HORIZON-AGN virtual observatory-2. Template-free estimates of galaxy properties from colours


Published in: Monthly Notices of the Royal Astronomical Society

DOI: 10.1093/mnras/stz2486

Publication date: 2019

Document version: Publisher's PDF, also known as Version of record

Document license: CC BY-NG

Citation for published version (APA):
HORIZON-AGN virtual observatory – 2. Template-free estimates of galaxy properties from colours


1 IPAC, Mail Code 314-6, California Institute of Technology, 1200 East California Boulevard, Pasadena, CA 91125, USA
2 Cosmic Dawn Centre (DAWN), Niels Bohr Institute, University of Copenhagen, Juliane Maries vej 30, DK-2100 Copenhagen, Denmark
3 Sub-department of Astrophysics, University of Oxford, Keble Road, Oxford OX1 3RH, UK
4 Aix Marseille University, CNRS, CNES, LAM, Jardin du Pharo, 58 Boulevard Charles Livon, F-13007 Marseille, France
5 Jet Propulsion Laboratory, California Institute of Technology, Pasadena, CA 91109, USA
6 Department of Astronomy, University of Geneva, ch. d’Ecogia 16, CH-1290 Versoix, Switzerland
7 Sorbonne Universités, CNRS, UMR 7095, Institut d’Astrophysique de Paris, 98 bis bd Arago, F-75014 Paris, France
8 Department of Physics, ETH Zürich, Wolfgang-Pauli-strasse 27, CH-8093 Zürich, Switzerland
9 Korea Institute for Advanced Study (KIAS), 85 Hoegiro, Dongdaemun-gu, Seoul 02455, Republic of Korea

Accepted 2019 September 2. Received 2019 August 20; in original form 2019 May 30

ABSTRACT

Using the HORIZON-AGN hydrodynamical simulation and self-organizing maps (SOMs), we show how to compress the complex, high-dimensional data structure of a simulation into a 2D grid, which greatly facilitates the analysis of how galaxy observables are connected to intrinsic properties. We first verify the tight correlation between the observed 0.3–5 μm broadband colours of HORIZON-AGN galaxies and their high-resolution spectra. The correlation is found to extend to physical properties such as redshift, stellar mass, and star formation rate (SFR). This direct mapping from colour to physical parameter space still works after including photometric uncertainties that mimic the COSMOS survey. We then label the SOM grid with a simulated calibration sample to estimate redshift and SFR for COSMOS-like galaxies up to z ~ 3. In comparison to state-of-the-art techniques based on synthetic templates, our method is comparable in performance but less biased at estimating redshifts, and significantly better at predicting SFRs. In particular, our ‘data-driven’ approach, in contrast to model libraries, intrinsically allows for the complexity of galaxy formation and can handle sample biases. We advocate that observations to calibrate this method should be one of the goals of next-generation galaxy surveys.

Key words: methods: data analysis – methods: statistical – galaxies: evolution – galaxies: fundamental parameters.

1 INTRODUCTION

One of the most successful techniques to understand galaxy formation is measuring galaxy properties in large-area surveys and comparing the results with cosmological-scale simulations based on theoretical models of galaxy formation. Typically, the comparison is done in physical parameter space, so secure estimates of redshift, luminosity (L), stellar mass (M), star formation rate (SFR) must be obtained from observational data. These estimates usually come from the analysis of the spectral energy distribution (SED) or the high-resolution spectrum of galaxies, relying on the correlation between specific wavelengths and physical properties: for example Hα emission and star formation (Kennicutt 1998) or ~2 μm light and stellar mass (Madau, Pozzetti & Dickinson 1998). In the past two decades, the data from multiwavelength photometry and spectroscopic surveys have become abundant, and fitting galaxy templates to observed SED and spectra is now the standard method to perform this analysis (among the pioneering studies: Sawicki & Yee 1998; Bell & de Jong 2000; Gavazzi et al. 2002; Pérez-González et al. 2003; Fontana et al. 2004; Gallazzi et al. 2005). Galaxy parameters are usually derived from the maximum-likelihood template (Bolzonella, Miralles & Pelló 2000) or from the full probability distribution function (PDF) of the template set (Benitez 2000). For quantities like stellar mass or star formation history (SFH), templates are built from stellar population synthesis...
The modelling process often introduces systematic effects that have been shown to severely bias M and SFR estimates in some cases (e.g. Mitchell et al. 2013; Mobasher et al. 2015; Laigle et al. 2019). For instance, the synthetic templates are not guaranteed to have fully realistic features; e.g. their SFH is often an analytically function (as the τ- and inverted-τ models, see Maraston et al. 2010) that does not include either multiple bursts or chemical enrichment. Discrepancy between synthetic templates and real galaxies is also due to the assumptions about their stellar population initial mass function (IMF) and dust attenuation of their stellar light (e.g. Davidzon et al. 2013). Moreover, templates not always take into account nebular emission lines, which may contaminate the observed broad-band photometric colours. Finally, some galaxy types may not even be included in the library (e.g. the old and dusty galaxies at z ≃ 2–3 discussed in Marchesini et al. 2010).

Beyond modelling problems, there are additional systematics introduced by the fitting procedure. The relative abundance of a given SED in the real universe is often not accounted in the synthetic library: most of the fitting codes assume that all templates are equally likely. Moreover, the SED-fitting (or spectral) algorithms may not treat the template set in an optimal way, as they often rely on computationally expensive brute-force approaches to explore the entire library (see Speagle et al. 2016) or they may introduce systematics when convolving templates with instrumental errors (see Cappellari 2017). These uncertainties all propagate into the commonly used statistical descriptors of a galaxy census, such as the galaxy stellar mass function (Ilbert et al. 2013; Grazian et al. 2015) and the specific SFR evolution of star-forming galaxies (Santini et al. 2017; Davidzon et al. 2018). Ultimately, all of these uncertainties combine to result in a biased view of galaxy demographics, preventing a clear and straightforward comparison between observations and simulations.

To make such a comparison more robust, significant effort has been devoted to improving template fitting techniques. To date, substantial progress has been achieved in each step of the computation, from the construction of galaxy models with more complex SFHs (Pacifici et al. 2013) to improved radiative transfer modes including the interstellar medium (da Cunha, Charlot & Elbaz 2008) and sophisticated Bayesian fitting techniques (Chevallard & Charlot 2016; Leja et al. 2017).

In parallel to this ongoing effort, other authors have explored alternate paths, replacing standard template fitting with new techniques based on machine learning (ML). Besides implicitly accounting for biases, a key advantage of ML techniques is indeed their speed, which enables analyses of extremely large data sets. Most of the existing work aims at estimating redshifts (see Salvato, Ilbert & Hoyle 2019, and references therein), with the exception of a few publications where ML has been applied, e.g. to recover SFR (Delli Veneri et al. 2019) and specific SFR (Stensbo-Smidt et al. 2017) of z ≃ 0 galaxies from the Sloan Digital Sky Survey (SDSS). A wider range of galaxy parameters (including stellar mass and metallicity) is estimated in Simet et al. (2019). That study, complementary to ours, uses a supervised neural network trained with a semi-analytic model simulation.

In this work, we describe a novel technique based on unsupervised ML combined with analytic data modelling, to simultaneously provide redshift and SFR estimates for galaxies across a large redshift range (0 < z < 3, spanning about 12 Gyr of universe’s life). The ML algorithm adopted here is the self-organizing map (SOM; Kohonen 1981), which is an unsupervised manifold learning algorithm used to analyse high-dimensional data (see also Kohonen 2001). Initially popular in engineering research, it soon circulated to many other fields including Astrophysics. Seminal work has used the SOM mainly to classify astronomical objects and their properties, including stellar populations (Hernandez-Pajares & Floris 1994), star versus galaxy separation (Maehoenen & Hakala 1995; Miller & Cee 1996), and morphological types (Molinari & Smareglia 1998). Since it does not require the manifold to have physical meaning, the SOM has also been used to classify astronomical publications (Poincôt, Lesteven & Murtagh 1998). More recently, the SOM has been applied to calibrating redshifts for weak lensing cosmology (Masters et al. 2015). Other recent studies using the SOM will be mentioned throughout this work.

As other ML methods, the SOM starts with a training phase. However, unlike supervised methods, the goal of the training is to create a compressed, lower dimensional representation of the data rather than estimate an output. In this work, we first perform the training on galaxy colours drawn from the HORIZON-AGN simulation. We then label the SOM with galaxy properties not learned during the training phase. These labels can be drawn from a data model based either on simulations or, as suggested later, bona fide galaxies observed as reference for calibration. Since the mapping from the data to the labels is explicit and analytic, control over selection functions, sample biases, and the effects of observational noise is retained (unlike supervised ML where these factors are part of the learning scheme).

In this paper, we focus on galaxy SFR estimates because they are fundamental to constraining galaxy evolution (Madau & Dickinson 2014) along with stellar mass measurements. However, compared to the latter, the SFR estimates from template fitting are much more uncertain: previous work (e.g. Laigle et al. 2019) shows that SFR is more sensitive than stellar mass to SED-fitting assumptions. This sensitivity is inherent to relying on the ultraviolet (UV) continuum as a star formation indicator because it is highly attenuated by dust, geometry dependent, and also sensitive on the details of SFH. Other techniques offer better performance by using either far-infrared (FIR) data (≥24 μm, Le Floc’h et al. 2009; da Cunha et al. 2008) or spectroscopic follow-up (Kennicutt 1998; Kewley, Geller & Jansen 2004), which is expensive and impractical to obtain for every galaxy. Therefore, we focus this study on estimating SFR from the rest-frame UV to near-IR (NIR) photometry, leaving the details of other physical properties to future work.

To test and develop our ML method, we use a mock galaxy catalogue of ~8 × 10^5 objects extracted from the cosmological hydrodynamical simulation HORIZON-AGN (Dubois et al. 2014); the mock catalogue was presented in Laigle et al. (2019, hereafter Paper I) as the first milestone of the HORIZON-AGN virtual observatory project. One of the main goals of the project is to bridge the divide between empirical and theoretical studies by adding observational-like features to simulated galaxy samples. To this purpose, we produced mock catalogues with characteristics similar to the COSMOS survey (Scoville et al. 2007) and Euclid (as predicted in Laureijs et al. 2011). By applying our SOM estimator to the COSMOS-like version of the HORIZON-AGN galaxies, we aim to demonstrate its feasibility for real data sets. Both the simulated data set and the SOM are described in Section 2.

Building on this result, in Section 4 we introduce the SOM-based estimator of redshift and SFR, and apply it to the COSMOS-like mock catalogue. In Section 5, we show that redshift and SFR must be known for only a subset of galaxies in order to ‘calibrate’ the SOM estimator and provide estimates without a synthetic template.
library. We then discuss possible ways to build such a calibration sample, inspired by previous work proposing a highly complete spectroscopic follow-up in large cosmological surveys (Masters et al. 2015; Hemmati et al. 2019b). To show the improvement of template-free ML with respect to standard fitting techniques, Section 5 ends with a comparison between SOM estimates versus the SFR derived in Paper I for the same galaxies by means of the code LEPHARE (Arnouts et al. 1999; Ilbert et al. 2006). We discuss the results and draw our conclusion in Section 6.

Throughout this work, we use a flat lambda cold dark matter cosmology with $H_0 = 70.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.272$, $\Omega_{\Lambda} = 0.728$, and $n_s = 0.967$ (Komatsu et al. 2011, WMAP-7). All magnitudes are in the AB (Oke 1974) system. The IMF is as in Chabrier (2003).

2 DATA AND METHODS

2.1 The HORIZON-AGN virtual observatory

This study relies on a mock galaxy catalogue built from the HORIZON-AGN hydrodynamical simulation1 (Dubois et al. 2014). This catalogue, presented in Paper I, includes 789 354 galaxies extracted from a $1 \times 1 \text{deg}^2$ light-cone by running the ADAPTAHOP halo finder (Aubert, Pichon & Colombi 2004) on the stellar particle distribution. Each stellar particle (of mass $\sim 2 \times 10^4 \text{M}_\odot$) is linked to a synthetic simple stellar population (Bruzual & Charlot 2003, redshift $2 < z < 4$). The upper limit in redshift is imposed to work with galaxy colours consistently defined across the whole redshift range, i.e. avoiding non-detection in the $u$ band due to the Lyman limit shifting into the band.

Our virtual observatory mimics the optical and NIR photometry of COSMOS2015 galaxies (Laigle et al. 2016) in 10 broad-bands ($u, B, V, r, i^+, z^+, Y, J, H, K_s$) and 14 medium-band filters (from Subaru/SuprimeCam, see Taniguchi et al. 2007). It also includes the Spitzer/IRAC channels centred at 3.6 and 4.5 $\mu$m (hereafter [3.6] and [4.5]). In each filter, we reproduce the signal-to-noise ratio (S/N) distribution as in the ‘ultra-deep’ stripes of COSMOS2015. Reference 3σ limits (in 3 arcsec apertures) used in previous work are $K_s < 24.7$ and $i^+ < 26.2$ (for a list of sensitivity depths in every filter, see table 1 in Laigle et al. 2016). After introducing such uncertainties, we perturb the original galaxy fluxes accordingly. Attenuation by dust and inter-galactic medium is also taken into account, whereas flux contamination by nebular emission is not implemented. In the following, we refer to the attenuated fluxes without photometric errors as intrinsic, while perturbed photometry is the one that takes into account galaxy S/N.

Further details about the realization of the HORIZON-AGN mock galaxy catalogue can be found in Paper I and Appendix A1 (see Online Supplementary Materials). We also use a simpler (‘phenomenological’) simulation to show that neither the Horizon-AGN limit in stellar mass nor the absence of nebular emission lines affect our main results (Appendix A2).

---

1http://www.horizon-simulation.org/  
2Cosmological redshifts ($z_{\text{sim}}$) in our light-cone include galaxies’ peculiar velocity.

2.2 The SOMs

In brief, an SOM represents a high-dimensional data distribution into fewer dimensions (e.g. a 2D space) through an unsupervised neural network that preserves topology. In other words, objects that are multidimensional neighbours remain close to each other also in the 2D space.

Assume that the original (compact) space $M$ with dimensions equal to $M$, has to be reduced into a space $N$, which we choose to be bi-dimensional ($N = 2$). To build the SOM, we create a neural network where each neuron is associated with a weight vector $\hat{\omega}$. Each element in these vectors comes from the corresponding dimension of $M$ (i.e. $\hat{\omega}$ has length $M$). Neurons (and the vectors attached to them) are ordered in the $N$-dimensional configuration defined by the user, for instance a rectangular lattice (see a pedagogical example in Fig. 1).

The SOM relies on a training sample of objects drawn from $M$. The neural network explores $M$ by adapting neurons’ weights to the training sample. Such a learning phase proceeds by iteration until the value of each weight gets as close as possible (according to a convergence criterion) to the input data. The first task in the procedure is to find the best-matching unit for any given data point ($\hat{x}$) of the training sample. The best-matching unit is the neuron whose weight $\hat{\omega}_0$ is the closest from $\hat{x}$. Then, the weight of each neuron (including the best-matching unit) is updated during an iterative process:

$$\hat{\omega}_i(t+1) = \hat{\omega}_i(t) + \alpha(t) \phi(\hat{\omega}_i, \hat{\omega}_0, t) [\hat{x} - \hat{\omega}_i(t)].$$

Equation (1) is written for the $i$-th neuron, updated from step $t$ to $t + 1$. The learning coefficient $\alpha$ is a monotonically decreasing function to ensure convergence, while $\phi$ is a neighbourhood function that modulates the update depending on the distance between the $i$-th neuron and the best-matching unit: $\phi \propto \exp(-(\hat{x} - \hat{\omega}_i, \hat{x} - \hat{\omega}_0))$. The procedure is repeated by scanning the other elements of the training sample. It is critical to use a training sample that is representative of the whole space, otherwise the grid of neurons/weights is adjusted to probe only a subset of $M$.

The learning process is unsupervised because it does not require the training sample to be labelled a priori. Neurons autonomously organize their weights: hence the name ‘self-organizing’ map. The resulting SOM is a mapping function that connects a point from $M$ to $N$ and vice versa. We stress out that the topology is preserved so that in the low-dimensional configuration (the 2D lattice in our example) two adjacent weights are linked to nearby regions of $M$.

In our case, the high-dimensional space is the typical baseline of an extragalactic survey, i.e. each dimension is a colour measured from broad-band filters (for example $u - g, g - r$, etc.). The training sample is a set of galaxies large enough to span the colour distributions observed in the universe. We specifically explore the panchromatic space because there is a straightforward connection to the physics of galaxy evolution we aim at studying.3 We choose a rectangular lattice to order the neurons. Because of its appearance, and to maintain the same lexicon of previous work, hereafter we refer to...
Figure 1. Pedagogical representation of the SOM using an artificial distribution of 2000 objects in an unspecified 3D space. Upper panel: After setting a 10 × 10 grid of ‘cells’, the algorithm adapts the grid (black lines) to the manifold of the training objects (magenta points). Here, as well as in the next figures, SOM axes are labelled with conventional names $D_1$ and $D_2$. The grid becomes finer where the density of the training sample is higher, while sparse objects in the outskirts will be linked to the border of the grid. Features $C_1$, $C_2$, $C_3$ can be regarded as three galaxy colours, but in principle they can be to any feature. Lower panels: The SOM as it appears in the 2D space, with a different layout in the three panels. The 2000 training objects (small dots) have been allocated into the 10 × 10 grid (their position within a cell has been scattered for illustrative purposes). In each panel, objects are colour coded according to one of their features ($C_1$, $C_2$, $C_3$ from left to right). Similar objects are clustered in the same (or nearby) cell and a smooth transition is observed across the grid. Outliers with extreme characteristics (e.g. $C_3 > 4$) are pushed to the grid corners. In this example, we use a simple distribution of data points for illustrative purposes. As a consequence, the SOM grid is a ‘simple’ 3D surface. In general, the grid can assume more complex high-dimensional configurations. Thanks to this property, the SOM and similar non-linear dimensionality reduction algorithms can accurately map the parameter space of real galaxies (which are a non-linear manifold). This is also a key difference from PCA, which can only assume a hyper-surface.

will refer to the neurons as ‘cells’ in a 2D ‘grid’ (Fig. 1). Each cell is defined by its weight vector, for example $\hat{w}_{ij}$ for the cell with coordinate $i, j$ in the grid. The weight connects its cell to a point in the panchromatic space, i.e. the vector components $(w_{ij,1}, \ldots, w_{ij,M})$ now represent a set of colours. The terminology used to describe the SOM is summarized in Table 1.

To follow Kohonen’s prescriptions – i.e. to find the best-matching units and implement equation (1) – the distance between weights and galaxies is computed assuming Euclidean metrics:

$$d_{ij} = \sqrt{\sum_{m=1}^{M} (C_m - w_{ij,m})^2},$$

(2)

where the given galaxy is defined by the colour vector $\hat{C} = (C_1, C_2, \ldots, C_M)$. The total $i \times j$ number of cells/weights is chosen by the user (see Section 3). As a result, each SOM cell ‘contains’ one or more galaxies from the training sample, whose colours are similar to the weight vector of that cell. The galaxy–cell association determined during the training phase is performed by the Python software SOMPY. Before the iterative process, to start with weights that are already close to the galaxy distribution, each weight vector is initialized by setting its colours via principal component analysis (PCA; Chatfield & Collins 1980) of the training sample. A parallelism between these weights and PCA eigenvectors can help understanding the SOM: its weights can be thought as a set of characteristic SEDs that describe the panchromatic space. However, the SOM has important differences from a PCA (see

\(^5\)It should be noticed that in our SOM implementation input data will be normalized in each dimension, rescaling the distribution to unit variance and centring the mean at zero.

\(^6\)https://github.com/sevamoo/SOMPY
Section 3.3). In particular, PCA is a linear hyper-surface defined by principle components, so it cannot fully describe a non-linear manifold, which is what we expect the galaxy colour space to be.

Once the SOM is trained, new galaxies can be mapped on to the grid by finding the nearest weight vector to each of them through equation (2). Moreover, the grid can be labelled a posteriori by looking to another galaxy property not included in the parameter space. For example, one can consider the redshift distribution of galaxies within a given cell and take their median \( \langle z \rangle \) cell to label that cell. Such explicit labelling gives our method a key advantage over supervised ML because we keep control of the relationship between features (the broad-band colours) and labels (the redshift in the example above). This means that if we have a model of the bias or errors in our data, we can directly account for that. However, it also means that an additional calibration phase is required to make the SOM work as an effective galaxy estimator. Indeed, as we will highlight in the following, galaxies clustered together in the colour space also share other (physical) properties.

### 3 SOM of HORIZON-AGN Galaxies

We apply the procedure summarized in Section 2.2 using HORIZON-AGN galaxies as a training sample. The considered features are their broad-band colours \( u - B, B - V, V - r, r - i^*, i^* - z^{++}, z^{++} - Y, Y - J, J - H, H - K_s, K_s - [3.6], \) and \([3.6] - [4.5] \). Except for the Subaru intermediate-band filters, which are not included here, this is the same baseline used in Paper I. As the SOM projects that 11-dimensional space into a rectangular grid (likewise Fig. 1), we can explore galaxy physical parameters as a function of their 2D position, to see whether training objects located in the same cell have in common other properties besides their broad-band colours. It should be noticed that a galaxy not detected in any of the filters poses a challenge to the SOM as one colour would be ill-defined. This is a common problem in ML methods that will be addressed in Section 4.

In the present section, we consider intrinsic colours (i.e. not affected by photometric noise) unless specified otherwise. The results discussed here are instrumental to show the fundamental properties of our method and its full potential in the case of an ‘ideal’ survey. In Section 5, we will address the impact of observational uncertainties.

### 3.1 Generating an ideal SOM

Since we decided to adopt a rectangular lattice for the SOM, the first step is to decide its size and axial ratio.\(^7\) We set them by iteration, looking at changes in galaxy dispersion as a function of those two quantities (i.e. how tightly clustered are the galaxies associated with a given cell). We also check that the number of galaxies per cell is large enough to assure a good sampling in the various regions of the parameter space.

First, we test the optimal SOM size. Starting from a \( 20 \times 20 \) grid, we gradually increase the size by adding 10 cells in both dimensions (i.e. maintaining a ‘square’ configuration). Each time we train the SOM with the whole HORIZON-AGN catalogue and measure (i) the average distance of galaxies from their best-matching weight, (ii) the number of galaxies associated with each weight. The SOM converges fast with respect to (i), so that in grids of \( \geq 6000 \) cells most of the galaxies are tightly clustered in their cells, i.e. their distance from the weight in the colour space is smaller than the typical photometric errors in deep surveys like COSMOS (0.01–0.05 mag from optical to IR). On the other hand, the larger the grid of weights, the fewer the number of galaxies associated with each of them. With the \( 90 \times 90 \) configuration, a significant area of the SOM starts to be undersampled, with about 15 per cent of the cells defined by less than 20 galaxies each (Fig. 2, upper panel). Therefore, we identify a slightly smaller size (\( 80 \times 80 \) cells) as a good compromise between high resolution and sampling, also considering computational efficiency.

The next step is to define the best geometry for our SOM, namely the ratio between its axes. In the previous test, we used only square grids with increasing number of cells, while now we fix the number of cells to 6400 and modify the aspect of the grid from 1:5 ratio to 1:1 (i.e. the \( 80 \times 80 \) configuration) in eight steps. We describe again the quality of each SOM in terms of (i) and (ii), finding that the best configuration is that with 1:1 axial ratio (Fig. 2, lower panel). In a rectangular grid, there are more galaxies not well represented (i.e. far from their best-matching weight) especially when the two sides have very different lengths.

In conclusion, the SOM we will use throughout is made by \( 80 \times 80 \) cells. The result is specific for the HORIZON-AGN parameter space: the optimal configuration for another galaxy sample may be different. We notice none the less that the total number of cells is comparable to those used to describe the real COSMOS and CANDELS data sets, respectively, in Masters et al. (2015, 11 250 cells for galaxies up to z \( \sim 6 \)) and Hemmati et al. (2019b, 4800 up to z \( \sim 4 \)). An alternate method, proposed by Hemmati et al., consists in increasing the grid size until the histogram of each weight vector component matches the distribution of the corresponding colour (see their fig. 6). We calculate these histograms and find that indeed they converge when the grid dimension is \( \geq 80 \times 80 \).

### 3.2 Redshift calibration

After the training phase, we can label each SOM cell according to a given property of the galaxies contained in it. We compute the median redshift \( \langle z_{\text{sim}} \rangle \) cell and the relative scatter \( \sigma \) defined as \( \sigma = \langle z_{\text{sim}} \rangle - \langle z_{\text{sim}} \rangle \) cell. The SOM of HORIZON-AGN shows the same cell–z relationship found by Geach (2012) in COSMOS, with a smooth redshift evolution as moving across the 2D space (Fig. 3).

\(^7\) Other 2D configurations are possible, e.g. a lattice made by hexagonal cells or a spherical projection divided in HEALPix (see Carrasco Kind & Brunner 2014, for a comparison).
redshift scatter in every cell (not shown in the figure) is particularly small, with $\sigma_z$ always between 0.05 and 0.1. The small scatter is even more remarkable when the $\sigma_z$ values are divided by the $1 + z$ factor, shrinking to 0.01–0.03. This is due to the algorithm’s ability of clustering objects with very similar (observer’s frame) colours, which correspond to similar redshift. One may expect some redshift interlopers – i.e. objects with a significantly different $z_{\text{sim}}$ from the rest of the cell – due to SED degeneracies (Papovich, Dickinson & Ferguson 2001). However, we do not find this in the ideal case discussed here. On the other hand, we do observe boundary effects produced by galaxies with extreme colours, which lie at the limits of the panchromatic manifold (see also the example in Fig. 1). Those galaxies are pushed to the border of the grid, but with a negligible impact on the redshift distribution inside a cell (the redshift scatter remains modest: $\sigma_z \approx 0.1$).

In Fig. 3, we also observe a long horizontal stripe of empty cells. No galaxy has been associated with their $\hat{w}$ during the training. The $(z_{\text{sim}})^{\text{cell}}$ labels explain the physical meaning of this empty region: it is a ‘caustic’ in the parameter space dividing $z \sim 3$ galaxies from those at lower redshift with similar colours. Since we are working with intrinsic photometry, their Lyman versus Balmer break degeneracy (e.g. Stabenau, Connolly & Jain 2008) is fully disentangled.

### 3.3 High-resolution spectra in the SOM cells

In the HORIZON-AGN virtual observatory, the broad-band colours are integrated from high-resolution BC03 spectra, which are built accounting for complex SFH and chemical enrichment (Section 2.1).

In the SOM, we stack galaxy spectra from the same cell, re-normalizing them to a fixed $i^\ast$ flux to ease the comparison. Stacking is performed in the observer’s reference frame: spectra are redshifted to their $z_{\text{sim}}$ before adding them, to be consistent with the analogue procedure one would implement in a real survey.

The fact that the colour-based SOM can efficiently map redshifts (Section 3.2) does not necessarily imply that it performs as well with spectral features. Given the small amount of spectroscopic information in real data sets, previous work has only proven that broad-band SEDs are well clustered within the grid, with the exception of Rahmani, Teimoorinia & Barmby (2018) analysing 142 spectra at $0.5 < z < 1$ and Hemmati et al. (2019b) showing a handful of $z \sim 1$ spectra that have similar shape and are also clustered in nearby cells. We find that this is actually the case for the whole HORIZON-AGN sample: galaxy spectra are in excellent agreement in most of the cells (see a few examples in Fig. 4). Inspecting the regions close to the redshift caustic, we find more dispersion, mainly because the median stacking is performed in observer’s frame and therefore it is affected by the difference between individual redshifts. We check that spectral shapes are even more similar if the comparison is made in rest frame, removing the $\sigma_z$ scatter.

In addition to the examples shown in Fig. 4, we perform the same stacking analysis in 225 distinct cells evenly distributed across the
Manifold learning and galaxy properties

Figure 4. Median stacked spectrum (observer’s frame, red line) of galaxies in a given cell with relative inter-quartile dispersion (grey shaded area). The label at the top of each panel indicates number of galaxies and cell coordinates (see also the open circles in Fig. 3). Individual spectra are assumed to be ‘observed’ at $z_{\text{sim}}$ and then stacked, as one would do in a real survey. They have also been re-normalized to the arbitrary $i^+$-band flux of 22 mag.

grid, finding that their average inter-quartile dispersion is always $\lesssim 15$ per cent ($<8$ per cent in half of the cells probed). It is worth emphasizing the differences between this result and what a PCA classification would give. First of all, PCA provides a basis of eigenvector to be linearly combined, whereas the SOM works also with non-linear transformations. Each weight in the SOM has a clear physical meaning by itself, i.e. it describes a galaxy phenotype in the observed frame (Sánchez & Bernstein 2019). On the other hand, in a PCA classification, the 2–4 eigenspectra that usually have the most discriminating power are difficult to interpret. They can be combined to reproduce actual galaxy features, but classes for those resulting spectra are not inherently provided by the PCA and human intervention is required (e.g. defining meaningful regions in a Karhunen–Loève diagram, Marchetti et al. 2013).

The degree of similarity of the simulated spectra within a given SOM cell also depends on the complexity of their features. Spectra used in this work are extracted from the HORIZON-AGN and their realism and complexity are constrained by those of the simulation. Modelling galaxy evolution on cosmological scales is inevitably done at expenses of resolution. Because HORIZON-AGN maximum spatial resolution is at best 1 pkpc, the impact on the interstellar medium (ISM) of any process occurring at a smaller scale is averaged through subgrid recipes. These recipes have been iteratively improved in order to reproduce as well as possible the statistical distribution of integrated galaxy properties throughout cosmic time (in HORIZON-AGN such a progress can be tracked through Dubois et al. 2012, 2014; Park et al. 2019). However, they might fail to some extent at reproducing ISM inhomogeneity and clumpiness. As a result, we expect the SFH of our simulated galaxies to be smoother (and their spectra less diverse) than the real ones. As a consequence, the dispersion that we measured within an SOM cell must be considered as a lower limit. A more extended discussion about caveats in our modelling is provided in Appendix A1.

3.4 Exploring other physical parameters in the SOM

The remarkable similarity between spectra in the same cell suggests that those galaxies went through a similar evolutionary path, resulting, e.g. in the same mass-to-light ratio at the redshift of observation. HORIZON-AGN provides us with galaxy physical parameters such

---

8Those cells have coordinates $D_1 = 5i$ and $D_2 = 5j$, where $i$ and $j$ are integers ranging from 1 to 15.
Figure 5. The SOM trained with the intrinsic colours from the HORIZON-AGN catalogue is able to group galaxies with similar physical properties together in the same cell. Left: The SOM grid (same as Fig. 3) is now labelled according to the median mass-to-light ratio in each cell. The open circles mark three (randomly extracted) cells used as examples to show the tight correlation between position in the grid and physical properties. Right: Each row corresponds to one of the example cells marked in the left-hand panel and shows the logarithmic distribution of $M_{\text{sim}}/L_V$ (grey histogram), $M_{\text{sim}}$ (red histogram), and sSFR (cyan histogram) in that cell. In the case of the $M_{\text{sim}}$ distribution, individual values have been normalized to a common $i^+-\text{band}$ flux (corresponding to 22 mag) to show that the dispersion in a given cell is mainly due to the fact that the SOM, being trained with colours only, is not informed about the normalization of the SED.

as luminosity ($L$), stellar mass ($M_{\text{sim}}$), and star formation rate (SFR$_{\text{sim}}$). Thus, we can use our simulation to test whether the objects that are grouped together by the SOM have other properties in common besides their redshift. Regarding SFR$_{\text{sim}}$, this is defined by averaging galaxy SFH over the last 100 Myr, an interval comparable to the time-scale of SFR indicators widely used in the literature (Kennicutt & Evans 2012).

We calibrate the SOM to show the typical mass-to-light ratio per cell (Fig. 5, left-hand panel). The procedure is similar to the redshift calibration in Section 3.2, this time computing the median $\langle M_{\text{sim}}/L_V \rangle_{\text{cell}}$ with $L_V$ being the luminosity in the rest-frame $V$ band. In this way, we can visualize the variation of this quantity across the grid, which is also an evolution across redshift: more mature galaxies with larger $M/L$ occupy cells with lower $\langle z_{\text{sim}} \rangle_{\text{cell}}$ (cf. Fig. 3). We also aim at verifying that the scatter inside a given cell is small by calculating the difference between the 84th and 16th percentile in the logarithmic $M_{\text{sim}}/L_V$ distribution. We find that in most of the cells this is smaller than 0.2 dex. A few examples of the tight correlation between position in the grid and $M/L$ are shown in the histograms of Fig. 5.

A similar trend can also be observed regarding stellar mass after a scaling factor is applied. This factor is required since we do not train the SOM with information about SED normalization, as instead other authors do with different ML methods (Bonjean et al. 2019). This is the same procedure used in Fig. 4 to compare galaxy spectra, which have similar shapes but different magnitudes. Therefore, to analyse the intrinsic $M_{\text{sim}}$ scatter within a given cell, we first normalize each galaxy to a reference point of $i^+ = 22$ mag. In principle, this should be done in rest frame, given the fundamental

9We prefer working in a pure colour space because an additional dimension with a different dynamical range may not be properly weighed with respect to the others.
global evolutionary path of the galaxy, whereas the sSFR depends on recent fluctuations in the mass assembly history. The 0.2–0.5 dex dispersion in the SOM (Figs 5 and 6) reflects such a stochasticity: sSFR is also more sensitive than stellar mass to different levels of dust attenuation.

These tight correlations are obtained with an SOM trained with intrinsic colours: larger scatter is expected when galaxy photometry is affected by observational uncertainties. The results shown in this section can be considered as an ‘asymptotic’ limit represented by an ideal galaxy survey with infinite S/N. This ideal example can be approximated by the brightest galaxies in an ‘ultradeep’ survey. In that case, the S/N should be high enough to enable the SOM to classify galaxies not only with respect to their redshift, but also stellar mass and SFR. Such a clustering ability is the cornerstone of our original technique to recover stellar mass and SFR. In principle, knowing the stellar mass of a ‘calibration’ object ($M_{\text{cal}}$, which can be independently obtained via template fitting) one could get a fairly precise $M$ estimate for other galaxies mapped into the same cell: it would suffice to rescale $M_{\text{cal}}$ by the flux ratio between the known galaxy and the target one: $M \simeq M_{\text{cal}} \times (f_{\text{cal}}/f_{\text{obs}})$. As suggested by the examples in Fig. 5, in the best-case scenario, the uncertainty of such an estimate would be comparable to the typical mass errors of template fitting codes ($\lesssim 0.3$ dex, see e.g. Davidzon et al. 2017) with significant improvement in computational speed (about $10^6$ times faster according to Hemmati et al. 2019a).

The same argument used for stellar mass applies to SFR, which is not shown in Fig. 5 as it will be thoroughly discussed in the following. A flux re-normalization will be necessary as in the case of stellar mass. In the present analysis, we use the $i'$ band for the flux scaling factor since it has one of the deepest sensitivity limits. The $K_s$ band is a better proxy for stellar mass but in COSMOS2015 (and therefore in our COSMOS-like sample) its $3\sigma$ limit is $\sim 1.5$ mag shallower than $i'$ and would result in a larger scatter of the results (but still preserving the properties of the SOM, see Appendix A2).

## 4 A NOVEL ESTIMATOR OF GALAXY SFR

We concluded Section 3 by suggesting that the SOM can be used to empirically recover galaxy physical parameters in the same framework used in Masters et al. (2015) for photometric redshift computation. In this section, we discuss how to calibrate the SOM in order to derive SFRs from broad-band colours in a fast but accurate way. We focus on SFR since standard SED fitting shows its limit when deriving this quantity (see Paper I). One can obtain robust SFR estimates based on IR imaging or spectroscopy, but this is generally possible for a small fraction of galaxies (which indeed we can use as a calibration sample for our method). An SOM-based estimator for stellar masses should also be feasible, but it would likely be based on template fitting, at least for calibration purposes, given the current state of the art in estimating stellar mass. For template-based approaches, we refer the reader to Hemmati et al. (2019a) for an overview of how to effectively use the SOM. Here, our goal is to empirically calibrate properties based on direct indicators rather than depending on synthetic SDP libraries.

With this goal in mind, we devise a method that can be applied to real data, requiring some adjustment to the SOM. We replace the ideal (noiseless) photometry used in the previous section with a catalogue that mimics the COSMOS survey, including errors and selection functions. In other words, apparent magnitudes and colours of HORIZON-AGN galaxies are now perturbed with observational-like errors and selection effects. As a consequence, we use a different training sample, selecting only galaxies above a given S/N threshold. Thus, the observational-like training sample does not include objects that are not detected in some band. In Section 4.1, we show that, after the S/N selection, photometric errors do not impair the relationship between SOM cells and galaxy properties shown above.

In Section 4.2, we explain the details of our methods. In that context, we modify the way to label SOM cells. In fact, in the previous sections, we made calibrated versions of the SOM by labelling its cells with median values of either redshift or other physical parameters, i.e. under the assumption of knowing them for the whole sample. Hereafter, we assume to know the SFR of a small subset of 6400 galaxies (i.e. one object per cell) and use them to label the grid. At the moment, we do not make particular assumptions on how such a calibration sample is built; this is discussed later in Section 5 where we also compare to SFR estimates from template fitting.

### 4.1 The COSMOS-like SOM

The observational uncertainties to perturb the HORIZON-AGN photometry are statistical errors affecting apparent magnitudes so that our mock galaxy catalogue resembles the quality of the COSMOS data (see Paper I). For this reason, in the following we refer to the (noisy) HORIZON-AGN sample also with the term ‘COSMOS-like’, in contrast to the previous version with intrinsic photometry (Section 3). We do not model confusion noise and contamination by saturated stars; this kind of issues shall be addressed in future work after providing the HORIZON-AGN virtual observatory with simulated images.

The training phase of the implemented algorithm does not account for cases of non-detection (e.g. when the ‘observed’ flux is smaller than the flux error). Therefore, while working with perturbed photometry, we limit the analysis to a galaxy subsample with $S/N > 1.5$ in each broad-band filter. A statistically correct treatment of lower and upper limits in the input colours would require an improved SOM algorithm that is beyond the goal of this work. We also note that template fitting codes often neglect such a treatment (as highlighted in Sawicki 2012). The S/N pre-selection will restrict the analysis to $z \lesssim 3.5$ because galaxies at higher redshift are $i'$-band drop outs (Steidel et al. 1996) with $S/N < 1$ in that filter. Given the sensitivity of our catalogue the S/N threshold roughly corresponds to a flux-limited survey with a cut at $i' < 25$ (see fig. B1 in the Online Supplementary Materials). Besides the removal of $z > 3.5$ galaxies from the sample, there are other caveats in the S/N selection, which are listed in Appendix B1. None of them affects the analysis between $z = 0.2$ and $z \sim 3$, but there is a ‘boundary effect’ at the lowest and highest redshifts of the range (see below).

After this preliminary test, we use the perturbed photometry of HORIZON-AGN galaxies with $S/N > 1.5$ to produce a new SOM; the multidimensional space is the same as in Section 3 (11 broad-band colours). Fig. 7 shows the resulting redshift map limited to $z_{\text{ideal}} \lesssim 3.5$. The redshift evolution across the $80 \times 80$ grid is similar to the ideal SOM, although some details are smeared out because of photometric errors. For example, the gap between low- and high-$z$ regions is now filled by scattered galaxies (cf. Fig. 3). We quantify redshift dispersion in each cell through the normalized median absolute deviation (NMAD; Hoaglin, Mosteller & Tukey 1983) and

---

10Other options are available in some case, e.g. dynamical masses from spectroscopy (Courteau et al. 2014).
The results are comparable to other classification methods (e.g. the NUV−r versus r−K diagram, Arnouts et al. 2013). The typical scatter in log (M_\text{sim}/M_\odot) within one cell is 0.3–0.4 dex, much larger than before because not only the input colours but also the i-band rescaling now is done with perturbed fluxes. However, this is of the same order of M statistical errors in observed galaxies (e.g. Davidzon et al. 2017), a further indication that the SOM estimator can also work in the observed universe.

### 4.2 Galaxy redshift and SFR measurements

Encouraged by the previous tests, we proceed in the implementation of the SOM estimator. First of all, we need a reference sample to label the SOM grid with both redshift and SFR values. Therefore, we assume to ‘observe’ one galaxy per cell to obtain an estimate of their redshift and SFR. These galaxies belong to the calibration sample and their ‘measured’ properties are dubbed \( z_{\text{cal}} \) and SFR_{\text{cal}} for the moment, we do not make stringent requirements about how \( z_{\text{cal}} \) and SFR_{\text{cal}} are measured: they may come, e.g. from a spectroscopic survey, but not necessarily. We only make the assumptions that these are \textit{bona fide} galaxies with reliable \( z \) and SFR, and that they cover the entire 80 × 80 grid. Each calibration galaxy is randomly targeted among those in the given cell, with a sampling rate of one target per cell. For the sake of simplicity, we do not model observational uncertainty so the \( z_{\text{cal}} \) and SFR_{\text{cal}} values correspond to \( z_{\text{sim}} \) and SFR_{\text{sim}} of the given galaxy. In Section 5.1, we will discuss which kind of survey might provide such a calibration sample, modifying \( z_{\text{cal}} \) and SFR_{\text{cal}} accordingly.

The other galaxies in the SOM, not used for the calibration, will get an estimate of redshift and SFR from the SOM through the procedure described here. The method takes into account not only the best-matching cell in which galaxies lie but also the nearby ones. This choice is motivated by the impact of colour uncertainties: even though the SOM training phase places any COSMOS-like galaxy into its best-matching cell, the colours of that galaxy are still compatible (within error bars) with the weights of other cells. There is a non-negligible probability that one of them, in absence of observational errors, would be the true best-matching cell for the given galaxy.

For each entry of the mock catalogue, our algorithm includes the following steps:

(i) consider \( N_c \) cells: the best-matching unit in which the HORIZON-AGN galaxies reside and the nearest \( N_c \rightarrow 1 \) cells;
(ii) calculate the distance between the galaxy and each of those cells, with a modified version of equation (2) that takes into account photometric errors:

$$d_i = \sqrt{\sum_n (C_{n_i} - w_{i,n})^2 / \Delta C_{n_i}^2},$$

(3)

where $\Delta C_n$ is the $1\sigma$ uncertainty for the $n$-th colour and $i$ is one of the $N_c$ cells;

(iii) take the $z_{cal}$ and SFR$_{cal}$ labels of the $N_c$ cells;

(iv) compute their distance-weighted mean $z_{SOM}$ and SFR$_{SOM}$.

In particular, the resulting SFR is re-normalized (as done for stellar masses in Section 3.4):

$$SFR_{SOM} = \frac{\sum_{i \in N_c} (SFR_{cal} / d_i^2) \times (f/f_{cal,i})}{\sum_{i \in N_c} 1/d_i^2},$$

(4)

where $f/f_{cal,i}$ is the flux ratio in a reference band (we choose $i^{th}$) between the given photometric galaxy and the $bona fide$ one that labels the $i$-th cell. The square distance from the $i$-th cell is also used in the weighted mean to compute $z_{SOM}$.

We set $N_c = 10$ as the scatter generated by photometric errors typically involves the first surrounding cells. We verify that including more distant neighbours does not alter the results owing to the $1/d^2$ factor in equation (4). A more accurate, object-by-object determination of $N_c$ could be done defining the 11-dimensional ellipsoid enclosing the 68 per cent confidence limit in all dimensions jointly. However, the colours’ covariance matrix is necessary for such a task (Press et al. 1992) and that is not available in HORIZON-AGN, to be consistent with the real COSMOS catalogue. To tackle this limitation, Hemmati et al. (2019a) suggest a Monte Carlo method based on multiple realizations of the SOM mapping, extracting each time a different SED for the various galaxies (consistently with their photometric errors). A more rigorous Bayesian approach can be found in Carrasco Kind & Brunner (2014) and Buchs et al. (2019, see also Bonnett 2015 for neural network redshifts). We postpone to future work a thorough analysis of the redshift PDF via SOM. That kind of analysis shall also improve the $z_{SOM}$ estimates by smearing out the horizontal stripes visible in Fig. 8 (upper panel).

Those are the caused by a discretization in redshift for galaxies well segregated in a restricted area of the SOM, even though they span a large $z_{sim}$ range. Their pseudo-observed flux in one of the filters is significantly different from the intrinsic one, despite a rather small error bar associated with it. In those cases, averaging over $N_c$ neighbours is not sufficient to explore distant cells. A full Bayesian approach would possibly capture their diversity better than the present implementation.

We emphasize that the entire procedure takes less than 30 min of wall clock time, whereas to process the same 371 168 galaxies LEPHARE needs more than 100 h (without considering the computational time to estimate redshifts in the first run). In Fig. 8, we provide a comparison between the true redshifts of HORIZON-AGN galaxies and those derived either through the SOM (upper panel) or LEPHARE ($z_{phot}$, lower panel). The figure shows 371 168 COSMOS-like galaxies from $z = 0$ to $\sim 3.5$, namely the S/N-selected sample with the exception of the $bona fide$ galaxies used for calibration. Overall, $z_{SOM}$ are in decent agreement with $z_{sim}$, despite the significant scatter. NMAD and outlier fraction are computed for $\Delta z = z_{SOM} - z_{sim}$, being 0.044 and 6.1 per cent, respectively.

Galaxies at $z_{sim} < 0.2$ and $z_{sim} > 3.2$ are the most problematic as they suffer from SOM boundary effects: at those redshifts, i.e. the extremes of the distribution, there are too few galaxies to train a distinct cell. For instance, there are only 910 galaxies with $z_{sim} < 0.2$, spread across 23 cells; in each cell, they represent 5–12 per cent of the objects because they are classified together with a much larger number of $0.2 < z_{sim} < 0.5$ galaxies.

The NMAD and outlier fraction we find are both larger than those computed in Masters et al. (2019) for the COSMOS $z_{SOM}$, but their method slightly differs from ours as they use a deeper sample for calibration and then map (typically brighter) spectroscopic galaxies on the SOM. Here we compute the NMAD and outlier fractions with a sample that goes fainter, which can explain the slightly worse results. In Paper I, we discussed the caveats of using a spectroscopically selected subset of galaxies to assess SED-fitting quality of the parent photometric sample, as it is a limited (and sometimes biased) representation of the entire population. The comparison of Fig. 8 does not have this caveat because the same
galaxies already in the red sequence are misclassified in cells mostly occupied by dusty star-forming galaxies at higher $z$. This bias should diminish in deeper surveys, as they better disentangle redshift degeneracies. On the opposite hand, the bending of the SFR$_{\text{SOM}}$ versus SFR$_{\text{sim}}$ relation for the most star-forming objects is a consequence of the intrinsic SFR distribution inside those cells. Galaxies with the highest activity are in the tail of such a distribution, a consequence of the intrinsic SFR distribution inside those cells. Our method is not affected by this bias because it can calibrate the SFR$_{\text{SOM}}$ relation for different redshift regimes.

2. The SFR$_{\text{SOM}}$ method, which is provided by our method at the same time as the SFR$_{\text{sim}}$ estimate, is more robust to the SFR$_{\text{cal}}$ selection because it uses a more advanced Bayesian framework during the SED fitting.

3. The SFR$_{\text{SOM}}$ method provides at the same time the SFR$_{\text{SOM}}$ estimate, which is provided by our method at the same time as the SFR$_{\text{sim}}$ estimate, and the NMAD, which is computed as a function of redshift.

4. The SFR$_{\text{SOM}}$ method is more accurate for dusty star-forming galaxies at higher $z$, which are typically found in the red sequence of galaxies.

5. The SFR$_{\text{SOM}}$ method is more accurate for dusty star-forming galaxies at higher $z$, which are typically found in the red sequence of galaxies.

6. The SFR$_{\text{SOM}}$ method is more accurate for dusty star-forming galaxies at higher $z$, which are typically found in the red sequence of galaxies.

7. The SFR$_{\text{SOM}}$ method is more accurate for dusty star-forming galaxies at higher $z$, which are typically found in the red sequence of galaxies.

8. The SFR$_{\text{SOM}}$ method is more accurate for dusty star-forming galaxies at higher $z$, which are typically found in the red sequence of galaxies.

9. The SFR$_{\text{SOM}}$ method is more accurate for dusty star-forming galaxies at higher $z$, which are typically found in the red sequence of galaxies.

10. The SFR$_{\text{SOM}}$ method is more accurate for dusty star-forming galaxies at higher $z$, which are typically found in the red sequence of galaxies.

11. The SFR$_{\text{SOM}}$ method is more accurate for dusty star-forming galaxies at higher $z$, which are typically found in the red sequence of galaxies.

12. The SFR$_{\text{SOM}}$ method is more accurate for dusty star-forming galaxies at higher $z$, which are typically found in the red sequence of galaxies.

5 APPLICATION OF THE SOM ESTIMATOR TO PRESENT AND FUTURE SURVEYS

So far, we have applied the new method without discussing the details about how to build its calibration sample in practice. To
collect robust measurements of their redshift and SFR, the *bona fide* galaxies can be observed with present or future facilities. We are particularly interested in the applications that our method will have in the next decade, as foreseen surveys will offer an ideal test bed for it. This is motivated by the clear advantage of ML methods in terms of computational speed, which will be a key factor, e.g. for future cosmology-driven missions probing large cosmic volumes. Moreover, the next generation of telescopes will allow us to exploit the full potentiality of the SOM by assembling unprecedented calibration samples (see Bundy et al. 2019). In Section 5.1, we envision two of these opportunities, assuming that the SOM will be calibrated either by a large-scale spectroscopic survey in optical–NIR or from FIR observations. In Section 5.2, we compare the results from both the calibrations to standard template fitting. The SOM method applied here is more realistic than Section 4.2 but is also affected by the selection function of those ‘pseudo-surveys’. More details about their design and the bias they may introduce can be found in Appendix B (see the Online Supplementary Materials).

### 5.1 How to build the SFR calibration sample?

We discuss the realization of a calibration sample within the HORIZON-AGN framework, to be consistent with the rest of our analysis. Thanks to the wealth of observations in the COSMOS field, a similar attempt can also be made using real data, although with some limitations; we postpone this test to future work. We propose two alternate calibrations for the SOM, namely

- **C1**: a spectroscopic follow-up targeting one galaxy per cell, to derive SFR$_{\text{cal}}$ from their H$\alpha$ flux.
- **C2**: a combination of UV and IR imaging covering a portion of the field, providing SFR$_{\text{cal}}$ for several galaxies per cell via energy balance equation.

We anticipate that the analyses resulting from the two calibrations will differ, because of the specific priors of each scenario. The calibration effort also provides spectroscopic redshifts (to be used as $z_{\text{cal}}$) but we will focus on SFR$_{\text{cal}}$ measurements since they introduce the major uncertainties in our SOM estimator.\(^{13}\) Although we imagine data to be taken from next-generation facilities, galaxy parameters are assumed to be derived with the usual prescriptions. For instance, the SFR indicator adopted in C1 follows Kennicutt (1998):

$$SFR(\text{H}$\alpha$) = 5.4 \times 10^{-42} \frac{L_{\text{H}\alpha}}{\text{erg s}^{-1}} \text{ M}_\odot \text{ yr}^{-1},$$

in which the original coefficient (7.9 $\times$ 10$^{-42}$) has been converted to Chabrier’s IMF. $L_{\text{H}\alpha}$, namely the luminosity of the H$\alpha$ line, must be corrected for dust absorption. This correction can be done, e.g. by using the Balmer decrement:

$$E(B-V) = \frac{E(\text{H}\beta - \text{H}\alpha)}{k(\text{H}\beta) - k(\text{H}\alpha)},$$

The numerator on the right-hand side of equation (6) is the colour excess due to dust reddening (see equation 2 in Moustakas, Kennicutt & Tremonti 2006), while the denominator comes from an attenuation function $k(\lambda)$, as e.g. in Cardelli, Clayton & Mathis (1989).

With respect to the C2 case, there are different approaches in the literature to derive SFRs from UV+IR luminosity. The one used in Arnouts et al. (2013) is based on the formula

$$SFR(\text{NUV, IR}) = 8.6 \times 10^{-44} \frac{L_{\text{IR}} + 2.3L_{\text{NUV}}}{\text{erg s}^{-1}} \text{ M}_\odot \text{ yr}^{-1},$$

where $L_{\text{IR}}$ is the total IR luminosity (8–1000 µm) and $L_{\text{NUV}}$ is the monochromatic luminosity in the near-UV rest-frame filter. The IR luminosity accounts for the new-born stars enshrouded by dust that do not contribute to the NUV term. Different dust corrections have been proposed for equation (7), also depending on the observations used as a proxy for $L_{\text{IR}}$ (see Hao et al. 2011). Further details about these SFR indicators can be found in Kennicutt & Evans (2012) and references therein.

As mentioned above, we aim at designing both calibration samples as they would be assembled by means of next-generation facilities. For instance, the spectroscopic survey required for C1 could be carried out in the optical with the 4-m Multi-Object Spectroscopic Telescope (4MOST; de Jong et al. 2019) and in NIR with the Multi-Object Optical and Near-infrared Spectrograph (MOONS; Cirasuolo et al. 2014; Taylor et al. 2018) or the Prime Focus Spectrograph (PFS; Takada et al. 2014). In principle, the James Webb Space Telescope (JWST) could also be considered, expanding up to the mid-IR, but it is not optimized for surveying across 1 deg$^2$ (see the discussion in Davidzon et al. 2018). We consider the case in which 4MOST and MOONS are used to measure $z_{\text{cal}}$ and SFR$_{\text{cal}}$ at $z < 1.7$. For the sake of simplicity, we exclude higher redshifts not to rely on another nebular emission line, since this would make the calibration sample less homogeneous. 4MOST and MOONS specifications are further discussed in Appendix B2 (Online Supplementary Materials).

To realize the C2 sample, one could carry out FIR observations with the proposed SPICA observatory\(^{14}\) or the Origins\(^{15}\) mission, both expected to launch in the 2030s. We can imagine using these telescopes to scan ∼0.1 deg$^2$ of our field in the wavelength range between 20 and 230 µm. This would result in robust $L_{\text{IR}}$ estimates up to $z \sim 3$ (Gruppioni et al. 2017; Kaneda et al. 2017). To complete equation (7) with rest-frame NUV luminosity, one can assume to rely on the GALEX data at $z < 0.5$ (Arnouts et al. 2013) and deep $u$ and $B$ photometry at higher redshift. Those data should be superseded by higher resolution photometry from CASTOR\(^{16}\) and from the Large Synoptic Survey Telescope (LSST Science Collaboration 2009). All these future facilities are expected to observe COSMOS as one of their calibration deep fields (Capak, Scolnic & Davitzion 2019), so in our simulated universe it is fair to assume that a COSMOS-like light-cone can benefit from them as well.

A difference between C1 and C2 is that the former provides also $z_{\text{cal}}$ by construction, whereas the C2 photometric data must be complemented by reliable redshifts to estimate galaxy rest-frame luminosity. In the assumption of using SPICA, this shall result from its FIR high-sensitivity grating spectrometer. We can also suppose that the simulated light-cone, like the real COSMOS field, will be

\(^{14}\)Space Infrared telescope for Cosmology and Astrophysics, https://spica-mission.org/

\(^{15}\)https://asd.gsfc.nasa.gov/firs/

\(^{16}\)CASTOR is the Cosmological Advanced Survey Telescope for Optical and ultraviolet Research proposed by the Canadian Space Agency (Côte et al. 2012). This satellite could launch as early as 2027, surveying the UV with a ∼30 better resolution than GALEX and a ×100 larger field of view than HST.
I. Davidzon et al.

Figure 11. HORIZON-AGN SOM trained with COSMOS-like colours and calibrated to work as a redshift and SFR estimator. Upper panels: the SOM is labelled according to the redshift ($z_{\text{cal}}$, left-hand panel) and SFR ($\text{SFR}_{\text{cal}}$, right) of 4749 ‘spectroscopic’ galaxies coming from a pseudo-survey of calibration (C1). The white pixels in the colour map are empty cells not covered by the C1 sample. Lower panels: in this case, the SOM is labelled according to the $z_{\text{cal}}$ and $\text{SFR}_{\text{cal}}$ values (left- and right-hand panels, respectively) coming from an alternate calibration sample (C2). The 37780 galaxies in this sample come from an area of 0.1 deg$^2$ within the HORIZON-AGN light-cone. Their $\text{SFR}_{\text{cal}}$ is assumed to be measured from their UV and IR luminosity, which in principle could be obtained with a deep pencil-beam imaging survey.

To summarize, the calibration sample C1 is made by 4749 bona fide galaxies in an equivalent number of cells. They are supposed to be H$\alpha$ emitters ($>2 \times 10^{-17}$ erg s$^{-1}$ cm$^{-2}$) at $0 < z < 1.7$. C2 assumes to observe 19 arcmin $\times$ 19 arcmin of the HORIZON-AGN light-cone in UV and FIR; the 40,046 galaxies in that area are stacked (binned per cell) to obtain median SFRs. In the former case, the logarithmic $\text{SFR}_{\text{cal}}$ is obtained by perturbing the original log (SFR$_{\text{sim}}$/M$_\odot$/yr$^{-1}$) of each bona fide galaxy with random Gaussian noise. The Gaussian standard deviation is set to $\sigma = 0.18$ dex from comparison to state-of-the-art surveys (e.g. FMOS-COSMOS; Kashino et al. 2019). In C2, we do not attempt to reconstruct $L_{\text{UV}}$ and $L_{\text{IR}}$ for the sake of simplicity. The $\text{SFR}_{\text{cal}}$ of a given cell is the median SFR$_{\text{sim}}$ of the bona fide galaxies inside it, perturbed with Gaussian noise ($\sigma = 0.1$ dex, see Ilbert et al. 2015).

Eventually, the SOM is labelled with the $z_{\text{cal}}$ and $\text{SFR}_{\text{cal}}$ values of either C1 (Fig. 11, upper panels) or C2 (lower panels). Depending on the used bona fide sample, certain cells do not get a label.

5.2 SFR estimates and comparison with template fitting

After labelling the SOM, we apply the procedure described in Section 4.2 to assign an SFR$_{\text{SOM}}$ estimate (equation 4) to each photometric galaxy. The outcome can be compared to that obtained in Paper I by using LEPHARE. We do not show the $z_{\text{SOM}}$ versus $z_{\text{sim}}$ comparison as the trend is similar to Fig. 8 (upper panel). Despite

$^{17}$Euclid will collect spatially resolved H$\alpha$ fluxes from $z = 0.9$ to 1.8 (down to $0.5-3 \times 10^{-16}$ erg cm$^{-2}$ s$^{-1}$, Pozzetti et al. 2016) that can be used, e.g. for aperture correction calibration of the multislit instruments.

$^{18}$This is expected to be a good proxy of the UV+IR estimator, whose timescale is similar to the 100 Myr interval used to define SFR$_{\text{sim}}$ in HORIZON-AGN (it is also comparable with H$\alpha$-derived measurements, see Kashino et al. 2019).
Manifold learning and galaxy properties

Figure 12. Comparison between intrinsic SFR$_{\text{sim}}$ versus estimates obtained from different methods: standard template fitting using the code LEPHARE (upper row of panels); using the SOM method with the calibration described as version C2 in the text (middle panels); SOM method with a different calibration sample, referred as C1 in the text (lower panels). Galaxies are binned in the different redshift bins according to either their $z_{\text{phot}}$ from LEPHARE or $z_{\text{SOM}}$ in the case of the new method proposed here. Version C1 is limited to the first two $z$ bins because of the way the calibration sample is constructed. In each panel, the solid line indicates the 1:1 relationship and the dotted lines a ±0.15 dex offset from it.

the additional uncertainties introduced in Section 5.1, the figure of merit does not change. For the C2 calibration, which covers the same redshift range of Fig. 8, NMAD($z_{\text{SOM}}$) and outlier fraction remain 0.043 and 6 percent, respectively. In the following, we focus on the SFR$_{\text{SOM}}$ results, which show a remarkable improvement with respect to template fitting estimates (SFR$_{\text{phot}}$). We remind that the estimate of physical properties via template fitting involves a two-step procedure. First, to find their $z_{\text{phot}}$, LEPHARE fits galaxy SEDs with a composite set of templates (described in Laigle et al. 2016); then, after fixing the redshift of each galaxy to $z_{\text{phot}}$, the code calculates the SFR (along with stellar mass and other physical quantities) by means of another SED library, this time made from the BC03 models. Since our mock catalogue reproduces COSMOS2015, LEPHARE is used with the same configuration as in Laigle et al. (2016). More details about running LEPHARE to estimate SFRs in HORIZON-AGN can be found in Paper I.

The upper panels of Fig. 12 show the comparison between SFR$_{\text{phot}}$ and SFR$_{\text{sim}}$ in different bins from $z_{\text{phot}} = 0.2$ to 3. Underestimates and overestimates produced by LEPHARE are clearly visible, generating two parallel sequences in the distribution. Such a bimodality is due to SED-fitting degeneracies. By comparing a dust-free vs dusty Universe, Paper I isolated the major role of dust attenuation in driving this bimodality. In particular, the choice of the extinction curves in the template library is pivotal. This remains true even when the redshift is fixed to its intrinsic value instead of $z_{\text{phot}}$. Inadequate extinction models or $E(B-V)$ values may cause indeed an overestimation or an underestimation of the SFR, as shown in Appendix B of Paper I.

The same photometric galaxies are reported in the middle and lower panels of Fig. 12 comparing intrinsic SFRs with the values computed through the SOM (C2 and C1 version, respectively). The performance of the SOM is significantly better than template fitting. The SFR$_{\text{SOM}}$ distribution does not show the same bimodality observed for the SFR$_{\text{phot}}$ estimates because the SOM fitting is based only on observed SEDs, which naturally include the ‘correct’ dust attenuation law and $E(B-V)$ range. In LEPHARE, the grid of templates is built without strong observational priors so the library is affected by artificial degeneracies.

Also, our method is model dependent because of the SFR$_{\text{cal}}$ labels. These measurements require some theoretical prescription (e.g. about dust attenuation or IMF). However, we argue that the required assumptions, for either C1 or C2, introduce a milder bias than template fitting. For instance, the C1 calibration requires the choice of a dust extinction curve (equation 6) but the difference

$^{19}$All the bona fide galaxies used for calibration have been excluded from the comparison.
between models is small: e.g. \( k(\text{H} \beta) - k(\text{H} \alpha) = 1.07, 1.27 \) for Cardelli et al. (1989) and Calzetti et al. (2000), respectively. On the contrary, LEPHARE templates are constrained by data at bluer r.f. wavelengths where the dust extinction curve plays a more important role (Ilbert et al. 2009); for the same models in the example above: \( k(2000 \, \text{Å}) - k(3000 \, \text{Å}) = 3.18 \) and 1.95.

With respect to the C2 sample, one may notice that the energy balance equation is also implemented in template fitting codes (e.g. MAGPHYS; da Cunha et al. 2008) sometimes in very elaborated ways including also the AGN contribution (e.g. SED3FIT; Berta et al. 2013). In fact, one may also use one of those codes instead of equation (7) but not for the other HORIZON-AGN galaxies that do not belong to C2. Moreover, even if the whole galaxy sample was observed in UV and FIR, codes like MAGPHYS are extremely expensive in terms of computational time and run only after fixing the redshift. This two-step fitting procedure, which is of widespread use in the literature, raises several issues (e.g. propagation of \( z \) uncertainties, Grazian et al. 2015; Davidzon et al. 2017). On the other hand, the SOM does not require such a procedure, providing \( z \) and SFR estimates simultaneously.

Fig. 13 proposes the same comparison of Fig. 12 in a different flavour, i.e. showing the median ratio \( \text{SFR}_{\text{SOM}}/\text{SFR}_{\text{sim}} \) in three bins of apparent magnitude from \( i^* = 22 \) to 25. At \( i^* < 23 \) (Fig. 13, middle panel), there is an excellent agreement of both C1 and C2 estimates with the intrinsic SFR. Such a trend is still observed at \( 23 < i^* < 24 \) even though the most star-forming galaxies start to be systematically underestimated by more than a factor of 2. This is a border effect inherent to the SOM analysis already discussed in Section 4.2; having a larger sample that allows for a more representative SOM would mitigate this effect (Buchs et al. 2019). The discrepancy becomes more accentuated at \( 24 < i^* < 25 \) (Fig. 13, lower panel), especially for the C1 calibration that by construction relies on bona fide galaxies systematically brighter than the average (an effect that could be accounted for by a higher sampling rate in those cells, see Masters et al. 2019). Concerning LEPHARE, underestimates and overestimates would compensate each other resulting in a misleading \( \text{SFR}_{\text{LEPHARE}}/\text{SFR}_{\text{sim}} \simeq 1 \). Therefore, Fig. 13 does not show the median of the \( \text{SFR}_{\text{LEPHARE}} \) distribution but only the interval between the 16th and 84th percentile. Such a dispersion is significantly larger than the ML estimates in all the magnitude bins.

6 SUMMARY AND CONCLUSION

Compared to the large number of studies measuring galaxy redshifts with ML techniques, little progress has been made concerning other physical parameters. In spite of that, ML methods will be pivotal in the near future to derive stellar mass, SFH, and other galaxy properties in extremely large data sets from surveys such as Euclid and LSST. In addition to their unprecedented speed, these algorithms (particularly the unsupervised ML methods) may lead to a ‘new paradigm’ in which human intervention (i.e. the application of interpretative models) starts after galaxy classification and demographics have been decided by the machine. However, results may be affected by new kinds of systematics introduced, e.g. during the data reduction process or the training set selection. A thorough investigation of ML performance and the role of its ‘observational priors’ is thus imperative before such high expectations may be deemed justified.

With this in mind, we have explored advantages and limitations of the SOM as a galaxy parameter estimator independent of model templates. We chose the SOM because it is an unsupervised dimensionality reduction algorithm able not only to learn the complex structure of data but also to project it in a lower dimensional space (2D in our analysis) still preserving its ‘topological’ features. It should be clarified that our goal is not advocating for the SOM to replace standard template fitting: the two complementary approaches should be used in synergy, the same way semi-analytic and hydrodynamical simulations have contributed to inform each other and together improve our understanding of galaxy evolution. For example, ML investigations may help to shed light on the systematic \( M_\odot \) underestimation in unresolved SED fitting of star-forming galaxies (Pozzetti et al. 2007; Sorba & Sawicki 2015, 2018).

We tested the SOM with a mock galaxy catalogue (presented for the first time in Paper I) derived from the HORIZON-AGN hydrodynamical simulation. Galaxies cover 1 deg\(^2\) area and a
redshift range $0 < z < 4$, with a photometric baseline similar to state-of-the-art surveys (broad-band filters from $u$ to $[4.5 \text{~mm}]$). The SOM has been trained using as input only galaxy colours, to be an analogue of ‘classical’ SED-fitting codes like LEPHARE or EAZY (Brammer, van Dokkum & Coppi 2008). In principle, other (e.g. morphological) features may be trained for, but this is left to future work. After classifying the mock galaxies in about 6400 different classes (called ‘cells’ in our jargon), we explored the connections between the class/cell a galaxy belongs to and its physical properties. Then, we calibrated a posteriori the SOM by labelling each cell with a value of $z$ and SFR, so that other galaxies in the same cell may have a proxy of their own redshift and star formation activity. Eventually, we used the calibrated SOM to estimate the SFR for a subsample of about 375 000 mock galaxies between $z \sim 0$ and 3. Our findings are summarized in the following.

(i) The SOM is an effective tool to visualize the characteristics of a complex, non-linear manifold as the HORIZON-AGN light-cone. Galaxies are organized in a (human-readable) 2D grid without smearing out the features of their original parameter space. Moreover, this is computational inexpensive, suggesting a convenient way to describe and inspect the properties of extremely large simulations (Mitra, Davé & Finlator 2015).

(ii) Since in our case the parameter space is made by observer’s frame colours, the SOM works like an SED-fitting algorithm without a precompiled library of templates: the SOM adapts its cells/weights to the data so that galaxies with similar colours (i.e. similar SEDs) are enclosed the same cell. We also find that the high-resolution spectra turn out to be nicely classified, in spite of using only broad-band photometry for training.

(iii) We confirm that objects in the same cell have similar redshift [as shown in Masters et al. (2015) in the observed universe] but we also find that their $M/L$ and $sSFR$ are similar, with a typical scatter of 0.15 and 0.3 dex, respectively. Also $M$ and SFR, after taking into account a normalization factor, are well correlated to the cell where a galaxy lies. After including photometric uncertainties (modelled after the COSMOS2015 survey) and rejecting objects with $S/N < 1.5$ in any band, we trained again the SOM: the correlation between galaxy properties and cells was still present, although with larger scatter. This indicates that our analysis can be reproduced in real optical–NIR surveys (provided a sufficient depth of the observations).

(iv) We have measured the redshift of COSMOS-like ($S/N > 1.5$) galaxies through the SOM, finding a fairly good agreement with intrinsic $z_{\text{sim}}$ but a larger scatter than template fitting: The $z_{\text{SOM}}$ versus $z_{\text{sim}}$ comparison results into NMAD = 0.044 and about 6 per cent of catastrophic errors, whereas with LEPHARE they are 0.024 and 1.5 per cent, respectively. On the other hand, the redshift bias in the SOM case is significantly smaller ($\sim 0.001$, compared to $\sim 0.011$ in LEPHARE). We considered such a result sufficiently good for our purposes so we did not attempt to improve the redshift estimator (as done, e.g. in Buchs et al. 2019).

(v) Exploiting these SOM properties, we have developed a new SFR estimator for photometric galaxies. We have assumed that a small fraction of them (10 per cent or less) has been followed up to serve as a calibration subsample, providing labels ($z_{\text{cal}}, \text{SFR}_{\text{cal}}$) to the SOM cells. We have discussed possible follow-up strategies with optical–NIR spectroscopy or with UV+IR instruments, and the possible bias introduced by each of them. After accounting for such uncertainties, we have compared the SFR$_{\text{SOM}}$ of COSMOS-like galaxies with their intrinsic SFR$_{\text{sim}}$. Overall, the dispersion (defined as the range between 16th and 84th percentile) in logarithmic bins of SFR is $\pm 0.2$ dex, with a small systematic offset [median log (SFR$_{\text{SOM}}$/SFR$_{\text{sim}}$) = 0.02–0.04 dex]. The most active galaxies are an exception, being significantly underestimated because they are in cells whose majority of objects (including the calibration ones) are less star forming.

(vi) LEPHARE SFR$_{\text{phot}}$ estimates are also available in HORIZON-AGN and we have compared them to the new indicator. The latter performs remarkably better: SFR$_{\text{SOM}}$ are more precise but also significantly less biased, as they do not rely on a template library that introduces artificial degeneracies in the SED fitting (as investigated in Paper I).

The suboptimal performance of the SOM as a redshift machine found in this analysis is partly due to the fact that we have not entirely followed Masters et al. (2015) prescriptions, e.g. we did not use cell occupation as a prior nor we distinguished a deeper calibration sample from the rest of the survey (or use a combination of multiple fields). We note that the comparison is not straightforward since Masters et al., working with observed galaxies, are forced to use a spectroscopic subsample that is biased to some extent (see Paper I). However, as highlighted in Masters et al., on that spectroscopic sample their $z_{\text{SOM}}$ figure of merit is better than LEPHARE.

On the other hand, the better performance of our SOM method to compute SFR does not imply that it is bias free: some systematics may be introduced while selecting the calibration galaxies and measuring their SFR$_{\text{cal}}$. We argue however that model assumptions in the SFR$_{\text{cal}}$ calculation are generally less severe than those involved in the construction of libraries from stellar population synthesis models, with a coarse grid of $E(B-V)$ values, simplistic SFHs, fixed stellar metallicity, and other limitations to which SFR is sensitive (Papovich et al. 2001, see also discussion in Paper I). Moreover, if the subsample used for calibration turns out to be strongly biased it can be replaced by a better one without reclassifying the target galaxies, while any improvement in the template library of LEPHARE would require to run again that (computationally expensive) code over the whole catalogue. It should also be emphasized that estimates of redshift and physical parameters are provided simultaneously – a unique advantage of the SOM method that in future developments shall allow for a better treatment of $z$-error propagation.

We aim at transferring our method to the real COSMOS catalogue in the next paper of this series, even though data available in that field may be able to calibrate the SFR only in a limited portion of the SOM. None the less, this effort can result in an original comparison between different estimators. For example, one could derive SFR from radio continuum stacking (as in Karim et al. 2011) versus UV+IR luminosity (as in Ilbert et al. 2015) for galaxies in the same cells, easily identifying the region of the parameter space where the indicators disagree.

This work is also intended to provide a new science case for upcoming large-area surveys. The SOM requires an accurate calibration sample relatively modest in size (but large enough to limit sample variance effects, Buchs et al. 2019), and then billions of galaxies (e.g. from the 15 000 deg$^2$ of Euclid) can be efficiently mapped to get a proxy for their redshift and physical properties. This is particularly true for the Euclid Deep Fields, which will have a photometric baseline similar to the one assumed here, thanks to the complementary surveys in optical (Hawaii two-O, PI: D. Sanders) and MIR (Euclid/WFIRST Spitzer Legacy Survey, PI: P. Capak). We also mentioned the contribution that 4MOST, MOONS, and PFS may provide to calibrating the galaxy colour space, owing to their unprecedented multiplexing. Our case study also supports the
concept of a deep surveying of COSMOS with CASTOR, SPICA, and Origins, to continue its use as a reference field for the coming decades.

ACKNOWLEDGEMENTS

ID thanks Stefano Andreon, Sirio Belli, Micol Bolzonella, Keerthana Jegatheesan, Chris Hayward, and Lucia Pozzetti for useful discussions, and Elvira Tibi for all the rest. CL is supported by a Beecroft Fellowship. OI acknowledges the funding of the French Agence Nationale de la Recherche for the project ‘SAGACE’. This research was supported in part by the National Science Foundation under Grant No. NSF PHY-1748958 and by the NASA ROSES grant 12-EUCLID12-0004. The analysis presented in this work relied on the HPC resources of CINES (Jade) under the allocations grant 12-EUCLID12-0004. The analysis presented in this work was supported in part by the National Science Foundation Agence Nationale de la Recherche for the project ‘SAGACE’. This study was supported by the ERC grant 670193 and HORIZON-UK. The authors thank O. Ilbert and H. Hemmati for useful discussions, and Elvira Tibi for all the rest. CL is supported by the ERC grant 670193 and HORIZON-UK. IS acknowledges the funding of the Arces project (ARB15-0008) and HORIZON-UK. IS is partly supported by the Agence Nationale de la Recherche for the project ‘SAGACE’. This research was supported in part by the National Science Foundation under Grant No. NSF PHY-1748958 and by the NASA ROSES grant 12-EUCLID12-0004. The analysis presented in this work relied on the HPC resources of CINES (Jade) under the allocations grant 12-EUCLID12-0004. The analysis presented in this work was supported in part by the National Science Foundation

REFERENCES

Komatsu E. et al., 2011, ApJS, 192, 18

Manifold learning and galaxy properties

Supporting Information

Supplementary data are available at MNRAS online.

Appendix A. Caveats in the SOM of HORIZON-AGN galaxies.

Appendix B. Training and calibration galaxy samples.

Please note: Oxford University Press is not responsible for the content or functionality of any supporting materials supplied by the authors. Any queries (other than missing material) should be directed to the corresponding author for the article.

This paper has been typeset from a \TeX/\LaTeX file prepared by the author.