/M_\odot)^{0.58}$ Myr (the mean and median time, for all stars that have finished accreting by the end of the simulation, are 0.38 and 0.22 Myr, respectively), comparable to the observational value of $\sim 0.5$ Myr for the sum of the Class 0 and I phases (e.g. Enoch et al. 2009; Evans et al. 2009; Dunham et al. 2014). This agreement suggests that the main role of outflows is to reduce the accretion efficiency (as in our subgrid model) rather than shortening the star-formation time by halting the accretion completely.

We use $10^5$ tracer particles in the global simulation to trace the mass flow in the box. The tracer particles are passively advected with the fluid velocity. This may lead to a growing inaccuracy between the gas density field and the density field defined by the tracer particles (Genel et al. 2013). This is a secular effect that at the end of the simulation, after 2.6 Myr, may introduce a discrepancy between mass defined by tracers compared to defined by the gas mass of $\approx 10$ per cent on the scale of 1 $M_\odot$. We remedy this effect by redefining trace particle masses according to the density field, at the time of core selection, making the core masses defined by gas density or by tracers consistent. The typical mass accretion time-scale for a low-mass core is 100 kyr, and the difference between using the gas density field and passive tracers is below the per cent-level in the analysis below. Passive tracers are accreted probabilistically to star particles with a probability matching the fraction of gas accreted in the enclosing cells.

Fig. 1 shows a snapshot of column density of the whole simulation box. The three zoom-in regions show examples of 0.5 pc subcubes that are used in the detection of the progenitor cores (see Section 3.3), drawn in the same colour scale.

\footnote{The global reduction in the stellar masses in Federrath et al. (2014) is actually a factor of three, due to the increase in the number of stars when outflows are included. A similar reduction factor is obtained also with $\epsilon_{\text{acc}} = 0.5$ in our simulations (compared with equivalent runs where $\epsilon_{\text{acc}} = 1.0$), due to the reduced gravity of the sink particles.}
3 SELECTION OF PROGENITOR CORES

3.1 Clumpfind algorithm

Cores are selected from the simulation with the clumpfind algorithm introduced in Padoan et al. (2007), updated in this work to consider both thermal and kinetic energies. In the clumpfind algorithm, cores are defined as ‘gravitationally unstable connected overdensities that cannot be split into two or more overdensities of amplitude $\delta n/n > f$, all of which remain unstable’. Cores are considered unstable if their gravitational binding energy is larger than the sum of their kinetic and thermal energies (see Section 3.2 for details). The algorithm scans the density field with discrete density levels, each of amplitude $f$ relative to the previous one. Only the connected regions above each density level that are found to be unstable are retained. After this selection, the unstable cores from all levels form a hierarchy tree. Only the final (unsplit) core of each branch is retained. Each core is assigned only the mass within the density isosurface that defines the core (below that density level the core would be merged with its next neighbour). This algorithm is different from the construction of a dendrogram (Rosolowsky et al. 2008), where a hierarchy tree of cores is first computed irrespective of the cores energy ratios, and unstable cores are later identified among the leaves of the dendrogram. In our algorithm, the condition for instability is imposed while building the tree, otherwise some large unstable cores would be incorrectly eliminated if they were split into smaller cores that were later rejected by being stable.

Once the physical size and mean density of the system are chosen, the clumpfind algorithm depends only on three parameters: (1) the spacing of the discrete density levels, $f$, (2) the minimum density above which cores are selected, $n_{\text{min}}$, and (3) the minimum number of cells per core. In principle, there is no need to define a minimum density, but in practice it speeds up the algorithm. The parameter $f$ may be chosen according to a physical model providing the value of the smallest density fluctuation that could collapse separately from its contracting background. In practice, the $f$ parameter is set by looking for numerical convergence of the mass distribution with decreasing values of $f$. The minimum number of cells is set to 4, to ensure that all the detected cores are at least minimally resolved in the simulation.

3.2 Stability condition

In the clumpfind algorithm, the absolute value of the gravitational binding energy is given by the formula for a uniform sphere:

$$E_g = \frac{3GM_{\text{prog}}^2}{5R_{\text{prog}}},$$

where $G$ is the gravitational constant, $M_{\text{prog}}$ is the mass of the core, and $R_{\text{prog}}$ is the radius of a sphere of an equivalent volume to that of the core. This proved to be a good approximation for the gravitational binding energy for the cores that we find, when compared to a pairwise calculation of the potential energy between the cells of the core.

The kinetic energy is given by

$$E_k = \sum_{i=1}^{N} \frac{1}{2} m_i(v_i - \bar{v})^2,$$

where $N$ is the number of cells in the core, $m_i$ and $v_i$ are the mass and the velocity of each cell, and $\bar{v}$ is the mass-weighted mean velocity of the core. The thermal energy is given by the formula for an ideal diatomic gas:

$$E_t = \frac{5}{2} N k T,$$

where $N$ is the number of hydrogen molecules, $k$ is the Boltzmann constant, and $T$ is the temperature, set to 10K. The condition that
cores are unstable is then based on the energy ratio,

\[
\frac{E_k + E_i}{E_g} \leq 1. \tag{4}
\]

The condition should be \((E_k + E_i)/E_g \leq 1/2\), based on the virial theorem, if surface terms were included. Our choice implicitly assumes a Bonnor-Ebert model including surface terms of the order of half the internal energy. To test this approximation, we have calculated the surface terms (see Appendix B). The median ratio of the surface terms divided by the internal energy is about 0.5. Thus, our \(\alpha_{\text{vir}} = 1\) without surface terms is on average equal to \(\alpha_{\text{vir}} = 0.5\) with surface terms accounted for, as in the virial theorem. Smith et al. (2009a) and Gong & Ostriker (2015) use the same condition as in equation (4) to select unstable cores in their simulations.

3.3 Selection set-up

We extract 1,024 3 subcubes of 0.5 pc in size centred on each star particle, in the snapshot where the star particle first appears. This resolution corresponds to 81923 resolution for the full 4 pc simulation box and a physical scale of 100 AU per cell. As found previously by e.g. Hennebelle (2018), the numerical resolution can have a large effect on the masses of the selected cores; lower resolutions can result in higher core masses as well as increase the number of cores with multiple stars inside them.

Nevertheless, given our large underlying resolution, on top of which we only vary the resolution of the clumpfind algorithm, the peak of the CMF changes much less than in e.g. Hennebelle (2018), and the peak converges towards a definite value as the resolution increases (see Appendix C). The parameters of the clumpfind algorithm and the effect of numerical resolution are discussed in Appendix C.

The clumpfind algorithm should in principle be applied to the whole periodic box, as the cores could depend on how neighbouring cores are selected, but this would be computationally infeasible at the highest resolution. However, most of the cores are well-defined within a 0.5 pc subcube. Due to their large size, for 22 cores with masses higher than 5 M⊙ in the 0.5 pc subcube, we repeat the clumpfind search using 1 pc subcubes.

Ideally, we would use a snapshot at a time immediately before the central star is created. In the absence of such a snapshot, and in the spirit of characterizing the core condition at the time immediately before the star formation, we add twice the initial mass of the central star particle (\(M_{\text{init}}/\epsilon_{\text{acc}}\)) to the density cube to account for the gravitational energy of the gas that has already been accreted on to or ejected by the central star particle between the time of its formation and the time of the detection snapshot. The mass of other stars present in the subcube is also added to the density cube, using a factor of 2 if they formed in the same snapshot as the central star or a factor of 1 if they had formed in a previous snapshot (we assume that the jet would have time to disperse the \(\epsilon_{\text{acc}}\) fraction of the accreted mass away from the core in that case). The mass is added into the cell where each star is located. The details of how the mass is added do not affect the calculation of the gravitational binding energy, as only the total mass is needed in the uniform sphere approximation of equation (1). Additionally, this method ensures that, if there is no extended material around the star, the single cell ‘core’ is not picked up, because the minimum number of cells per core is set to 4.

For the overdensity amplitude, \(f\), we adopt a conservative value, \(f = 2\) per cent. Given that the 0.5 pc subcubes are in overdense regions of the full box, we select the minimum number density level to be \(n_{\text{min}} = 10^5 \bar{n} = 7950\) cm\(^{-3}\). We have varied \(f\) and \(n_{\text{min}}\) using \(f = 8\) per cent and \(n_{\text{min}} = 2 \bar{n}\) and verified it resulted in almost identical core masses.

The clumpfind algorithm is run for each subcube, to find all the unstable cores. Then a search is made for the core that contains the star particle (in the central cell of the subcube). This core is labelled as the progenitor core for that star particle. If no core containing the central cell is found, we search for the closest core inside a 213 cube around the star, and record the distance to the star if a core is found. Otherwise, the distance is set to a high number to indicate that no match is found.

4 PROGENITOR CORES

The clumpfind algorithm outputs a list of cell indices that are part of each core, as well as the masses of the cores. Once the progenitor cores are identified, their cell indices are used to find any other star particles within the progenitor. As explained in Section 3.3, we include twice the masses of the star particles that formed in the same snapshot as the primary star into the density cube, whereas older star particles were already considered to be stars.

Out of a total of 413 star particles in the simulation, we are able to match 382 unambiguously with a progenitor core. Among the other 31 stars, pre-dominantly of low mass, 22 of them are found within 1000 AU of a core and 9 are more distant. Some of these stars are brown dwarfs that have collapsed quickly from a small core and have already accreted their parent core by the time of the snapshot we analyse. Others are stars that have already decoupled from the accreting gas due to pressure forces acting on the gas or dynamical encounters with other stars. A small fraction of them may be numerical artefacts, as discussed in Haugbølle et al. (2018). We may exclude those 31 stars from the analysis.

We further divide our 382 unambiguously matched progenitors in three categories based on the stars within the progenitor: (1) a single star (the primary one, 312 cores); (2) multiple stars, but all formed in the same snapshot (32 cores); (3) one or more older stars in addition to the primary one (38 cores). The older stars may dominate the mass reservoir inside the core. To be conservative, we exclude category three from the analysis.

The final sample used in the paper is therefore 344 stars with an unambiguous progenitor detection and no older stars inside the progenitor core.

To study the mass distribution of the accreted gas (see Section 5), we extract the passive tracer particles that are within a progenitor core at the time of its identification. These tracer particles are used to calculate the fractions of the progenitor mass accreted by the primary star \(f_{\text{tr, prog}}\), accreted by any other stars \(f_{\text{tr, other}}\), and not accreted by any star \(f_{\text{tr, unacc}}\) at the end of the simulation. \(f_{\text{tr, prog}}\) is defined as \(M_{\text{tr, prog}}/M_{\text{prog}}\), where \(M_{\text{tr, prog}}\) is the mass of all the tracers inside the progenitor that will be accreted by the primary star. The mass fraction going to other stars is simply defined as tracer particles that will be accreted by any other stars by the end of the simulation; these other stars do not need to form at the same time or become binaries, and most often do not. Progenitors that do form multiple stars in the same snapshot are flagged as such, as explained in the previous paragraph. Furthermore, we calculate the fraction of the final stellar mass contained within the progenitor core: \(f_{\text{st, star}} = \epsilon_{\text{acc}} f_{\text{tr, prog}} M_{\text{prog}}/M_{\text{star}}\). Here, the efficiency factor \(\epsilon_{\text{acc}}\) is already included in the final stellar mass, \(M_{\text{star}}\), and thus needs to be applied for the tracer mass as well. These fractions evolve while the stars accrete their mass, and some of them have not stopped accreting yet. Thus, we further check if the stars have stopped accreting at the end of the simulation by computing the final accretion rate as the mass
increase between the last two snapshots, divided by the time interval between the snapshots. This is an accretion rate averaged over 22 kyr. If the stars need 10 Myr or longer to double their final mass given that accretion rate, we consider them as having finished accreting (242 stars out of 344). Finally, to characterize the size of the region from which a star accretes its mass, we calculate the inflow radius, $R_{\text{infl}}$, as was done in Padoan et al. (2020). $R_{\text{infl}}$ is defined as the radius of the sphere that contains 95 per cent of the tracer particles’ mass accreted by the star by the end of the simulation. We refer to it as the inflow radius in reference to our scenario where growing stars are fed by inertial inflows, as extensively demonstrated in Padoan et al. (2020).

The mass fractions and the inflow radius defined through the tracer particles are used in Section 5, where we address the relationship between the stars and their progenitor cores.

Since the clumpfind algorithm does not consider the magnetic field, we check for magnetic support against gravitational collapse after the fact. We follow the same methodology as in Ntormousi & Hennebelle (2019). We calculate the magnetic critical mass (Mouschovias & Spitzer 1976),

$$M_{c\phi} = \frac{c_1}{3\pi} \left( \frac{5}{G} \right)^{2/3} \phi$$

where $c_1 = 1$ for a uniform sphere, $G$ is the gravitational constant, and $\phi$ is the magnetic flux.

We measure $\phi$ for each core by selecting three planes going through the core centre perpendicular to each axis. We then flag the cells belonging to the core, and sum the flux along the perpendicular axis over all the cells. We then select the highest of the three fluxes to calculate the magnetic critical mass. The mass-to-flux ratio, normalized by the magnetic critical mass, is then simply given by:

$$\mu = \frac{M_{\text{prog}}}{M_{c\phi}}$$

where $M_{\text{prog}}$ is the mass of the core and $M_{c\phi}$ is the magnetic critical mass, assuming a uniform sphere. Fig. 2 shows the normalized mass-to-flux ratio, $\mu$, as a function of core mass, $M_{\text{prog}}$. We find that all of our unstable cores are supercritical, which is to be expected, as we selected for unstable cores associated with recently formed star particles.

To further describe the sample of progenitor cores, Fig. 3 shows their size (upper panel) and their rms sonic Mach number (lower panel) as a function of their mass (blue dots). Although we make no attempt to retrieve observational properties of the cores through synthetic observations, it is still instructive to compare these quantities with some observational values. For that purpose, Fig. 3 also shows values of sizes, rms Mach numbers and masses of pre-stellar cores from a number of large observational surveys.

The cores from the simulation are studied at the time when they have just started to collapse in order to identify the maximum value of their mass in the pre-stellar phase. Thus, our cores are in the transition from pre-stellar to protostellar, and they could also be compared with very young protostellar cores whose central star is still a small fraction of the core mass. For simplicity, we consider only observed cores in the pre-stellar phase.

The gravitational stability of cores is often defined by reference to a critical Bonnor-Ebert sphere. The critical radius, $R_{\text{BE}}$, of a Bonnor-Ebert sphere with a temperature of 10 K is given by $R_{\text{BE}} = M_{\text{BE}}/20.2$, where $M_{\text{BE}}$ is the mass of the sphere in $M_{\odot}$, and the radius is in parsecs. This expression for the critical radius as a function of the
mass is shown by the red dashed line in the upper panel of Fig. 3. The progenitor cores from our simulation span a range of values between approximately 100 AU and 0.2 pc, with a median value of approximately 800 AU. They are all well below the critical Bonnor-Ebert radius, because they are selected as gravitationally unstable cores accounting also for their internal kinetic energy, as shown in equation (4).

For comparison, we show the observational values of the pre-stellar cores in Aquila from the Herschel Gould Belt Survey (Könönen et al. 2015), in Orion from a subsample of a SCUBA survey that includes follow-up line observations (Kirk et al. 2017; NH\textsubscript{i} observations from Friesen et al. 2017), in a number of infrared dark clouds from a large ALMA survey (Sanhueza et al. 2019), and in another set of infrared dark clouds observed with ALMA where core velocity dispersions are also published (Ohashi et al. 2016). There is a significant overlap between the observed pre-stellar cores and the cores from our simulation, except that core sizes below 1000 AU are missing in the observational samples, due to their spatial-resolution limit. Furthermore, the observed core masses at any given radius tend to extend to larger values than in our sample, probably also as an effect of the limited spatial resolution (see discussion in section 9.2 of Padoan et al. 2020). Finally, for the Aquila and Orion cores we have selected all pre-stellar cores with a radius smaller than or equal to the critical Bonnor-Ebert radius for their mass, which explains the large number of cores near the critical radius line. Although such cores, and even those with half a critical Bonnor-Ebert mass, are usually considered pre-stellar cores in dust-continuum studies, a fraction of them are probably not gravitationally bound, due to their internal kinetic energy.

To illustrate the importance of internal motions in the progenitor cores, the lower panel of Fig. 3 shows the one-dimensional velocity dispersion inside the cores, \(\sigma_v\), in units of the isothermal speed of sound for a temperature of 10 K, \(c_s \approx 0.18 \text{ km s}^{-1}\), as a function of the core mass, \(M_{\text{prog}}\). In the case of the observational samples, the sound speed value estimated in the corresponding papers is adopted. Most of the progenitor cores (blue dots) are within a factor of two from the equipartition between kinetic and thermal energy, marked by the horizontal dashed line. They show a trend of increasing rms Mach number with increasing core mass, and some of the least massive cores have an rms Mach number several times smaller than the value corresponding to the energy equipartition, or velocity dispersions as low as 1/5 of the sound speed.

Apart from the pre-stellar cores in Orion and in the infrared dark clouds already shown in the upper panel of Fig. 3, we consider also the velocity dispersion of pre-stellar cores in Perseus from Kirk, Johnstone & Tafalla (2007). The observed values overlap with those of the progenitor cores from our simulation. However, in the range of core masses between approximately 1 and 10 \(M_\odot\), the observed cores extend to lower Mach number values than our progenitor cores. This partial discrepancy may have two origins. First, as mentioned above, and extensively documented in Section 9.2 of Padoan et al. (2020), a significant overlap between the observed pre-stellar cores and the cores from our simulation is shown to illustrate that the values of the physical parameters of the cores from our simulation are reasonable, which does not require that such values cover the full range of parameter space from the observations. All the physical parameters of the progenitor cores used in this study are listed in Table 1. The Table, as well as other supplemental material, can also be obtained from a dedicated public URL (http://www.erda.dk/vgrid/core-mass-function/).

5 PROGENITOR MASSES VERSUS STELLAR MASSES

5.1 Statistical comparison

The main goal of this work is to test the hypothesis of the core-collapse model, which we express as \(M_{\text{star}} \approx \epsilon_{\text{prog}} M_{\text{prog}}\), with \(\epsilon_{\text{prog}} \approx 0.5\) and approximately independent of mass, using previously defined quantities. Before comparing cores and stars one-to-one, a look at their mass distribution is already instructive. Fig. 4 shows the mass distribution of the progenitors selected at the star-formation snapshots and that of the stars at the end of the simulation. Only the 344 pre-stellar progenitors, those without older star particles in them (see Section 4), are included in the figure. Both the progenitor CMF and the IMF distribution peak at \(\approx 0.3 M_\odot\). Our resolution convergence test in Appendix C indicates that the mass peak of the CMF converges towards a well-defined value \(M_{\text{conv}} \approx 0.26 M_\odot\), almost identical to the value of the IMF peak. This is problematic for the core-collapse model, as it would imply \(\epsilon_{\text{prog}} \approx 1\).

The similarity of the mass distributions continues to the high-mass tail, as well. However, this should not be taken to mean that the high-mass progenitors are undergoing a monolithic collapse. In order to show this, we used the tracer particles (see Section 4) to study how the gas from the progenitor core is either accreted by the primary star (\(f_{\text{acc}, \text{prog}}\)), by other stars (\(f_{\text{acc}, \text{other}}\)), or remains unaccreted (\(f_{\text{acc}, \text{unacc}}\)). These mass fractions, defined in Section 4, are shown in Fig. 5 as a bar chart for the 16 cores with masses larger than \(5 M_\odot\), where the x-axis is ordered by growing progenitor mass. The mass fractions for two high-mass cores, 7.5 and 88 \(M_\odot\), are not shown as they are identified less than 100 kyr before the end of the simulation, and most of their mass is unaccreted. The bar charts show that in the majority of the massive progenitors, the primary fractions...
Table 1. Stellar and progenitor parameters for a set of 10 stars and their progenitors. The full table is included as an electronic download. The columns are: 1 star index, 2 snapshot number when the new star was recorded, 3 final mass of the star, 4 mass of the progenitor, 5 radius of the progenitor (as an equivalent volume sphere), 6 radius within which the star accretes 95% of its mass, 7 one-dimensional sonic Mach number, 8 kinetic-to-gravitational energy ratio, 9 thermal-to-gravitational energy ratio, 10 inverse of normalized mass-to-flux ratio, 11 final accretion rate as a fraction of the final stellar mass, 12 fraction of progenitor mass which is accreted by other stars, 13 fraction of progenitor mass which is accreted by the star itself, 14 fraction of final stellar mass already present in the progenitor, and 15 flag for the state of the progenitor (1 for single star, 2 for multiple stars born at the same time). The fraction of progenitor mass which remains unaccreted by any star can be derived from $f_{\text{unacc}} = 1 - (f_{\text{other}} + f_{\text{prog}})$.

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<th>$M_{\text{prog}}$ [M$_{\odot}$]</th>
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<th>$R_{0.5}$ [AU]</th>
<th>$\sigma \sqrt{c_s}$</th>
<th>$E_k/E_g$</th>
<th>$E_{t}/E_g$</th>
<th>$t/\mu$</th>
<th>$M/M_{\text{star}}$ [Myr$^{-1}$]</th>
<th>$f_{\text{other}}$ [per cent]</th>
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The result is also illustrated by the fact that the massive cores show a lot of internal structure, and their time evolution always results in their fragmentation. This is exemplified for star 391 in Fig. 6, where the lower panel shows that another star has formed 66 kyr later and the bound core around star 391 has shrunk to a mere 0.02 M$_{\odot}$ protostellar envelope (the protostar itself is 0.14 M$_{\odot}$). The vast majority of the gas in its 88 M$_{\odot}$ progenitor core is no longer bound to star 391. Even accounting for the protostellar mass, the bound core around star 391 is not even the locally dominant core, as the mass of the progenitor core of star 405 is 1.1 M$_{\odot}$.

Thus, the statistical similarity between the high-mass tails of the CMF and the stellar IMF does not imply a monolithic collapse of the massive cores as further discussed in the next subsection.

Figure 4. Histogram of pre-stellar progenitor masses (blue, 344 cores) and the final masses of the stars born in them (red, 344 stars), with bin sizes 0.34 and 0.30 dex, respectively. Dashed lines are lognormal fits ($N \propto \exp(-\log_{10}M - \log_{10}M_{\text{peak}})^2/2\sigma^2)$ to masses lower than 2M$_{\odot}$ (CMF: $M_{\text{peak}} = 0.29$ M$_{\odot}$, $\sigma = 0.40$; IMF: $M_{\text{peak}} = 0.29$ M$_{\odot}$, $\sigma = 0.63$) and the red dotted line is a power-law fit ($N \propto M^{-1.2}$) to stellar masses above 2M$_{\odot}$ with $\Gamma = 1.20$.

Figure 5. Bar chart of the fractions where the progenitor mass goes, for progenitors with $M_{\text{prog}} > 5$M$_{\odot}$ (the most massive cores in our sample). The total mass of the progenitor is stated on the x-axis, and the fractions are unaccreted mass ($f_{\text{unacc}}$, black), mass accreted by other stars ($f_{\text{other}}$, red), and mass accreted by the star whose progenitor the core is ($f_{\text{prog}}$, blue). Two high-mass cores, 7.5 and 88 M$_{\odot}$, are not shown as they are identified less than 100 kyr before the end of the simulation.

5.2 One-to-one comparison

The one-to-one relation between progenitor masses and final stellar masses is addressed by the scatter plots in Fig. 7. The figure shows that, for a given core mass, there is a scatter of about two orders of magnitude in the resulting stellar masses (Pearson’s correlation coefficient, $r$, is 0.51 for all stars). The top panel of Fig. 7 distinguishes the stars that have finished accreting (magenta open circles). Limiting the sample to these stars does not make the correlation significantly stronger ($r = 0.57$). The correlation is even worse at lower resolution (see Appendix C).

The relatively weak correlation between core and stellar masses is in conflict with the core-collapse model, because it shows that even if we know the mass of the progenitor core at the birth time of the star, we cannot predict the final stellar mass with any reasonable accuracy.
Figure 6. Upper panel: Column density map of the progenitor core of star 391, seen from the x-direction. Cyan contours are drawn where there is at least one cell belonging to the progenitor core on the line of sight. The star being formed is in the middle (white circle and number), but it is clear that there are other nodes forming in this high-mass ($88 \, M_\odot$) core, too. The white dashed box shows the approximate location of the lower panel. Lower panel: As above, but for star 405, 66 kyr (3 snapshots) later. The density structure around star 391 is clearly identifiable, but the bound core around it is just a protostellar envelope with only $0.02 \, M_\odot$ (the protostar itself is $0.14 \, M_\odot$ at this time). The progenitor core associated with star 405 is $1.1 \, M_\odot$.

Furthermore, a least-squares fit to the data points gives a slope of $a = 0.52$ for all stars (blue line), and $a = 0.60$ for the stars that have finished accreting (magenta dashed line). This shows that the average relation between core and stellar masses is inconsistent with the idea of a constant efficiency factor, $\epsilon_{\text{prog}}$, as a constant efficiency would imply a slope $a = 1$ (red solid line in Fig. 7).

Some of the high-mass progenitors can be expected to fragment and contribute to several stars, as already mentioned in Section 5.1. In the bottom panel of Fig. 7 we distinguish between stars that formed alone or accompanied by other stars. Progenitors with multiple stars have an elevated progenitor mass on average at lower stellar masses. This is easily understood, as those progenitors are feeding two or more stars, while at higher masses, the progenitor alone is not enough for those massive stars to grow. If the star is the first one to form inside the core, even if it appears later in another progenitor, it is still counted as single (when we check for stars that appear later in other progenitors, we do not find a clear correlation with their own progenitor masses, so this does not bias the result). For single stars, the Pearson’s correlation coefficient and the slope are $r = 0.53$ and $a = 0.53$, comparable to that of all the stars that have finished accreting. In the case of the stars that grow beyond their progenitor core mass, more mass needs to come in from outside the progenitor.
Converging flows may continue feeding mass into the core from beyond its gravitationally bound limit, allowing the star to accrete much more mass than what was initially available from the core. This is the case in particular with high-mass stars, as further documented in the following, using tracer particles.

Fig. 8 shows the histograms of mass ratios, $f_{\text{tr, prog}}$ (solid lines) and $f_{\text{tr, star}}$ (dashed lines). The first fraction, $f_{\text{tr, prog}}$ is the fraction of the progenitor mass that is accreted on to the star (solid lines), and stellar mass fraction, $f_{\text{tr, star}}$, that is the fraction of the stellar mass that came from the progenitor (dashed lines). The dashed lines have been shifted down by a factor of 0.10, to avoid confusion with the solid lines. The blue lines are for all stars, while magenta lines are for the stars that have effectively finished accreting. Vertical lines mark the median value for each sample. Black (high-mass star) and red (low-mass star) dots show the fractions for the example progenitor cores in Fig. 9.

Figure 8. Histograms of progenitor mass fraction, $f_{\text{tr, prog}}$, that is the fraction of the progenitor mass that is accreted on the star (solid lines), and stellar mass fraction, $f_{\text{tr, star}}$, that is the fraction of the stellar mass that came from the progenitor (dashed lines). The dashed lines have been shifted down by a factor of 0.10, to avoid confusion with the solid lines. The blue lines are for all stars, while magenta lines are for the stars that have effectively finished accreting. Vertical lines mark the median value for each sample. Black (high-mass star) and red (low-mass star) dots show the fractions for the example progenitor cores in Fig. 9.

Figure 9. Examples of progenitor cores that will form a high-mass star, $M_{\text{star}} = 28 M_\odot$ (upper panels), and a low-mass star, $M_{\text{star}} = 0.21 M_\odot$ (lower panels), visualized through their tracer particles. Left panels: The 0.25 pc (top) and 0.01 pc (bottom) central regions of the 0.5 pc subcubes where the two cores were selected. Red dots are tracers that will accrete on to the star, blue dots are the remaining tracers of the cores. Right panels: The whole 4 pc simulation box (top), and a 0.5 pc subcube (bottom) centred around the same star and at the same (star-formation) snapshot as the left panels. The red dots are the locations of all the tracers that will accrete on to the stars by the end of the simulation. A significant fraction, $\sim 90$ per cent (top) and $\sim 60$ per cent (bottom), of the final stellar mass is found outside the progenitor core.

from fig. 23 of Padoan et al. (2020), where it was obtained as a fit to the inflow radius of the stars with the highest accretion rate and was shown to be a good approximation to the lower envelope of the $R_{95}$ versus $M_{\text{star}}$ plot. In Padoan et al. (2020) that plot covered stellar masses above 2–3 $M_\odot$. Here, the same function is found to be a good approximation to the lower envelope of the plot for all stellar masses, down to brown dwarfs.

The inset in the lower panel shows the ratio of $R_{95}/R_{\text{prog}}$ as a function of the final stellar mass for stars that have already finished accreting, with the dashed red line indicating a ratio of unity. The scatter plot covers rather uniformly a range of values of $R_{95}/R_{\text{prog}}$ between approximately 1 and $10^3$, with a median of 14. There is no correlation between the ratio and the final stellar mass, which indicates that even lower-mass stars are influenced by proportionally as large a region around them as the more massive stars. Of the five lowest ratio cases (with a ratio $< 1$), four are massive progenitors ($M_{\text{prog}} > 7 M_\odot$) that later undergo sub-fragmentation to form relatively low-mass stars (0.3, 0.4, 0.7 and 1.7 $M_\odot$), and the remaining one is a low-mass progenitor ($M_{\text{prog}} = 0.3 M_\odot$) that results in the formation of a brown dwarf (0.05 $M_\odot$).

Fig. 11 shows the progenitor mass fraction, $f_{\text{tr, prog}}$, and the stellar mass fraction, $f_{\text{tr, star}}$, in a scatter plot. The ratio of the stellar mass and the progenitor mass is $M_{\text{star}}/M_{\text{prog}} \approx f_{\text{tr, prog}}/f_{\text{tr, star}}$, so the core-collapse model may appear to be satisfied along the diagonal of Fig. 11, where $f_{\text{tr, prog}} = f_{\text{tr, star}}$, or, equivalently, the red line in Fig. 7. However, for many stars where $M_{\text{star}} \sim \epsilon_{\text{prog}} M_{\text{prog}}$, this agreement is only due to the fact that both $f_{\text{tr, prog}}$ and $f_{\text{tr, star}}$ are $< 1$, so both mass fractions actually violate the physical assumption of the core-collapse model (although
not its mathematical expression based only on $M_{\text{star}}$ and $M_{\text{prog}}$. In other words, the core-collapse model is truly satisfied, within an error of a factor of two, only in the upper right quadrant of the scatter plot in Fig. 11. Only $\sim 35$ per cent of the 344 star-progenitor pairs are in the upper right quadrant, where both $f_{\text{tr, prog}}$ and $f_{\text{tr, star}}$ are higher than 0.5. Thus, from the perspective of the tracer particles, the one-to-one relation between core and stellar masses assumed by the core-collapse model would be correct within a factor of two for only a minority of the cores.

6 DISCUSSION

6.1 The core-collapse model

We have compared the final stellar masses with those of their pre-stellar cores. Accurate predictions of both masses are difficult to obtain, due to the complexity of the star-formation process. However, we argue that uncertainties related to such mass determinations are not critical to our approach to test the core-collapse model and do not affect our conclusions. The mass of a star at the end of the simulation is a good approximation to the final stellar mass, particularly for the stars that were tagged as finished accreting. Because the simulation does not resolve jets and outflows, only half of the accreting mass is assigned to the star particle, a typical value found in theoretical models (e.g. Matzner & McKee 2000). This simple approach to modelling the mass loss from protostellar jets and outflows introduces some uncertainty in the final stellar mass. However, this uncertainty does not affect the fundamental question addressed here, which is the origin of the stellar mass reservoir, irrespective of how much of that may get ejected during its formation.

The estimation of the pre-stellar core mass is particularly difficult, because they arise within dense filaments as a result of converging flows in the turbulent gas, so they rarely appear as isolated objects with simple morphology. Furthermore, a comparison of pre-stellar core masses from a simulation with those from observations would have to address a number of observational limitations that are briefly mentioned in Section 6.3. This would require an analysis of the simulation based on synthetic observations, and a method of core selection following the observational procedures. We have not attempted that, as our main focus is to test a theoretical idea. In the theoretical models, the stellar progenitors are well-defined entities. In the IMF models of Hennebelle & Chabrier (2008) and Hopkins (2012) the stellar-mass reservoir is a gravitationally bound, overdense region in the turbulent flow, consistent with the core-collapse scenario. Such mass reservoir may not correspond precisely to what the observers identify as pre-stellar cores (e.g. it may have to contract somewhat before reaching a characteristic core density), or with analytical models of isolated cores (e.g. McKee & Tan 2002, 2003), as it is selected through a statistical description of a complex turbulent flow. However, that complexity is fully accounted for in our simulation, and our progenitor cores are defined as bound regions, as in the models. So the progenitor masses we derive are relevant for...
testing the IMF models based on the idea of core-collapse, and our approach is not affected by the uncertainties related to a comparison with the observations.

We have found (1) a poor correlation between progenitor and stellar masses, (2) a mean dependence of stellar mass on core mass with a slope significantly shallower than unity, (3) a stellar mass reservoir that extends well beyond the limits of the gravitationally bound pre-stellar core. These results are inconsistent with the main hypothesis of the core-collapse model, which is $M_{\text{star}} \approx \epsilon_{\text{prog}} M_{\text{prog}}$ (with $\epsilon_{\text{prog}} \approx 0.5$ and approximately independent of mass) for the simulation. Because most of the stellar mass comes from a larger and unbound region, rather than from a gravitationally bound reservoir, the fundamental assumption of the IMF models of Hennebelle & Chabrier (2008) and Hopkins (2012) and their further developments (e.g. Hennebelle & Chabrier 2009; Hopkins 2013) is incorrect, and an understanding of the IMF based on those models is incomplete at best.

A similar conclusion was reached in Padoan et al. (2020), based on a star-formation simulation of a 250 pc region of the interstellar medium, driven by supernovae. However, in that work only high-mass stars are resolved, so the core-collapse model, as well as the competitive-accretion model, is ruled out only for the origin of massive stars. Here, instead, we show for the first time that the lack of correlation between core and stellar masses applies to the whole IMF, although it may be more extreme for the most massive stars. To further confirm this, we show in Fig. 12 a scatter plot of the stellar mass fraction, $f_{\text{star}}$, as a function of the final stellar mass, $M_{\text{star}}$. The plot shows that the stellar mass fraction that comes from the progenitor has a rather uniform distribution between approximately 0.05 and 1, irrespective of $M_{\text{star}}$. There is only a slight trend with mass. Even at the IMF peak, $\sim 0.2M_\odot$, there are stars with values as low as $f_{\text{star}} = 0.1$. For low-mass stars ($M_{\text{star}} < 2M_\odot$) with $f_{\text{star,prog}} > 0.5$, we find that the median value of $f_{\text{star}}$ is 0.48 (172 stars).

For intermediate-mass stars ($2-5M_\odot$), the median value of $f_{\text{star}}$ is only 0.14 (13 stars). Thus, the main assumption of the core-collapse model is clearly violated for a majority of stars at all masses, not only for the most massive stars.

### 6.2 Competitive accretion

Although we find that a significant fraction of the stellar mass comes from outside of the progenitor cores, our simulation rules out also the competitive-accretion model (Zinnecker 1982; Bonnell et al. 2001a, b). According to competitive accretion, the accretion rate of a star should increase with its mass as $M \propto M^{2/3}$ in the case of gas-dominated potentials, or $M \propto M^{2}$, in the case of stellar-dominated potentials (e.g. Bonnell et al. 2001a, b). Previous works that claimed to support competitive accretion, only showed scatter plots of accretion rate versus sink mass at a fixed time (Maschberger et al. 2014; Ballesteros-Paredes et al. 2015; Kuznetsova et al. 2018), but no evidence that the accretion rate of a given star grows over time as the mass of that star increases. The time evolution of the accretion rates in our simulation is shown by the solid lines in Fig. 13. After computing the time evolution of $M$ and $\dot{M}$ for every star, the profiles of $\dot{M}$ versus $\epsilon\dot{M}_{\text{star}}$ (the stellar mass in units of its final value) are stacked together to obtain an average profile. This is done separately for stars with $M_{\text{star}} \leq 1M_\odot$ (bright blue line) and $M_{\text{star}} > 1M_\odot$ (bright red line). The accretion rate is relative constant as the stellar mass increases, for $M_{\text{star}} > 1M_\odot$, or decreases with increasing mass for $M_{\text{star}} \leq 1M_\odot$, in contrast with the prediction of competitive accretion. This confirms our earlier results in Padoan et al. (2014, 2020).

The average profiles in Fig. 13 appear to be relatively smooth, which is suggestive of analytical models of the collapse of an isothermal sphere (Shu 1977; Dunham et al. 2014). However, the profiles of individual stars (see the two examples shown by the faint blue and red lines in Fig 13) are much more irregular than the average ones, exhibiting fluctuations of one order of magnitude or larger that are inconsistent with the analytical collapse models. This is to be expected, because a significant fraction of the stellar mass originates well outside of the progenitor core. We have verified that only the mass that is initially found in the progenitor core is accreted in a way consistent with the collapse of an isothermal sphere, meaning with an accretion rate profile that is very smooth, relatively constant in time and approximately independent of the final stellar mass.

To further illustrate the departure from competitive accretion, we also estimate the Bondi-Hoyle accretion rate (Bondi & Hoyle 1944; Bonnell et al. 2001a), $\dot{M}_{\text{BH}}$, using the current mass of the star, $M$, and the rms velocity, $v_{\text{rms}}$, and the mean gas density, $\rho_{\text{gas}}$, within the $R_{\text{BH}}$ sphere of each sink particle at birth (the sphere with radius equal to $R_{\text{BH}}$ and centred at the sink-particle position at birth): $\dot{M}_{\text{BH}} = \epsilon_{\text{acc}}\pi G^2 M^2 \rho_{\text{gas}}(\epsilon_{\text{f}}^2 + v_{\text{rms}}^2)^{3/2}$. This is just an order-of-magnitude estimate, as we account for the increase of the stellar mass over...
predicted Bondi-Hoyle accretion rates are on average a couple of same stacking procedure for the two groups of stars as before. The accretion rate, because time. It is generally a conservative overestimate of the Bondi-Hoyle accretion rates. The predicted Bondi-Hoyle accretion rates, $\dot{\text{M}}$, are stacked in the same way, with dashed lines representing the median values, and dotted lines the mean values (see the text for the method of computing $\dot{\text{M}}_{\text{BH}}$).

time, while the gas properties in the $R_{95}$ spheres are not varied with time. It is generally a conservative overestimate of the Bondi-Hoyle accretion rate, because $v_{95}$ is adopted as an estimate of the relative velocity between the star and the gas, without including the difference between the mean gas velocity in the $R_{95}$ sphere and the velocity of the star. The estimated rates are shown in Fig. 13, using the same stacking procedure for the two groups of stars as before. The predicted Bondi-Hoyle accretion rates are on average a couple of orders of magnitude lower than the actual accretion rates of the sink particles in the simulation.

Low values of $\dot{\text{M}}_{\text{BH}}$ and the failure of the competitive accretion model can be easily understood from the properties of the stellar mass reservoirs. The Bondi-Hoyle accretion rate is known to be too low if the virial parameter of the region containing the stellar mass reservoir is not much smaller than unity (e.g. Krumholz et al. 2005). Fig. 14 shows that the sphere centred on the sink particle position at birth and with radius equal to the inflow radius, $R_{95}$, is almost always unbound. In the case of the two most massive stars, the values of $R_{95}$ are approximately half the size of the computational volume, so the energy ratio of their mass reservoirs is approximately the same as that of the whole simulation volume, shown by the triangle in Fig. 14. Thus, the drop in the energy ratio with increasing $R_{95}$ for $R_{95} \gtrsim 1$ pc is a numerical constraint. With a larger computational volume, the outer scale of the turbulence would be much larger than 2 pc, and the mass reservoirs of the most massive stars could also be unbound. This is the case in the SN-driven simulation by Padoan et al. (2020), where the outer scale is ~70 pc.

6.3 The observed core mass function

We have identified the progenitor cores from the 3D density and velocity data cubes of the simulation, and with the knowledge of

Figure 14. Scatter plot of the energy ratio, $E_k/(E_{\text{tot}})$, of the spheres centred around the sink particles positions at birth and with radius equal to the inflow radius, $R_{95}$, versus $M_{\text{star}}$, shown for all stars that have finished accreting by the end of the simulation. Magenta circles and black squares are for $M_{\text{star}} \leq 1 M_\odot$ and $M_{\text{star}} > 1 M_\odot$, respectively. The blue triangle marks the energy ratio for the whole box, when the mass is calculated within a sphere of 2 pc radius rather than the whole simulation volume. The red dashed line marks the equipartition in the energy ratio, while the red dotted line marks the 2 pc size limit imposed by the 4 pc simulation cube.

when and where the star particles are formed. Although this allows us to test the main hypothesis of the core-collapse model, it does not closely resemble the process of identification of pre-stellar cores in the observations. The observed pre-stellar CMFs are extracted from 2D intensity information, such as dust-emission or dust-extinction maps, which involves a degree of line-of-sight confusion (e.g. Juvela et al. 2019). Furthermore, the observed quantities must be converted into column density, which, in the case of submm observations, depends on possible temperature and dust-opacity variations, leading to a significant uncertainty in the mass determination (e.g. Malinen et al. 2011; Roy et al. 2014; Pagani et al. 2015; Men'shchikov 2016). Resolution plays a role in deriving the CMF in our simulation, as shown in Appendix C: lowering the resolution by a factor of 8 results in an increase of the median mass by a factor of 3. A similar dependence of the CMF on resolution must also affect the observations.

When a pre-stellar core is identified in the observations, it is hard to know how close it is to produce a protostar. The core may further increase in mass, or perhaps fragment into smaller cores, before the start of the collapse. In our study, we have selected the progenitors at the (approximate) time of star-particle formation. If we search for cores over the whole simulation box, using all available snapshots, and independent of the star-formation time (see Appendix D), we recover pre-stellar cores with median masses about a factor of 2–3 higher than in the case of the progenitor cores at the time of star formation (Fig. D1). We interpret this result as showing that, well before their collapse, pre-stellar cores are more massive, and later fragment into smaller units before they start to collapse into protostars. This is confirmed by the fact that the mass factor decreases over time (Fig. D1). Further evidence of subfragmentation of the more massive cores has already been shown in Section 5.1. A similar 2–3 mass factor due to the fragmentation of cores over time may also affect the observed CMF, in particular at the high-mass end.

It should also be stressed that CMFs are often derived from dust-continuum data without a knowledge of the internal velocity dispersion in the cores, so the internal kinetic energy is neglected in the selection of gravitationally bound cores. Beside the neglect of the kinetic energy, the core thermal and gravitational energies derived
from the observations have significant uncertainties. To account for such uncertainties, observers often assume that a core is gravitationally bound, and can be classified as pre-stellar, if its estimated mass is half of the critical Bonnor-Ebert mass corresponding to the core radius. Besides the uncertainties in the mass determination mentioned above, the peak of the derived CMF is sensitive to this definition of pre-stellar cores, and would shift to larger masses if only gravitationally unstable cores (more massive than the critical Bonnor-Ebert mass) were selected, and/or the core internal kinetic energy were included.

The issues we have raised with regards to the observed CMFs may explain the variation of the peak of the CMF from region to region, even within a homogeneous set of CMFs (same telescope, same data analysis, same research group). For example, the peak mass is found to be a few times larger than the IMF peak in Aquila and Orion (Könyves et al. 2015, 2020), while it is very close to, or even slightly smaller than the IMF peak in Taurus and Ophiuchus (Marsh et al. 2016; Ladjelate et al. 2020). Despite the observational uncertainties and the significant differences in the way cores are extracted from the simulation and the observations, we do find a statistical similarity between the CMF and the IMF, as in the observations. However, our results show that, rather than looking at the IMF as being born from the CMF through a constant efficiency factor, both the CMF and the IMF should be viewed as being formed and fed by the same inertial inflows that arise naturally in supersonic turbulence.

7 CONCLUSIONS
We have addressed the relation between the final mass of a star and that of its pre-stellar core to test the main hypothesis of the core-collapse model. Using a simulation that produces a realistic stellar IMF under realistic physical conditions found in molecular clouds, and hence goes well beyond the earlier investigations of Smith et al. (2009a) and Gong & Ostriker (2015), we have extracted, for each star particle, its gravitationally bound progenitor core, at the time when the star is created. From a statistical analysis, a one-to-one comparison between progenitor and stellar masses, and a study of the mass flow based on tracer particles, we have reached the conclusions listed in the following.

(i) The progenitor CMF converges with resolution, with a peak moving from 0.66 $M_\odot$ to 0.28 $M_\odot$ using resolutions from 800 AU to 100 AU. The estimated converged position of the peak is 0.26 $M_\odot$, close to the IMF peak, which is contradictory to the core-collapse model.

(ii) The CMF derived from the simulation is very similar to the stellar IMF from the same simulation. Irrespective of this statistical similarity, we find no direct correlation between the progenitor core mass and the final stellar mass for individual stars, contrary to the hypothesis of the core-collapse model.

(iii) A significant fraction of the mass reservoir of stars is generally outside of the progenitor cores. This applies across the whole IMF, not just for massive stars. For stars less than 1 $M_\odot$, $\approx 50$ per cent of the stellar mass originates outside the core. This increases to $\approx 90$ per cent for intermediate-mass stars ($2 < M/M_\odot < 5$).

(iv) The inflow region that contains 95 per cent of the mass reservoir of a star is generally much larger than the size of the progenitor core. The ratio between the inflow radius and the core radius has a median value of 14 and its largest values are $\sim 10^3$. This size ratio shows no significant correlation with the final stellar mass.

(v) The competitive-accretion model is also ruled out: the region that amounts to the stellar mass reservoir is not gravitationally bound, hence the Bondi-Hoyle accretion rate from that region is far too small to explain the actual accretion rate. On average, the accretion rate of a star is a decreasing function of its mass, contrary to competitive accretion.

(vi) Observed CMFs should in principle result in a larger core mass on average, compared to the cores selected in the numerical data, because of resolution effects and the possibility that observed cores fragment prior to the star formation. Inclusion of cores that may not be gravitationally unstable in the observed CMFs may have the opposite effect.

The main conclusion of this work is that the results from one of the highest dynamic range star-formation simulations to date, which resolves both the IMF and the CMF, rule out the core-collapse idea for all stellar masses. Because this idea is a fundamental assumption in some recent theoretical models of the stellar IMF, our work implies that attempts at understanding the stellar IMF based on this assumption are incomplete. Specifically, the similarities of the observed CMF with the stellar IMF should not be interpreted as a one-to-one relation between individual core masses and final stellar masses, as the two masses are poorly correlated even when pre-stellar cores are identified without all the uncertainties affecting the observations. Having now established that the stellar mass reservoir resides well beyond the limits of gravitationally bound pre-stellar cores, future theoretical and observational work should address the role of inertial inflows in shaping the stellar IMF.

The main aspects of the results we present here are conceptual in nature, and are thus not likely to crucially depend on numerical resolution or simplifying assumptions such as using an isothermal equation of state. That said, access to even larger computational resources and more efficient computational methods will make it possible to follow up on this investigation by removing some of the computational limitations and omissions of physical effects. Candidates for such improvements include non-ideal MHD, and realistic cooling and heating, with diffuse and point-source radiative energy transfer, to name the perhaps most important ones. In addition, the effective resolution that may be achieved with given resources also depends crucially on optimal use of adaptive mesh refinement, where a mix of criteria may well result in more optimal distributions of cells than relying entirely on the traditional Jeans’s length criterion.

ACKNOWLEDGEMENTS
We are grateful to the anonymous referee for a detailed and useful report. PP and VMP acknowledge support by the Spanish MINECO under project AYA2017-88754-P, and financial support from the State Agency for Research of the Spanish Ministry of Science and Innovation through the ‘Unit of Excellence Maria de Maeztu 2020-2023’ award to the Institute of Cosmos Sciences (CEX2019-000918-M). The research leading to these results has received funding from the Independent Research Fund Denmark through grant No. DFF 8021-00350B (TH). We acknowledge PRACE for awarding us access to Curie at GENCI@CEA, France. Storage and computing resources at the University of Copenhagen HPC centre, funded in part by Villum Fonden (VKR023406), were used to carry out part of the data analysis.

DATA AVAILABILITY
Table 1, as well as other supplemental material, can also be obtained from a dedicated public URL (http://www.erdalab.com/).
From the CMF_to_the_IMF_supplemental_material.pdf.

Column density maps for progenitors of stars 41-50 in Table 1. Please note: Oxford University Press is not responsible for the content or functionality of any supporting materials supplied by the authors. Any queries (other than missing material) should be directed to the corresponding author for the article.

APPENDIX A: IMF CONVERGENCE

Our IMF results are in semi-quantitative agreement with those of Ballesteros-Paredes et al. (2015) and Federrath, Krumholz & Hopkins (2017), while the much larger mass scale obtained by Guszejnov et al. (2020) is incompatible with our results as well as with observations. Using a cloud with 1000 solar masses of gas concentrated into an isolated Bonnor-Ebert like structure with radius 0.084 pc, Lee & Hennebelle (2018) find convergence of the IMF only as with observations. Using a cloud with 1000 solar masses of gas, the simulations of Haugbølle et al. (2018) using a different method that allows us to estimate the converged value. The results are shown in Fig. A1. The top panel shows the stellar IMF histograms from simulations with different root grid sizes (for details, see Haugbølle et al. 2018). The bottom panel shows the peak of the IMF minus the converged value as a function of the simulation root-grid size. A convergence of the peak of the IMF is shown by these points forming almost a straight line (dashed blue line) in logarithmic space. The converged value of the peak of the IMF is found by minimizing the least-squares fit residuals of the points from the straight-line fit, by iterating through a mass range. This results in the converged IMF peak value of 0.17 $M_\odot$, shown in the inset. The lowest root grid size, $16^3$, is not included in the convergence fitting, as its peak value is not fitted well even with a mass limit of 4 $M_\odot$, as can be seen from its histogram in the top panel. Lowering the mass limit to 2 $M_\odot$ requires dropping the $32^3$ case from the fitting, but the remaining three higher root grid sizes points fit almost the same converged peak value as before.

APPENDIX B: SURFACE TERMS

Following the formulation of the Eulerian Virial Theorem (Parker 1979; McKee & Zweibel 1992; McKee 1999) by Dib et al. (2007), the kinetic, $S_k$, and thermal, $S_t$, surface terms are defined as

$$S_k = \frac{1}{2} \oint_S r_i \rho v_i v_j dS,$$

$$S_t = \frac{3}{2} \oint_S r_i P_{ij} dS,$$  \hspace{1cm} (B1)

where $r$ is the distance from the centre-of-mass, $\rho$ is density, $v$ is the velocity relative to the centre-of-mass, $P$ is the thermal pressure.

Given the highly complicated shape of some of our cores, we approximate the surface terms in the following manner. We go over each cell in the progenitor core and flag it as a border cell if at least one of its six face-on neighbours is not part of the core. We then calculate the surface terms by summing over the border cells:

$$S_k = \frac{A_{cell}}{2} \sum r_n \rho_n v_n^2, \quad S_t = \frac{3A_{cell}}{2} \sum r_n P_n,$$  \hspace{1cm} (B2)

where $A_{cell}$ is the area of one face of a cell, $r_n$ is the distance of cell $n$ from the sink particle, $\rho_n$ is the density of cell $n$, $v_n$ is the radial component of the velocity of cell $n$ after the subtraction of the mean velocity of the core, and $P_n$ is the thermal pressure of cell $n$. 

Table A1. Parameters of the lognormal fits to mass histograms in the top panel of Fig. A1, and the number of stars, $N_{\text{star}}$, in each histogram.

<table>
<thead>
<tr>
<th>Resolution</th>
<th>$M_{\text{peak}}$ [$M_\odot$]</th>
<th>$\sigma$</th>
<th>$N_{\text{star}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>1.59</td>
<td>0.42</td>
<td>107</td>
</tr>
<tr>
<td>32</td>
<td>1.14</td>
<td>0.45</td>
<td>170</td>
</tr>
<tr>
<td>64</td>
<td>0.62</td>
<td>0.48</td>
<td>278</td>
</tr>
<tr>
<td>128</td>
<td>0.37</td>
<td>0.47</td>
<td>364</td>
</tr>
<tr>
<td>256</td>
<td>0.26</td>
<td>0.60</td>
<td>411</td>
</tr>
</tbody>
</table>

Figure A1. Top: Stellar IMF histograms for different MHD runs with root-grid sizes $16^3$, $32^3$, $64^3$, $128^3$, and $256^3$. Dashed lines are lognormal fits ($N \propto \exp\left(-\frac{(\log_{10}M - \log_{10}M_{\text{peak}})^2}{2\sigma^2}\right)$) to masses lower than 4 $M_\odot$, and the values are given in Table A1. Bottom: The peak of the IMF as a function of the simulation root-grid size. The peak of the IMF converges towards $0.17 M_\odot$, as shown by $M_{\text{peak}}(t) - M_{\text{conv}}$ almost forming a straight line (blue dashed line) in logarithmic space. The $16^3$ resolution is not included in the convergence fitting. The inset shows the least-squares fitting residuals, with the minimum marked by a vertical dashed blue line.
In addition, we also calculate the kinetic energy of the collapse motion towards the sink particle, $E_{\text{coll}}$:

$$S_k = \frac{V_{\text{cell}}}{2} \sum \rho_n v_{r,n}^2,$$

where $V_{\text{cell}}$ is the volume of a single cell.

Fig. B1 shows the surface terms and the kinetic energy of the collapse motion against the sum of internal kinetic and thermal energies, $E_k$ and $E_t$. The inset shows the histograms of the ratios, showing that the median value of the contribution of the surface terms is 44 per cent and that of the collapse motion is 14 per cent.

### APPENDIX C: CLUMPFIND PARAMETERS

Although the use of density isosurfaces and the value of the related parameters in the clumpfind algorithm are somewhat arbitrary, the tests reported here demonstrate that the main results are insensitive to the details of the choice of parameters.

The clumpfind lower limit of 4 cells per core has no significant effect on the results, since while the selection is done at 100 AU resolution, the MHD run goes down an additional step in resolution. The 4 clumpfind cells thus correspond to 32 MHD cells. Only 12 cores (3.5 per cent) have less than 100 such cells, and excluding those cores would not have a noticeable effect on the results. Only 62 cores (18 per cent) have less than 1000 cells, and excluding even those cores would not have a significant effect.

The effect of the resolution is shown in Fig. C1. The top panel shows the progenitor CMFs for resolutions $1024^3$, $2048^3$, $4096^3$, and $8192^3$ for the whole box, using $f = 2$ per cent and 0.5 pc subcubes around the star particles in the selection. Dashed lines are lognormal fits ($N \propto \exp\left(-\frac{(\log_{10} M - \log_{10} M_{\text{peak}})^2}{2\sigma^2}\right)$ to masses lower than $2 M_\odot$, and the values are given in Table C1. The peak of the CMF converges towards $M_{\text{conv}} = 0.26 M_\odot$, as shown by $M_{\text{peak}}(x) - M_{\text{conv}}$ forming an almost straight line (blue dashed line) in logarithmic space.

### Table C1.

<table>
<thead>
<tr>
<th>Resolution</th>
<th>$M_{\text{peak}} [M_\odot]$</th>
<th>$\sigma$</th>
<th>$f_d$</th>
<th>$f_s$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1024</td>
<td>0.66</td>
<td>0.43</td>
<td>0.93</td>
<td>0.49</td>
</tr>
<tr>
<td>2048</td>
<td>0.46</td>
<td>0.37</td>
<td>0.96</td>
<td>0.62</td>
</tr>
<tr>
<td>4096</td>
<td>0.34</td>
<td>0.43</td>
<td>0.96</td>
<td>0.74</td>
</tr>
<tr>
<td>8192</td>
<td>0.28</td>
<td>0.42</td>
<td>0.92</td>
<td>0.81</td>
</tr>
</tbody>
</table>

By contrast, the density ratio, $f$, does not seem to have an effect at the highest resolution, 8192$^3$. The CMFs are almost identical for residuals are shown in the inset, with the minimum residual value marked by a vertical dashed blue line. The bottom panel of Fig. C1 also shows that $f_s$ increases with resolution, which is another reason to use the highest feasible resolution.
Figure C2. Same as the bottom panel in Fig. 7, but the core selection is done at 1024\(^3\) whole box resolution in 0.5 pc subcubes around the star particles. Progenitors are plotted with different symbols based on how many and how old stars they have inside them: progenitors with only one star (blue crosses), and progenitors that have multiple stars born at the same time (green triangle). The red line is drawn at \(M_{\text{star}} = \epsilon_{\text{acc}} M_{\text{prog}}\), with \(\epsilon_{\text{acc}} = 0.5\). Black and blue lines are fits to all progenitors and the single-star progenitors, respectively.

\(f = 2, 4, \text{ and 8 per cent. This is presumably because, at 8192}^3\), the core boundary is already sharp enough that we do not need to have a lower value of \(f\) to separate neighbouring cores from each other.

Fig. C2 shows the one-to-one scatter plot of final stellar masses and the masses of their progenitors, like in the bottom panel of Fig. 7, but the selection is done at 1024\(^3\) resolution instead of 8192\(^3\). It is clear that the one-to-one correlation of progenitor and stellar masses is even worse than in Fig. 7, giving a value of the Pearson’s correlation coefficient \(r = 0.48\), even though the slope is similar, \(a = 0.54\). However, considering only the progenitors with a single newborn star, we get \(r = 0.53\) and \(a = 0.57\), which are similar to those found for single-star progenitors in Fig. 7, \(r = 0.55\) and \(a = 0.54\).

APPENDIX D: THE CMF OF THE WHOLE BOX

What does the CMF look like, if we do the detection on the whole 4 pc simulation box without a priori knowledge of the star particles? We add the stellar mass in (see Section 3.3) and do the bound core selection in each snapshot at 1024\(^3\) resolution, using minimum density level 10 and \(f = 2\) per cent. We then categorize them as pre-stellar cores without stars, pre-stellar cores with stars (one or more stars that formed in that snapshot) which would be our progenitor cores, and protostellar cores (one or more older stars), according to the star locations and ages.

Fig. D1 shows the mass histograms of all pre-stellar cores detected in the 118 snapshots of the simulation, divided between the first half and the second half of the simulation, and in subcategories of pre-stellar cores without stars and progenitors where a star is currently forming. We can see from the median values that if we do not have a priori information on current star formation, the median mass of all pre-stellar cores is about three times higher than that of just the progenitors for the first half, but this decreases to a ratio of two in the second half, hinting that the larger bound clouds fragment into smaller ones as the simulation progresses.

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