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Orbital eccentricity–multiplicity correlation for planetary systems and comparison to the Solar system

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ABSTRACT

The orbit eccentricities of the Solar system planets are unusually low compared to the average of known exoplanetary systems. A power-law correlation has previously been found between the multiplicity of a planetary system and the orbital eccentricities of its components, for systems with multiplicities above two. In this study we investigate the correlation for an expanded data sample by focusing on planetary systems as units (unlike previous studies that have focused on individual planets). Our full data sample contains 1171 exoplanets, in 895 systems, and the correlation between eccentricity and multiplicity is found to follow a clear power law for all multiplicities above one. We discuss the correlation for several individual subsamples and find that all samples consistently follow the same basic trend regardless of e.g. planet types and detection methods. We find that the eccentricities of the Solar system fit the general trend and suggest that the Solar system might not show uncommonly low eccentricities (as often speculated) but rather uncommonly many planets compared to a ‘standard’ planetary system. The only outlier from the power-law correlation is, consistently in all the samples, the one–planet systems. It has previously been suggested that this may be due to additional unseen exoplanets in the observed one-planet systems. Based on this assumption and the power-law correlation, we estimate that the probability of a system having eight planets or more is of the order of 1 per cent, in good agreement with recent predictions from analyses based on independent arguments.

Key words: astробiology – methods: data analysis – planets and satellites: fundamental parameters – planets and satellites: general – planets and satellites: dynamical evolution and stability.

1 INTRODUCTION

Extrasolar planets reveal orbital eccentricities much higher than those found among the planets of the Solar system, a deviation that in the beginning was considered so strange that it even lead some people to doubt whether the radial-velocity (RV) exoplanet measurements actually showed real planets. In this study we will show that the eccentricity of the Solar system planets actually follow the same trend as all other known planetary systems, but belong to the tail of a continuous distribution. When searching for extraterrestrial life we often focus on Earth-like planets and Solar-system-like systems, and so low eccentricities are included in our search criteria. But exactly how the habitability of a planet might be affected by the eccentricity of its orbit is yet unknown. A planet on a high-eccentricity orbit can undergo drastic seasonal changes in surface temperature due to the difference in stellar radiation from perihelion to aphelion. These seasonal changes could lead to periods of time without liquid water on the surface, which would greatly limit the habitability of the planet (Bolmont et al. 2016). However, a series of studies (reviewed in Kopparapu, Wolf & Meadows 2019) have found that often the atmosphere and oceans of a planet can act like a buffer to the temperature variations, in which case the surface climate will be determined by the average stellar radiation rather than the seasonal extremes. In other cases large seasonal variability was found to expand the habitable zone for the planet, by allowing water to remain liquid at larger semimajor axes (Linsenmeier, Pascale & Lucarini 2015). Since it is still uncertain how orbit eccentricities affect the habitability of a planet, it is critical for us to study and understand the eccentricities in the existing exoplanet sample and how they might deviate from those in the Solar system.

From previous investigations (Chatterjee et al. 2008; Ford & Rasio 2008; Jurić & Tremaine 2008a,b; Carrera, Raymond & Davies 2019), planet–planet interaction has been suggested as the dominating mechanism determining orbital eccentricities of planets, either through dynamical relaxation or planet–planet scattering. The dynamical interactions of planetary systems are reviewed in Davies et al. (2014). As a conclusion of this, a correlation between orbital eccentricity and multiplicity (number of planets) is predicted. This prediction has been tested empirically by Limbach & Turner (2015) based on 403 exoplanets detected by the RV method and listed in the Exoplanet Orbit Database, exoplanets.org, (Han et al. 2014)). A strong anticorrelation between eccentricity ($e$) and multiplicity ($M$) was found, and for multiplicities above two the correlation could be described by a power law: $e(M) \approx 0.584 \cdot M^{-1.20}$. The eccentricity–multiplicity correlation has later been investigated by Zinzi & Turrini (2017), who found a similar correlation for multiplicities above one based on 258 selected RV and transit planets from NASA Exoplanet Archive. Both of the previous investigations have based their analyses on individual planets rather than treating the systems as units.

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The main motivation for this article is to further the investigations by Limbach & Turner (2015) and Zinzi & Turrini (2017) using the expanded planet sample known to date, comparing search methods, population groups, and data bases, and aiming to set the results in perspective to our own Solar system and habitability. Our planet sample contains planets found by several detection methods including RV, transiting planet (transit), microlensing (ML), and others. By including all planets, regardless of detection method, we will be able to comment on whether there is an observational bias related to the specific methods, and the large data set available today makes it possible to exclude more planets that might potentially introduce unwanted bias into the correlation. Unlike the previous investigations we will treat each system as a unit by conducting the analysis based on the average orbital eccentricities in the systems rather than the eccentricity of each individual planet. This is done since both the multiplicity and potential planet–planet interactions are properties of the planetary system as a whole rather than the individual planets.

From the resulting eccentricity–multiplicity correlation an estimate of the mean multiplicity of a planetary system can be obtained in addition to a probability distribution of the multiplicity of planetary systems. From this we wish to set our Solar system in perspective against a ‘standard’ planetary system. We envision that planetesimals are formed in relatively circular orbits, then gravitationally scatter one another into higher eccentricity, before they over longer timescales collide to build up solid planets or the planetary cores of giants. After the evaporation of the gas disc, planet–planet interaction would be the dominating mechanism determining the final eccentricities, in such a way that the more planets there end up being in the system the more circular the orbits become. This is a logic scenario to provide an image of the physical process behind the correlation we investigate in this paper, but we stress that this is only an image that helps us (and hopefully the reader, too) to imagine the process. Our study is empirical, and hence has no a priori assumption about which exact mechanisms cause the correlation. In order to further the development of the theoretical understanding, we take advantage of the large sample now available to also analyse whether different populations of exoplanets show different correlations.

A major concern when investigating extrasolar planets is that we are highly constrained by limitations in our detection methods. When using RV the detection probability of a planet is biased towards large masses, and when using transit it is biased towards ultrashort periods. That leaves a large parameter space where planets go mainly undetected, and thereby bias conclusions about standard planetary systems drawn from the limited sample. Today the two most abundant detection methods (RV and transit) basically have shown us that exoplanetary systems very different from our own Solar system are abundant. Direct observational estimates of how abundant exoplanetary systems resembling our own Solar system are, may most likely come from future extensive microlensing surveys from space [perhaps from a dedicated microlensing satellite (Bennet & Rhee 2002) or from WFIRST (Penny et al. 2019)] or from the ground [perhaps from GravityCam-like instruments (Mackay et al. 2018)], and they will give us the full set of orbital parameters of Solar-system-like exoplanets (Gaudi 2012; Ryu et al. 2018), as opposed to today where orbital eccentricity has been obtained for only one microlensing exoplanet (Gaudi et al. 2008). Until then it can be useful to look at indirect evidences for what a standard exoplanetary system looks like. A motivation for this article is to go beyond the data sample by finding a general theory for all systems (including those with planets yet undetected), and from this estimate the characteristics of standard planetary systems. This may give us some insight into the standard formation mechanism of planetary systems and how they develop into the most common configurations of planets, give hints about what to look for and thereby which instruments to develop, and maybe contribute to give us a more realistic view on how abundant truly Earth-like exoplanets might be. One such indirect method is the study of the eccentricity distribution among known exoplanets, as presented here.

In Section 2, the data set is discussed. In Section 3, the correlation between eccentricity and multiplicity is examined, both for the full data samples from two different data bases, for subsamples sorted for detection methods and for population groups, and for a high-eccentricity subsample in which we attempt to exclude most systems containing undiscovered planets. Based on the correlation a power law is found. In Section 4, some of the potential implications of the power-law correlation are explored. A probability distribution of the multiplicity is found, and from this a mean multiplicity of planetary systems is estimated. In Section 5, the results and theories are discussed. Finally in Section 6, the conclusions are summarized.

2 THE DATA SET

Our data from The Extrasolar Planets Encyclopaedia, exoplanet.eu, (Schneider et al. (2011)) were retrieved in August 2019. All confirmed planets regardless of detection method are included. We are aware that exoplanet.eu, like most other data bases, might be subject to errors in their data listing. For the sake of this study we mostly try not to question the validity of the data found on the website. Planets without listed eccentricities or where the eccentricity is falsely listed as zero (i.e. without listed uncertainties) are excluded from the sample. Of the 4103 planets listed on exoplanet.eu a total of 1171 planets remain in the sample, 2932 are excluded due to unknown eccentricities and 60 of these have eccentricities listed as zero with unknown uncertainties. In Table 1 the number of planets sorted by multiplicity can be seen for each of the included detection methods.

Because no multiplicities are listed on exoplanet.eu each planet has been given a multiplicity based on the number of confirmed planets orbiting the same star listed in the data base. Since some of the systems might contain yet undiscovered planets the known companions in these systems will initially be sorted into the wrong multiplicity bins, and the actual distribution might differ from Table 1. Due to the small number of systems with high multiplicities, all systems with more than 5 known planets have been combined in one bin. The multiplicity of this bin is calculated as the mean multiplicity of the included systems. Note that the number of planets in each bin is not necessarily a multiple of the multiplicity. This is

<table>
<thead>
<tr>
<th>Multiplicity</th>
<th>Total</th>
<th>RV</th>
<th>Transit</th>
<th>Other</th>
<th>Systems</th>
</tr>
</thead>
<tbody>
<tr>
<td>M1</td>
<td>667</td>
<td>408</td>
<td>234</td>
<td>23</td>
<td>667</td>
</tr>
<tr>
<td>M2</td>
<td>274</td>
<td>215</td>
<td>52</td>
<td>5</td>
<td>151</td>
</tr>
<tr>
<td>M3</td>
<td>121</td>
<td>65</td>
<td>50</td>
<td>6</td>
<td>45</td>
</tr>
<tr>
<td>M4</td>
<td>63</td>
<td>43</td>
<td>17</td>
<td>3</td>
<td>20</td>
</tr>
<tr>
<td>≥5</td>
<td>46</td>
<td>34</td>
<td>10</td>
<td>2</td>
<td>12</td>
</tr>
<tr>
<td>Total</td>
<td>1171</td>
<td>765</td>
<td>363</td>
<td>39</td>
<td>895</td>
</tr>
</tbody>
</table>

Table 1. Planets included in data samples. Retrieved from exoplanet.eu. Planets are sorted for detection method. Rightmost column show the number of systems present in each multiplicity bin, whereas columns 2-5 show number of individual planets.

1 All planets and systems with a multiplicity of X will henceforth be referred to as MX-planets or MX-systems
caused by the fact that not all planets in each system are included, mainly because their eccentricities are unknown. Our data set is three to four times larger than any of the previous analyses [1171 in this study, compared to 403 in Limbach & Turner (2015) and 258 in Zinzi & Turrini (2017)]. We have not accounted for the uncertainties listed for each of the eccentricities in the data base in this analysis, which will be discussed further in Section 5.

3 ECCENTRICITY AND MULTIPLICITY

Each system is assigned an eccentricity found as the mean eccentricity of the planets in the system. This differs from previous studies, where the planets were not sorted into systems, and the authors looked at the eccentricities of the individual planets. The final results from the two methods do not differ greatly, but we find that sorting the planets into systems is more meaningful, since the effects we observe might be caused by planet–planet interactions within the systems and will change the system as a whole. These assigned system eccentricities are then used to calculate overall mean and median eccentricities within each multiplicity bin. In Fig. 1, mean and median values of the system eccentricities are plotted for each of the multiplicity bins, together with our Solar system with a multiplicity of eight.

The errors are calculated using the following methods: Mean: As the standard deviation of system means found by the Bootstrap method. Median: As the one-third and two-third quantiles from a Cumulative Distribution Function divided by √N − 1, where N is the number of systems in the multiplicity bin. Notice that the errors indicate the uncertainties of the mean and median eccentricities of each multiplicity bin, and not the spread of the eccentricities among the individual planets, which is significantly larger than the errors shown. Fig. 1 suggests a trend of decreasing eccentricity for increasing multiplicity. As can be seen the Solar system too follows this trend indicating that our system does not deviate from the norm. An exception for this trend, is the M1 systems. Whereas the other systems are dominated by super-Earths (m_p < 0.1M_J), the M1 systems are giant-planet systems, whereas the larger multiplicity systems are dominated by super-Earths. A priori one could expect that since the cold-Jupiters dominate the M1 systems, we could seek the explanation for the deviation from the power law followed by the M > 1 systems in the cold-Jupiter population. However, we find that this is not the case, when we look at the mean eccentricities plotted as a function of multiplicity in Fig. 2.

Fig. 2 shows the mean eccentricities plotted for the full sample (equivalent to the mean values from Fig. 1) together with the three

![Figure 1. Mean and median values of the eccentricity for each multiplicity. The mean eccentricity of the Solar system is plotted with a black ×. The multiplicity of the ≥M5 multiplicity-bin is plotted as M = 5.7.](image)

Table 2. Distribution of the systems in Table. 1 where in addition to the eccentricity, also the mass or msin(i) is known, such that they can be divided into the groups: hot-Jupiters (HJ), cold-Jupiters (CJ), super-Earths (SE), and plotted in Fig. 2. Last column shows the number of systems (Number). A total of 849 systems are included.

<table>
<thead>
<tr>
<th>Multiplicity</th>
<th>HJ (per cent)</th>
<th>CJ (per cent)</th>
<th>SE (per cent)</th>
<th>Number</th>
</tr>
</thead>
<tbody>
<tr>
<td>M1</td>
<td>39.2</td>
<td>51.3</td>
<td>9.4</td>
<td>637</td>
</tr>
<tr>
<td>M2</td>
<td>22.9</td>
<td>57.6</td>
<td>19.4</td>
<td>144</td>
</tr>
<tr>
<td>M3</td>
<td>25.6</td>
<td>20.5</td>
<td>53.8</td>
<td>39</td>
</tr>
<tr>
<td>M4</td>
<td>21.1</td>
<td>26.3</td>
<td>52.6</td>
<td>19</td>
</tr>
<tr>
<td>≥M5</td>
<td>10.0</td>
<td>30.0</td>
<td>60.0</td>
<td>10</td>
</tr>
</tbody>
</table>

3.1 Planet populations

A potential uncertainty related to the study of an eccentricity–multiplicity correlation is the dependence of the correlation on factors such as planet mass and semimajor axis. Turrini, Zinzi & Belinchon (2020) and Laskar & Petit (2017) therefore looked at the correlation of multiplicity and angular momentum deficit (AMD), rather than multiplicity and eccentricity. The AMD does depend on the eccentricity, but also on the semimajor axis and the mass of the planets, and Turrini et al. (2020) found an anticorrelation between the normalized angular momentum deficit (NAMD) and the multiplicity. Turrini et al. (2020) argues that the eccentricity–multiplicity correlation found by other studies is a reflection of the underlying NAMD–multiplicity correlation. The study of the NAMD–multiplicity is complicated by the fact that few planets have both their masses, eccentricity and semimajor axis well-known, and as such the data set is smaller. The larger sample in our data set compared to previous data sets, allows us to study directly the correlation of eccentricity and multiplicity for a number of different subsamples, in order to test how the planet mass (m_p) and semimajor axis (or period, P) might affect the eccentricity–multiplicity correlation.

To test the impact of mass and period, we have divided the systems into three different populations: (1) Systems containing a hot-Jupiter (m_p > 0.1M_J and P < 100 d). (2) Systems containing a cold-Jupiter (m_p > 0.1M_J and P > 100 d), and no hot-Jupiters. (3) Systems dominated by super-Earths (m_p < 0.1M_J) with no giant planets. In order to increase the data sample, planets with no listed mass in the data base, have been sorted based on their mass · sin(i) value, when this is known, and a total of 849 systems are sorted into the population categories. The distribution of systems in each population category can be seen in Table 2. It should be noted, that the observed planet sample does not represent the true planet population since some planet types are more easily observed than others, but the differences between the populations, as shown here, might still give us an insight into the uncertainties of the eccentricity–multiplicity correlation. Research in the actual occurrence rate of different planet types is reviewed in e.g. Winn & Fabrycky (2015).

Table 2 shows that different multiplicities are dominated by different populations of planets, such that most of the M1 systems are giant-planet systems, whereas the larger multiplicity systems are dominated by super-Earths. A priori one could expect that since the cold-Jupiters dominate the M1 systems, we could seek the explanation for the deviation from the power law followed by the M > 1 systems in the cold-Jupiter population. However, we find that this is not the case, when we look at the mean eccentricities plotted as a function of multiplicity in Fig. 2.

Fig. 2 shows the mean eccentricities plotted for the full sample (equivalent to the mean values from Fig. 1) together with the three
Limbach & Turner (2015), and a full sample of the 704 planets with known eccentricities, a subsample consisting of RV planets listed on exoplanets.org systems containing undiscovered planets. According to the trend have been fitted to all samples for multiplicities above one. Due to the small overall mean eccentricities for all systems in each multiplicity bin, corresponding to the data points seen in the figure. Due to the small sample of Jupiter-systems with four or more planets, the M4 and ≥M5 bins have been combined for the hot-Jupiter and cold-Jupiter systems. The multiplicities for these bins are the mean multiplicities among the systems combined in the bins. The main conclusion from Fig. 2 is that all three populations follow similar power law trends to the one for the full sample (although of course with larger scatter of the individual points due to the smaller data sample). We notice that the cold-Jupiter population is not the cause of the low eccentricities of the M1 systems, but on the contrary displays the highest eccentricities of the M1 systems among all populations.

3.2 The undiscovered planets in the systems

To get further understanding of the uncertainties of the power-law correlation, Fig. 3 shows the mean eccentricities plotted as a function of multiplicities for three additional subsamples: Beside the full system sample from exoplanet.eu, are shown a high-eccentricity subsample consisting of only the 75 per cent systems with highest eccentricities, a subsample consisting of RV planets listed on exoplanets.org before 2014 (L&T) equivalent to the sample used by Limbach & Turner (2015), and a full sample of the 704 planets with known eccentricities from the data base exoplanets.org. Power laws have been fitted to all samples for multiplicities above one.

The high-eccentricity subsample has been created to exclude systems containing undiscovered planets. According to the trend visible in Fig. 1 larger systems have lower eccentricities, and systems with additional, undiscovered, planets should therefore have eccentricities below what is appropriate for their given multiplicity. We might therefore expect, that the systems showing the lowest orbital eccentricities, could have extra undiscovered planets. Removing these systems from the fit does change the relation a bit (obviously shifting the line to somewhat higher eccentricities), but do keep the same trend of a fine linear fit to the systems with M > 1 and a substantially lower average eccentricity for the M1 systems than expected from the power law.

Since both of the dominating detection methods (the RV method and the transit method) depend on the size of the planets, smaller planets are more difficult to detect, and only few planets with a size comparable to Mercury or Mars have been found. Mars and Mercury represent one fourth of the (known) planets in the Solar system, and following this line of argument a first attempt of a qualified guess on a typical number of undetected planets could be, that a minimum of 25 per cent of the planets in exoplanet systems remain undiscovered. By removing the 25 per cent systems with the lowest eccentricities in each multiplicity-bin we hope to lower the bias in the correlations by ’contamination’ due to systems with unknown planets. No systems are removed from the M8 bin, since this only consist of the Solar system. We see from Fig. 3 that the high-multiplicity systems are less affected than the low-multiplicity systems when removing the 25 per cent lowest eccentricity systems, indicating that high-multiplicity systems could be more completely surveyed.

The L&T subsample has been plotted to compare the power-law correlation found in this study with one found using a data sample similar to the one used in the original study by Limbach & Turner (2015). Notice that whereas the mean eccentricities for the full, high-eccentricity, and exoplanets.org subsamples are found as the mean of the system eccentricities for each multiplicity, the mean eccentricities of the L&T subsample are found as the mean of all planets in each multiplicity-bin (to stay consistent with the analysis methods used by Limbach & Turner (2015) as explained previously).

In order to further constrain potential uncertainties related to our data, we repeated the entire analysis using data from the data base exoplanets.org. It should be remembered that our main data base, exoplanet.eu, is more complete and up to date than exoplanets.org, but that the planets listed on exoplanets.org have undergone a more
strict selection process in regard to peer-review (Han et al. (2014),
Schneider et al. (2011), and personal communication with Jason
Wright and Françoise Roques). Although the two data bases therefore
will not contain the exact same data sample, comparison of the
results based on both data bases gives more clear impression of the
uncertainties.

Fig. 3 shows that all the subsamples, display the same general
tendency of a power-law correlation between eccentricity and mul-
tiplicity for $M > 1$ as the full sample, and a lower eccentricity of the M1
systems not following the power-law trend of the higher multiplicity
systems. The slopes, however, vary for the different samples.

3.3 Detection methods

Whereas the L&T subsample consists only of RV planets our sample
contains planets found by all detection methods. To test how this
difference might affect the eccentricity–multiplicity correlation, and
to better understand whether the behaviour of the correlation could
be dominated by a bias effect related to the detection method, a plot
for the transit and RV subsamples together with the full sample can
be seen in Fig. 4. It should be noted that the eccentricities listed for
planets discovered with the transit method are often determined from
follow-up RV observations, so the two populations are not completely
separated. Fig. 4 shows that both the transit and the RV subsamples
have eccentricity–multiplicity correlations similar to that of the full
sample, and the trend of the M1 systems falling below the $M > 1$
relation is identical.

We also see that the transit systems show lower eccentricities at
all multiplicities compared to the RV systems. This bias, that transit
planets generally have lower eccentricities, is in correspondence with
a study by Van Eylen & Albrecht (2015) who found high-multiplicity
Kepler planets to generally have lower eccentricities than the RV
planet sample. This tendency might be caused by the bias, that there
are more low-mass planets in the transit subsample than in the RV
sample, and that lower mass planets are more easily circularized by
planet–planet interaction (Kane et al. 2012). We see a hint of the same
tendency in Fig. 2 where the super-Earth subsample shows lower
eccentricities than the full sample, and the important conclusion is
that independent of the shift and its potential explanation in an
observational bias, the same tendencies discussed above applies to
both of the subsamples.

It is also possible that planet–planet scattering could cause a spread
in the orbital inclinations (Chatterjee et al. 2008) in addition to
lowering the multiplicity of the system. The spread in inclination
could lead to a higher number of undiscovered planets in the transit
systems and thereby a higher number systems with eccentricities too
low to fit their assigned multiplicity. This trend would be strongest
for low-multiplicity systems, as seen in Fig. 4, if these are formed
due to severe planet–planet scattering. It can be seen from the error
bars given in Fig. 4 that the listed eccentricities of the transit planets
have a greater variation than the RV planets, possibly caused by a
larger uncertainty in their determination (Kane et al. 2012; Van Eylen
& Albrecht 2015).

3.4 Kolmogorov–Smirnov test

To statistically test the correlation between multiplicity and eccen-
tricity, a two-sample Kolmogorov–Smirnov is conducted on the full
system sample. The test compares the multiplicity-bins one and one
to test the difference in the eccentricity distributions of the systems.
The test results can be seen in Table 3. Notice that the distribution of
eccentricities for the individual planets is used for the Solar system,
whereas the distributions of the systems are used for the rest.

It can be seen that the eccentricities of most of the multiplicity-
combinations show significant differences, on a 5 per cent sig-
ificance level. This indicates that the difference in eccentricity
for systems of different multiplicity is caused by a connection
between the two factors and not by coincidence. The higher $p$-
values seen for high-multiplicity combinations might be caused by
the small number of systems in these multiplicity-bins. Altogether
the statistical test supports, that there is a correlation between multiplicity
and eccentricity.

3.5 Quantification of the multiplicity-eccentricity correlation

In the standard core-accretion model for the formation of planetary
systems, the dust component of the disc relatively quickly clumps
together (via simple condensation or even faster via streaming
instability) to form many objects of planetesimal sizes (Johansen
& Lambrechts 2017). Over a longer time-scale the planetesimals
then excite one another’s orbits by gravitational interaction, leading
to collisions and hence growth to planet size. After the dissipation of
the protoplanetary disc the orbits of the planets are largely determined
by planet–planet interactions, indicating a correlation between the
orbital eccentricity and the number of interactions and hence planets.
The numerical simulations by Chatterjee et al. (2008) and Jurić
& Tremaine (2008) confirms that this expectation is correct, by
showing that the final architecture of a system is almost independent

<table>
<thead>
<tr>
<th>Multiplicity</th>
<th>M1</th>
<th>M2</th>
<th>M3</th>
<th>M4</th>
<th>$\geq$M5</th>
<th>M8 (SS)</th>
</tr>
</thead>
<tbody>
<tr>
<td>M1</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>M2</td>
<td>&lt;0.01</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>M3</td>
<td>0.04</td>
<td>0.01</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>M4</td>
<td>0.01</td>
<td>&lt;0.01</td>
<td>0.15</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\geq$M5</td>
<td>0.04</td>
<td>&lt;0.01</td>
<td>0.06</td>
<td>0.31</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>M8 (SS)</td>
<td>0.01</td>
<td>&lt;0.01</td>
<td>0.05</td>
<td>0.38</td>
<td>0.65</td>
<td>1</td>
</tr>
</tbody>
</table>

Figure 4. Mean values of eccentricities for each multiplicity for three
subsamples. Full red line: The full sample. Dashed: Subsample consisting
of planets discovered by the transit method. Dotted: Subsample consisting
of planets discovered by RV. Mean value of the Solar system (SS) is plotted
in black. Power laws (PL) have been fitted to all samples for multiplicities
above one.
of the assumed starting conditions of planetesimals, and suggesting that planet–planet interaction is the dominating mechanism for changing the average orbital eccentricity. The simulations do not in themselves predict a specific analytical correspondence between eccentricity and multiplicity, which, however, can be done by fitting the corresponding observational data. In Fig. 3, it was indicated that the high-multiplicity systems seemed to have fewer undiscovered planets, and in Figs 2–4 we quantified the relation by fitting the mean eccentricities for \( M > 1 \) to a power law. Our best fit to the full set of data (as shown in red in the figures) can be expressed as

\[
e(M) = 0.429 \cdot M^{−0.93},
\]

where \( e \) is the eccentricity and \( M \) is the multiplicity. Figs 2–4 further demonstrate that this fit also agrees with the Solar system despite the fact that the \( M = 8 \) was not included in the fit. This adds extra confidence in believing that the quantification is universal, and two fits, with and without the Solar system, showed the following correlation coefficient: \( R^2 = 0.98 \) for \( M = [2; 7] \) and \( R^2 = 0.99 \) for \( M = [2; 8] \).

Since the physical cause behind the relation is thought to be planet–planet gravitational interaction, one should expect the decreasing tendency to range all the way from \( M1 \) systems to a maximum number of planets, \( M_{\text{max}} \), for which the systems can still remain stable (Papaloizou & Terquem 2001; Jurić & Tremaine 2008b), with the \( M1 \) systems having the largest average eccentricity. Observationally, the \( M1 \) planets, obviously, do not show the high eccentricity expected from the correlation, and therefore the observed \( M1 \) systems must be affected differently from the multiplanet populations. In the following section, Section 4, we will elaborate on one potential explanation for the deviation of the \( M1 \) systems from the trend, namely the idea that the low \( M1 \) eccentricity is caused by a combination of mechanisms other than the general planet–planet interaction, lowering the eccentricities, plus an observational bias. When correcting for these two effects, the remaining \( M1 \) systems are made to follow the same trend as the rest of the systems, and potential implications for the trend are explored.

An alternative explanation for the discrepancy between the \( M1 \) and multiplanet systems could be that they are dominated by different planet populations. To analyse if any specific population dominates the lowering of the \( M1 \) eccentricities, we investigated, in Section 3.1, whether the population of large planets (which observationally dominates the \( M1 \) and \( M2 \) systems) and the population of smaller planets (that have a more dominating role in the higher multiplicity systems), show different observational trends. We concluded that all of the populations follow the same general trend between eccentricity and multiplicity, indicating that the same general mechanism is responsible for all the observed populations of exoplanets from \( M1 \) to \( M8 \) (and is likely to be planet–planet interaction with some correction for the \( M1 \) systems).

In all cases, it is obvious from Figs 1–4 that the observed \( M1 \) systems do not follow the trend expressed in equation (1). If a reasonable transformation from the observed abundance of \( M1 \) systems to intrinsic \( M1 \) system abundances can be obtained, it will be possible from equation (1) to give an estimate of the true probability distribution of multiplicities among the observed systems.

### 4 Perspective and Implications: Conversion of Observed Multiplicity Distribution to Actual Distribution

Figs 1–4 demonstrate that the observed average eccentricity of one-planet systems (\( M1 \)) falls below the relation for multiplanet systems. The main assumption in this further analysis is that the \( M1 \) systems intrinsically follow the same eccentricity correlation as the other multiplicities. This assumption is supported by a series of studies by He, Ford & Ragozzine (2019), He et al. (2020), who recreated the multiplicity distribution of the Kepler observations, by forward-modelling multiplanet systems at the AMD-stability limit [introduced in Laskar & Petit (2017) and Petit, Laskar & Boué (2017)]. He et al. (2020) found that all multiplicities from one to ten followed the same eccentricity–multiplicity power-law correlation, with the intrinsic \( M1 \) systems having higher eccentricities than the multiplanet systems, and they found that most observed \( M1 \) systems contain yet undiscovered planets. In this section we will try to identify these systems with undiscovered planets, and redistribute them to the multiplicity bin appropriate to their multiplicities.

We will first investigate whether some of the low eccentricity \( M1 \) planets can have got their low eccentricity due to other mechanisms than the general planet–planet interaction assumed to be responsible for equation (1).

Exoplanets in ultrasmall orbits are often tidally locked to the host star, which could lead to circularization of the planetary orbit (Jackson, Greenberg & Barnes 2008). By looking at the eccentricity damping time-scale (Ogilvie 2014), the eccentricity damping from these planet-star interactions can be approximated by

\[
\dot{e} \propto \frac{m_p}{m_* a^2},
\]

where \( \dot{e} \) is the change in eccentricity, \( a \) is the semimajor axis of the planet, and \( m_p \) and \( m_* \) are the masses of the planet and the star respectively.

In order to distinguish systems that have low eccentricities due to planet-star interactions from those that may have low eccentricities for other reasons, all planets for which the value from equation (2) exceeds a certain threshold are excluded. The threshold was chosen to \( 6.77 \times 10^5 \), and 191 \( M1 \) planets, and 100 planets among the other multiplicities, were excluded on this basis. These planets will be excluded in the following probability analysis, but were not excluded in the making of equation (1) (which would have very small effect as described below). The chosen threshold is the value of Mercury, and even though Mercury is far from being circularized (it holds the highest eccentricity in the Solar system), it is ‘almost’ tidally locked (in a 2/3 orbital/rotational resonance), and is the planet in the Solar system that has the highest potential for tidal circularization. In an analysis of hot-Jupiters with known obliquities, Hjort (2019) was able to divide the planets into two distinct groups, with 15 per cent of the planets having extremely low obliquity (and hence low eccentricity) and 85 per cent having a continuous obliquity distribution. Hjort (2019) assigned the former group to planet migration in the disc and the latter to migration due to planet–planet interaction (scattering). It is therefore likely that also a fraction of the \( M1 \) systems will have much lower eccentricities than expected from equation (1) due to disc migration.

Next, we pursue the idea that some of the remaining systems may contain yet undiscovered planets, and that these systems will lower the mean eccentricity of their multiplicity bins, since systems with more planets are expected to have lower eccentricities. Those of the observed systems that have had their eccentricity determined by planet–planet interactions (as opposed to the systems excluded above due to a potential star–planet circularization) are to first approximation expected to follow the planet–planet eccentricity relation expressed in equation (1). We align the mean eccentricities of the multiplicity bins with the power-law correlation by moving the lowest eccentricity systems of the multiplicity bins to an \( M \) corresponding
The new multiplicity, $M$, by artificially counting them as belonging to higher values of $M$ undiscovered planets, we attempted a redistribution of the systems with eccentricities that potentially could be attributed to yet undiscovered planets. The rightmost column indicates the probability of a system having a given multiplicity according to equation (3).

Table 4. Redistribution of systems. Left: the observed multiplicity distribution of systems from exoplanet.eu. Right: the multiplicity distribution of systems after the M1 systems have been redistributed according to their eccentricities as described in the text. The rightmost column indicates the probability of a system having a given multiplicity according to equation (3).

<table>
<thead>
<tr>
<th>Multiplicity</th>
<th>Observed distribution</th>
<th>Redistribution</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Number of systems</td>
<td>Percentage (per cent)</td>
</tr>
<tr>
<td>M1</td>
<td>667</td>
<td>75</td>
</tr>
<tr>
<td>M2</td>
<td>151</td>
<td>17</td>
</tr>
<tr>
<td>M3</td>
<td>45</td>
<td>5</td>
</tr>
<tr>
<td>M4</td>
<td>20</td>
<td>2</td>
</tr>
<tr>
<td>M5</td>
<td>4</td>
<td>&lt;1</td>
</tr>
<tr>
<td>M6</td>
<td>6</td>
<td>&lt;1</td>
</tr>
<tr>
<td>M7</td>
<td>1</td>
<td>&lt;1</td>
</tr>
<tr>
<td>M8</td>
<td>1</td>
<td>&lt;1</td>
</tr>
<tr>
<td>M9</td>
<td>5</td>
<td>&lt;1</td>
</tr>
<tr>
<td>M10</td>
<td>9</td>
<td>&lt;1</td>
</tr>
<tr>
<td>Total</td>
<td>895</td>
<td></td>
</tr>
</tbody>
</table>

Figure 5. Percentage of systems with given multiplicity, corresponding to values from Table 4. Probability function found as exponential fit. Mean multiplicity estimated to ~2.5.

We therefore suggest that the $M_{\text{new}}$ distribution in Table 3 is a reasonable first qualified guess of the relative distribution of the number of planets in planetary systems, whose average eccentricity distribution is determined by planet–planet interactions. This probability distribution is shown in Fig. 5 and has been fitted to an exponential function described as

$$P(M) = 0.72 \cdot e^{-0.54M},$$

where $P(M)$ indicates the probability of a system having $M$ planets. This relation has been found by normalizing the exponential fit seen in Fig. 5, such that $\sum_{M=1}^{10} P(M) = 1$. 

to their observed eccentricity (i.e. assuming undiscovered planets in those systems). During this exercise it was found that the best alignment occurred when 55 per cent of the M1 systems and all of the $M > 1$ systems were assumed not to contain undiscovered planets and the rest had new multiplicities estimated based on their eccentricity.

Of the M1 systems 50 (i.e. roughly 10 per cent of the 667 − 191 = 476 M1 systems that remained after the exclusion of planets that might have experienced planet-star circularization) have such low eccentricities that they should be moved to multiplicities that might exceed $M_{\text{max}}$ (in some cases more than 50 planets). It was therefore assumed that these systems might not contain undiscovered planets, but that other physical mechanisms were responsible for circularizing these 10 per cent. For the proceeding estimates, have in mind that the effect of keeping these 50 planets would be to slightly increase the estimated abundance of M1 systems and decrease correspondingly the abundance of high multiplicity systems like our own Solar system. Non-planet–planet interacting mechanisms that could be responsible for circularization of a fraction of this amount of M1 systems could include migration of a single large planet to small orbit while substantial amount of the protoplanetary disc was still in place (Hjort 2019).

For those of the remaining group of (667 − 191 − 50 = 426) M1 systems with eccentricities that potentially could be attributed to yet undiscovered planets, we attempted a redistribution of the systems by artificially counting them as belonging to higher values of $M$. The new multiplicity, $M_{\text{new}}$, was determined from the eccentricity of the planet using equation (1). A total of 164 M1 systems were redistributed and the new multiplicity distribution can be seen in Table 4.

In addition to the number of systems within each multiplicity bin, Table 4 also shows the percentage and probability distributions for the redistributed planets. The probability distribution is found by fitting an exponential fit to the percentage distribution as shown in Fig. 2 and explained later.

The redistribution of the M1 systems has been made such that the mean eccentricity of the remaining 262 systems falls on the same relation as the rest of the multiplicity systems described by equation (1). For the sake of this experiment, we assume that these remaining M1 systems would be the intrinsic M1 population among the observed systems, with no additional undiscovered planets and whose eccentricity is determined by the same planet–planet interactions as the multiplanet systems. In this sense one can think of the relation given by equation (1) applied to all the systems from M1 to $M_{\text{max}}$ as giving a minimum abundance of M1 systems and corresponding maximum abundance of high multiplicity systems. We stress this fact because it for many might seem intuitively (for example based on the antropic principle) surprising that our Solar system belongs to such a relatively rare type of planetary systems as predicted from equation (1) and shown in Fig. 5; without the redistribution suggested above, the Solar system would be predicted to be of an even more rare type of planetary system.

Eccentricity–multiplicity correlation
The average number of planets in planetary systems, according to the distribution in Table 4, is $\langle M \rangle = 2.48$, and is marked by a diamond in the figure. Based on the discrete probability distribution in equation (3) the probability of a system having eight planets is $P(8) \approx 1$ per cent, indicating that systems the size of the Solar system are rare but not exceptionally so. In this interpretation the Solar system is in the tail of a distribution of multiplicity, and corresponding orbital eccentricities, near the maximum possible from stability considerations. We have in the above summation assumed that the maximum cut-off is near to $M_{\text{max}} = 10$ planets, but we note that the exact value of $M_{\text{max}}$ is unimportant for the conclusion, since the integral of equation (3) from 8 to infinity is very small. Remark also that the number 1 per cent refers to the fraction of the systems that have had their eccentricities determined by planet–planet interaction, or a similar process that is responsible for equations (1) and (3). If one is counting also the M1 planets that were excluded in deriving equation (3), then the probability of finding 8 planets would be slightly lower. It should be noted that all results in this analysis rely on the assumption that the power law in equation (1) describes the true intrinsic correlation between eccentricity and multiplicity. The redistribution was based on a correlation fitted to the observed multiplanet systems. The fact that some of these multiplanet systems might host yet undiscovered planets could therefore pose a uncertainty to the analysis. However, theoretical studies have found that the observed M1 population is the only one that differ greatly from the theoretical predictions (Johansen et al. 2012). As mentioned previously, some have suggested that this is caused by the fact that the observed M1 systems are especially prone to containing undiscovered planets (He et al. 2020). As such, the analysis should not be affected greatly by undiscovered planets in the multiplanet systems. As mentioned previously planet-star interaction has not been taken into account when making equation (1). If the planets from the multiplanet systems that might have experienced planet-star interaction had been excluded in equation (1), the mean multiplicity would have been 2.6 rather than 2.5 planets per system.

It is encouraging to note that Jurić & Tremaine (2008b) found the average number of planets to be between 1.8 and 3.0 planets per system from a series of individual simulations with different initial planetesimal conditions, and that Raymond, Izidoro & Morbidelli (2018) found the probability of forming planetary systems with a number of planets similar to our own to be $\sim 1$ per cent based on dynamical arguments. Both results are very similar to our result but based on completely different and independent arguments.

5 DISCUSSION

We find an anticorrelation between orbital eccentricity and multiplicity of known exoplanet systems similar to the reports by previous studies (Limbach & Turner 2015; Zinzi & Turrini 2017). Our planet sample and method differ from the investigation by Limbach & Turner (2015) by including planets discovered by all detection methods, not just RV, and from both studies by including a much larger data set and by comparing the results obtained based on different data bases with different selection criteria. In addition we have chosen to consider systems as units unlike the previous studies, which treated each planet separately. When comparing our investigation to the previous ones, it should be noted that we, of course, share a great part of our data sample, and although the larger data set in our analysis has allowed for a more restrictive debias process, all our analyses are biased by the basic limitation by the RV technique (biased towards larger planets), and the transit technique (biased towards ultrasmall orbits).

The fact that we include all planets regardless of detection methods has shown us that similar eccentricity–multiplicity correlations can be found for the full sample, and RV- and transit subsamples respectively, though with slightly different fits as discussed above. Explicitly, we also studied the eccentricity–multiplicity correlation for subsamples of hot-Jupiters, cold-Jupiters, and super-Earths separately, and found that also these subsamples followed the same general tendency. This shows that the correlation is not solely caused by the giant planets, that currently dominate our observations, or by planets at very short periods, but might also apply to the population of planets that have yet to be observed, with smaller masses and at larger periods.

A correlation between orbit eccentricity and multiplicity is supported by several other studies. Surveys conducted by Howard (2013) and Wright et al. (2009) found lower orbit eccentricities among planets in multiplanet systems compared to single planets. Howard (2013) suggests that the trend could be due to severe planet–planet scattering in the existing single-planet systems where giant planets have excited the eccentricities of its previous companions before ejecting them. Multiplanet systems have had fewer scattering events (otherwise they would no longer be multiplanet) and have thereby been allowed to stay in stable low-eccentricity orbits. Wright et al. (2009) argues that multiplanet systems will naturally favour low-eccentricity orbits because of the need for high orbital stability in the system. The stability of multiplanet systems was studied further by Huang, Petrovich & Deibert (2017), who found that a single outer high-eccentricity giant planet would greatly affect the stability of an inner system, by reducing the multiplicity and exciting the eccentricities of the remaining planets. Both Wright et al. (2009) and Chatterjee et al. (2008) support the theory of single high-eccentric planets as a result of ejecting companions. The ejection of planets from planetary systems have been confirmed by Mróz et al. (2017), who from analysis of short-duration events in 6 yr of microlensing data have found free floating planets of both Jupiter- and Earth-size, although they also conclude that the abundance of free floating planets is small, and can therefore only account for the eccentricity of a small fraction of the M1 systems. A study by Xie et al. (2016) have also reported lower eccentricities in multiplanet systems. This study measured the eccentricity distribution of a sample of transit planets using transit duration statistics, and found that single-planets in general show eccentricities of $e \approx 0.3$, whereas their multiplanet counterparts have average eccentricities of $e \approx 0.04$. Xie et al. (2016) found all planets from multiplanet systems to follow similar eccentricity distributions, and so, found no general correlation between eccentricity and multiplicity.

Several studies have suggested that the correlation between eccentricity and multiplicity originates in an underlying correlation between multiplicity on the stability of the system, or the AMD (Laskar & Petit 2017; He et al. 2020; Turrini et al. 2020). In their study, He et al. (2020) recreate the multiplicity distribution observed at the Kepler data, using a forward model, by looking at the AMD-stability limit. They find that the median eccentricities as a function of multiplicity follow a power-law correlation for all multiplicities from one to ten. Their model predicts that intrinsic single-planet systems have higher eccentricities than multiplanet systems, whereas most observed single-planet systems contain yet undiscovered planets, similar to our assumptions in Section 4. Like previous studies He et al. (2020) argued that the correlation between intrinsic multiplicity and the eccentricity of the systems was caused by the fact that the AMD-stability criteria puts strong demands on the total system AMD and minimum system period ratio, in order for no planet orbits to cross, and thereby destabilizing the system.
The eccentricity–multiplicity anticorrelation is opposed by Bryan et al. (2016) and Dong, Katz & Socrates (2014), who found lower eccentricities among single planets compared to planets with outer companions. Both surveys mainly focus on jovian planets, Dong et al. solely on warm-Jupiters with jovian companions. Dong et al. (2014) suggest that their results indicate that planet–planet interactions are not the dominating mechanism for creating short-period jovian planets, as opposed to the suggestions by several other studies (Rasio & Ford 1996; Marzari & Weidenschilling 2002; Chatterjee et al. 2008; Nagasawa, Ida & Bessho 2008).

As argued by Bryan et al. (2016) a significant uncertainty is involved with the investigation by Limbach & Turner (2015) and some of this apply to our study as well. Many planets included have small semimajor axes (the majority within 1 AU), and the low eccentricities found in high-multiplicity systems might reflect the fact that systems this closely packed would not be able to remain stable at higher eccentricities. With our larger data sample we have found similar correlations between RV- and transit subsamples which lowers the probability that the correlation is caused by observational biases. Bryan et al. (2016) further emphasize the uncertainty related to the fact that Limbach & Turner (2015) do not account for the individual errors of each of the listed eccentricities, which could also pose an uncertainty for this study.

Since we have not included the listed uncertainties to the eccentricities of each individual planet, we have not accounted for the uncertainty involved with the estimation of orbit eccentricity of exoplanets. In addition to this, previous studies have found that many eccentricities are systematically overestimated (Shen & Turner 2008), and that some seemingly high-eccentricity single planets can turn out to have an unknown outer companion that artificially increase their estimated eccentricity (Fischer et al. 2001). The latter, fits our eccentricity–multiplicity correlation, with a decrease in eccentricity for an increasing number of known planets, it does however represent an uncertainty to our calculated model.

Unlike this study, the study by Zinzi & Turrini (2017) did account for the uncertainties related to the eccentricity measurements. When calculating the mean eccentricities, Zinzi & Turrini (2017) weighted their data with one over the listed uncertainties, which resulted in a steeper curve for the power-law correlation compared to unweighted data. Especially the M2 systems seemed to differ between the weighted and unweighted data by having a significantly higher mean eccentricity in the weighted sample. They did not give an explanation as to why the low-eccentricity M2 planets should have generally higher uncertainties. In this study we find that the M2 systems have eccentricities that fit the general eccentricity multiplicity correlation for $M > 1$ without correction for the uncertainties. In our analysis only the M1 systems falls substantially below the power-law fit, but since no M1 systems were included in the analysis by Zinzi & Turrini (2017) we are not able to compare this trend to their results.

## 6 CONCLUSION

During this study we have investigated the correlation between orbital eccentricity and multiplicity for 1171 planets distributed in 895 systems listed in the data base exoplanet.eu. We found a strong correlation between average eccentricity and multiplicity for all systems with two or more planets, which could be expressed as $e(M) = 0.429 \cdot M^{-0.93}$ (equation 1). The Solar system fits this trend, without being included in the making of the power law, whereas the average eccentricity of the observed M1 systems were markedly lower than predicted from equation (1). It is not unexpected from standard core accretion theory that the M2 to $M_{\text{max}}$ systems fit the same power-law distribution, but it is surprising that the M1 systems fall substantially below the correlation. The eccentricity–multiplicity anticorrelation is investigated for the number of different subsamples, in order to explore the stability of the power-law correlation, and investigate possible explanations for the deviating M1 average eccentricity. All subsamples show the same general pattern, with all multiplicities fitting a power-law correlation well, except the M1 systems having consistently lower eccentricities. The analysed subsamples include: different planet populations (divided into hot-Jupiter-, cold-Jupiter-, and super-Earth systems), planets detected by the RV- or transit method respectively, etc.

In order to investigate some of the implications of the power-law trend, we speculated on the potential consequences, if the trend that was found for $M > 1$, in reality applies to all multiplicities. Following the idea that equation (1) describes the true eccentricity–multiplicity correlation, we assumed that the seemingly low eccentricities of the M1 systems were caused by a combination of some systems having been circularized through planet-star interactions, and others containing yet undiscovered planets. Correcting for these assumptions, a probability distribution over the different multiplicities was expressed by equation (3), and based on this the mean multiplicity among the observed systems was estimated to $\langle M \rangle \approx 2.5$, while the probability of a system having eight planets was $\sim 1$ per cent.

It is not surprising that the probability of finding high-multiplicity systems comes out this low, after all there are very few known exoplanetary systems with more than six planets, but it is assuring that the average number of planets in a ‘standard’ exoplanet system in our Galaxy comes out very close to the number predicted independently from numerical simulations of planetesimal collisions (Jurić & Tremaine 2008b) and that the probability of finding Solar-system-like multiplanet systems comes out close to recent independent predictions from dynamical simulations (Raymond et al. 2018). This indicates that the orbit eccentricities of the Solar system planets are not unusually low, when the multiplicity of the system is taken into account, but rather that the number of planets in our Solar system is unusually high. The rarity of the large number of planets in our Solar system, and the corresponding low value of the orbital eccentricities, raise the simple and central, but speculative, question ‘Is there a connection between the high number of planets in our Solar system and the fact that we are here?’.

## ACKNOWLEDGEMENTS

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## DATA AVAILABILITY

The data underlying this article are available in The Extrasolar Planets Encyclopaedia, at http://exoplanet.eu/catalog/.