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Enhancing quantum transduction via long-range waveguide-mediated interactions between quantum emitters

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Efficient transduction of electromagnetic signals between different frequency scales is an essential ingredient for modern communication technologies as well as for the emergent field of quantum information processing. Recent advances in waveguide photonics have enabled a breakthrough in light-matter coupling, where individual two-level emitters are strongly coupled to individual photons. Here we propose a scheme that exploits this coupling to boost the performance of transducers between low-frequency signals and optical fields operating at the level of individual photons. Specifically, we demonstrate how to engineer the interaction between quantum dots in waveguides to enable efficient transduction of electric fields coupled to quantum dots. Owing to the scalability and integrability of the solid-state platform, our transducer can potentially become a key building block of a quantum internet node. To demonstrate this, we show how it can be used as a coherent quantum interface between optical photons and a two-level system like a superconducting qubit.

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I. INTRODUCTION

Transduction of information between physical systems operating at different energy scales is of immense technological importance. In particular, efficient transduction between the microwave and optical domains is an essential requirement for telecommunication networks. The advent of quantum communication technologies necessitates analogous transduction devices capable of coherent information transfer for quantum fields. Possible applications of such devices range from a quantum internet [1–5] and distributed quantum computing [6,7] to quantum metrology [8–10].

Due to the large range of applications, several different methods for implementing quantum transducers have been investigated. A large class of these relies on the use of nanomechanical systems [11–15] or direct electro-optical coupling [16,17]. Other proposals exploit quantum emitters with both microwave and optical transitions [4,18–22]. Many of these rely on weak magnetic interactions to single emitters, but exploit strong coupling to ensembles of emitters (see Refs. [20,23] for exceptions). Despite these efforts, efficient low noise quantum transduction of low-frequency excitations to the optical regime remains elusive.

Common to the approaches discussed above is the use of strong optical control fields. This can be a major source of light-induced decoherence [24], since even the absorption of a single optical photon can have a significant influence on a quantum system operating in the microwave regime. Furthermore strong light fields pose a filtering problem since weak quantum fields have to be distinguished from strong background signals. It is therefore highly desirable to work at very low light levels.

In this paper, we propose an electrically coupled quantum transducer that works at the few-photon level. The principal elements of our transducer are semiconductor quantum dots (QDs) grown in photonic crystal waveguides with transform-limited linewidth [25] and experimentally demonstrated coupling efficiency $\beta$ up to 98% [26]. We show that such high coupling efficiencies enable a high transduction efficiency due to the strongly suppressed loss rate out of the waveguide. A key feature of our transducer is that it works efficiently even when all light fields contain at most a few photons. We achieve this by engineering the waveguide-mediated interactions between multiple QDs. This low light level minimizes the light-induced decoherence of the quantum systems, as well as ensures negligible background light in the transduced signal.

For a particular application we show how to exploit the proposed transducer as a quantum interface between optical photons and superconducting (SC) qubits. Related approaches were recently proposed using two nearby dipole-coupled molecules [27] or a double-QD molecule [28]. As opposed to these systems, experimental demonstrations of QD-waveguide interfaces have shown more efficient coherent coupling to traveling light fields [26]. This strongly enhances the transduction efficiency in our scheme. We also show that long-range waveguide-mediated interaction allows engineering super- and subradiant states [29–34] between distant QDs, which can be exploited to improve the transduction without requiring engineering complicated near-field interactions.

II. SYSTEM HAMILTONIAN

In Fig. 1(a), we show schematically our proposed quantum transducer. It consists of three components; a one-dimensional (1D) waveguide for efficient confinement of the optical mode; one or more QDs coupled to the photon mode with high efficiency; and finally a nearby oscillating electric dipole, which electrically couples to a QD excitation. For specificity, we focus on transduction from a coherent two level system (TLS) with a dipole allowed transition at a non-optical frequency,
The Raman transition entangles the frequency of a scattered weak photon pulse with the internal state of the TLS, thereby achieving coherent transduction between the two systems. To study the dynamics of the transducer, we apply the formalism of Refs. [42,43] and find that the total scattered field is given by
\[ \hat{a}_{\text{out}} = [1 + i\delta_0 \hat{S}_{00} + i\delta_0 \hat{S}_{10}] \hat{a}_{\text{in}} + F, \]
where \( \hat{a}_{\text{in}} \) and \( \hat{a}_{\text{out}} \) are the right-going input and output field operators, respectively, and \( \delta_0 = |1\rangle \langle 0 | \) and \( \delta_0 = | 0 \rangle \langle 0 | \) are, respectively, the Heisenberg operators for the coherence and population of the ground state of the combined QD-TLS system. \( F \) is a noise operator and \( S_{01} \) and \( S_{10} \) are the scattering amplitudes for the transitions from state \( |0\rangle \) to \( |0\rangle \) and \( |1\rangle \), respectively, and are calculated from the total contribution of all excited states.

We assume that the ground states are sufficiently separated in energy compared to the width of the incoming photon pulse, so that scattered photons can be filtered spectrally and the only contribution to “red” photons comes from the term \( i\delta_0 \hat{S}_{10} \hat{a}_{\text{in}} + F \). Detection of such a red-detuned photon heralds a flip of the TLS; the Raman-scattering detection probability \( P_R \) for a single-photon input can be found by the expectation value of the photon-number operator of the red field
\[ P_R = \int_0^T \langle \hat{a}_{\text{out}}^\dagger \hat{a}_{\text{out}} \rangle \, dt = |S_{10}|^2 \]
where we have normalized the incoming pulse of duration \( T \) to contain a single photon. Note that the quantum vacuum noise term \( F \) in \( \hat{a}_{\text{out}} \) does not contribute to the photon number expectation value. The scattered right-going mode (transmission) is expected in magnitude to the scattered left-going mode (reflection). Similarly the QD couples equally to left and right propagating modes. Experimentally, the scattered red field amplitude can therefore be twice enhanced by combining both modes on a beamsplitter [44], or using a single-sided waveguide [45], corresponding to a factor of four improvement in the success probability.

From the scattering formalism of Ref. [42], we find the scattering matrix element \( S_{10} = \frac{\epsilon_1}{2} \langle e1 | \hat{H}_{\text{ph}} | e0 \rangle \) and therefore \( P_R = \Gamma_{1D}^2 |\langle e1 | \hat{H}_{\text{ph}} | e0 \rangle|^2 \). Here, the scattering dynamics of the excited subspace of the system are fully absorbed into an effective non-Hermitian Hamiltonian \( \hat{H}_{\text{ph}} = \hat{H}_{\text{ph}} - \frac{i}{2} \sum_k \hat{L}_k^\dagger \hat{L}_k \), where \( \hat{H}_{\text{ph}} \) describes the energies and couplings in the excited subspace of the total Hamiltonian, and \( \hat{L}_j \) are the Lindblad operators associated with interactions with the environment. For our single-QD system, \( \hat{H}_{\text{ph}} = -\delta \hat{\sigma}_z + \omega_p (\hat{\sigma}_z - \hat{\sigma}_x) / 2 + g_s \hat{n}_s \), with \( \delta = \omega_q - \omega_p \) being the photon-QD detuning and \( \hat{n}_s = |e0\rangle \langle e0 | + |e1\rangle \langle e1 | \). The operators representing the decay dynamics of the system are defined as \( \hat{L}_k = \sqrt{\Gamma_k} |g\rangle \langle e| + \Gamma_k \hat{S}_{10} \), with \( \Gamma_k \) being the QD decay into and out of the waveguide with rates \( \Gamma_{1D} \) and \( \gamma' \), respectively.

We maximize \( P_R \) as a function of the detuning between input field and QD, yielding the resonance conditions \( \Delta_\pm = (\omega_q + \sqrt{\omega_p^2 + g_s^2 - \Gamma^2}) / 2 \). At these resonances, \( P_R^{(\text{QRD})} = \beta^2 \frac{g_s^2}{\omega_p^2} \), and in the strong- and weak-coupling limits we find
\[ P_R^{(\text{QRD})} \approx \beta^2 \frac{g_s^2}{\omega_p^2} \text{ for } g_s \gg \omega_q, \]
\[ P_R^{(\text{QRD})} \approx \beta^2 \frac{g_s^2}{\omega_p^2} \text{ for } g_s \ll \omega_q, \]
respectively, where \( \beta = \Gamma_{1D} / (\Gamma_{1D} + \gamma') \) describes the QD-waveguide coupling efficiency. Equation (1) expresses the striking advantage that can be obtained by exploiting strong coupling of emitters with a waveguide. For \( \beta \) approaching

III. SINGLE-EMITTER QUANTUM TRANSDUCTION

We consider a Raman transition between the states of the combined TLS-QD system [Fig. 1(c)] via a single incoming optical photon in the waveguide with central frequency \( \omega_p \).
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FIG. 2. (a) Transducer based on two QDs in a waveguide. One of the QDs is electrically coupled to the TLS. (b) Energy-level diagram of the combined QD-TLS system. |0⟩, |1⟩ represent the TLS internal states. |{A}, |S} represent the (anti-)symmetric states of the two-QD coupled system. The incoming photon is tuned into resonance with |A⟩. (c) Four QDs in a waveguide are spaced equidistantly such that kΔz = π/2. One of the central QDs is coupled to a coherent two-level system. (d) Energy-level diagram of the combined QD-TLS system for four QDs, with two sets of (anti-)symmetric eigenstates spaced by ν ≈ 1.3Γ1D, decaying at enhanced(reduced) decay rates.

unity, a transducer can be constructed where even a single optical photon is sufficient to efficiently transduce a low-frequency signal. This minimizes any possible decoherence induced by light.

IV. MULTI-EMITTER QUANTUM TRANSDUCTION: SUBRADIANCE ENGINEERING

Many of the qubit systems relevant for this transduction scheme operate in the microwave (GHz) regime, which is larger than the maximal estimated coupling $g_{e} \lesssim 2\pi \times 1$ GHz. The resulting reduction of $P_{g}$ in Eq. (2) arises because the electric dipole moment of the TLS is linked to a transition between two energy levels. The QD thus feels an oscillating field, and this averages out the coupling. To counter this effect, we propose to engineer the excited subspace using multiple coupled emitters. This exploits the high β factor achievable for QDs in photonic crystal waveguides to get strong waveguide-mediated interactions between distant QDs. With two QDs we show how to engineer an increased interaction time, thereby improving the effective coupling. By using four QDs one can even engineer a resonant Raman transition, thereby avoiding the averaging effect.

We first consider two emitters in a 1D waveguide [see Fig. 2(a)]. The photonic field in the waveguide induces long-range interactions between the two. In Ref. [43] this interaction is included as part of a non-Hermitian Hamiltonian of the single-excitation subspace for the bare two-emitter system $H_{ab} = -\Delta \hat{I}_{1} + (\Delta / 2 - i\Gamma_{1} / 2)|e\rangle\langle g| + (\Delta / 2 - i\Gamma_{1} / 2)|g\rangle\langle e| + \Omega|e\rangle\langle g| + |g\rangle\langle e|$, where $|e\rangle = |e\rangle_{1} \otimes |g\rangle_{2}$, $|g\rangle = |e\rangle_{1} \otimes |e\rangle_{2}$, $\Delta \neq \text{difference between the emitters’ transition frequencies}$, and $\delta$ is the detuning between the incoming photon and mean QD transition frequency. $\Gamma_{i} = \Gamma_{1,1D} + \gamma_{i}$ is the decay rate of emitter $i$, which consists of the decay rate into the waveguide $\Gamma_{1,1D}$ and to the environment $\gamma_{i}$. The collective complex coupling term $\Omega = -i\sqrt{\Gamma_{1,1D}\Gamma_{2,1D}}\exp[i\Delta z_k]$ is the waveguide-mediated coherent coupling between emitters and collective decay. $\Delta z = |z_2 - z_1|$, and $z_i$ is the position of emitter $i$ [46].

We diagonalize the Hermitian part of the Hamiltonian $H_{ab}$ and find (anti-)symmetric eigenstates $|A⟩ = \xi_{1}|eg⟩ - \xi_{2}|ge⟩$ and $|S⟩ = \xi_{2}|eg⟩ + \xi_{1}|ge⟩$. Here coefficients $\xi_{1,2}$ depend on the collective coupling $\Omega$ and detuning $\Delta$ between the emitters. The decay rates $\Gamma_{j} = \gamma_{j} + \Gamma_{j,1D}$ with $j = A, S$ consist of a part going outside the waveguide $\gamma_{j} = \xi_{1}^{2}\gamma_{1} + \xi_{2}^{2}\gamma_{2}$ and a part going into the waveguide $\Gamma_{j,1D} = \xi_{1}^{2}\Gamma_{1,1D} + \xi_{2}^{2}\Gamma_{2,1D}$, where $\Gamma_{j,1D}$ is the decay rate of the $j$th QD. The resulting reduction of $\Gamma_{j}$, thereby improving the effective coupling. By using an external field (note that deterministic placement of a QD in a waveguide with a precision less than 10 nm has been achieved [47]). Here $Γ = Γ_{1} = Γ_{2}$ and $β$ is
 FIG. 3. (a) Raman transition probability as a function of coupling strength $g_s$. The exact forms (markers) include all scattering pathways, while approximate forms (lines) include only the most significant pathway, as given by Eqs. $(2), (4), \text{and } (5)$. For the one-QD (red) and two-QD (blue) cases, we set $\omega_q = 2\pi \times 5 \text{ GHz}$, $\Gamma_{1\text{D}} = 1 \text{ ns}^{-1}$, $\beta = 0.9$. In the four-QD case (green), we assume a Purcell enhanced emitter decay rate $1/\Gamma_{1\text{D}} = 1.27/\omega_q \approx 250 \text{ ps}$ and $\beta = 0.9$. We optimize the detunings $\delta$ and $\Delta$ in the full numerics and fix the inter-QD spacing $k\Delta z = n\pi$ (with integer $n$) in the two-QD case and to $k\Delta z = \pi/2$ in the four-QD case. (b) Infidelity $(1 - F$, solid lines) and success probability $P_{\text{succ}}$ (dashed lines) of entanglement generation for a coherent pulse input, as a function of average photon number. Detection efficiency $\eta = 0.7$, coupling $g_s = 2\pi \times 1 \text{ GHz}$, and the other parameters as in panel (a).

defined analogous to the one-emitter case. For this condition, we find

$$P_R^{(2\text{QD}), \text{opt}} \approx \frac{\beta^2}{1 - \beta^2} \left(\frac{g_s}{\omega_q}\right)^2.$$  

(4)

Comparing Eq. $(4)$ to Eq. $(2)$ there is a factor $1/(1 - \beta^2)$ improvement in transduction efficiency compared to the single-QD case. For $\beta = 0.9$, this is a factor 5 improvement. For $\beta = 0.98$, as experimentally demonstrated in Ref. [26], this is a factor 25. This conclusion is verified in Fig. 3(a), where we compare Eq. $(4)$ to the single-QD case and the full calculation including all paths.

For nonidentical emitters we have verified numerically that there is an enhancement of the Raman probability as discussed below Eq. $(3)$. In the Appendix we show that for two emitters with identical $\beta$ but different rates $\Gamma_i$, Eq. $(4)$ remains an excellent approximation regardless.

The main limitation of the above scheme is that the relevant transition is still far off resonant, resulting in the factor $(g_s/\omega_q)^2$ suppressing the efficiency. With four QDs we can further engineer the energy of the long-lived states. By tuning the frequency of two such states in resonance to the TLS energy $\omega_q$, we can achieve an enhanced Raman probability.

To this end, we consider four QDs placed in a 1D waveguide [see Fig. 2(c)]. At zero mutual detuning between the emitters and assuming equal decay rates we have identified an optimum at $k\Delta z = \pi/2$ between each QD. There, we find two bright and two dark states, with an energy splitting $\nu = \sqrt{2(\sqrt{5} + 1)}\Gamma_{1\text{D}} \approx 1.27 \Gamma_{1\text{D}}$ between them. The dark states exhibit suppressed decay rates $\Gamma_{1,1\text{D}} = \Gamma_{2,1\text{D}} = (1 - \alpha_k)^2\Gamma_{1\text{D}}$ into the 1D waveguide with $\alpha_k = \sqrt{\sqrt{5} - 1} \approx 0.79$. The resonance condition in the excited-state manifold for a Raman process $|0\rangle \rightarrow |1\rangle$ is achieved for $\omega_q = \nu = 1.27\Gamma_{1\text{D}}$ [Fig. 2(d)]. This condition can be met by choosing a TLS with matching transition energy and/or by Purcell enhancing the waveguide decay rate [48–50].
The CPB qubit is defined by a single Cooper pair oscillating on and off a superconducting island. We simulate the electric-field strength coming from two electrons on the island in order to estimate the Stark shift in the QD. Self-assembled In(Ga)As QDs with transform-limited linewidths [25] and near-unity $\beta$ [26] have been reported to exhibit a Stark coefficient $|\beta|$ = 2$\pi$×100 MHz/(kV/m) [41]. From the electric-field strength we find a Stark coupling $g_s = 2\pi \times 0.4$–1 GHz for a separation of $d = 0$–100 nm between qubit and waveguide, with the QD in the middle of the waveguide [Fig. 4(c)].

We also simulate the optical field in this configuration with a three-dimensional numerical integration of Maxwell’s equations, and analyze the optical absorption by integrating the total power flow over the surface of the superconducting island. This yields the total absorbed fraction of the power, which directly translates into the photon absorption probability [Fig. 4(f)]. We assume an optical wavelength of $\lambda = 980$ nm (in air). We model the system as a 300-nm-wide nanobeam waveguide made of GaAs with refractive index $n_{GaAs} = 3.456$ [51] suspended in vacuum. We assume negligible absorption in these media, while for the superconductor the real part of the refractive index is $n_{\text{SC}} = 1.47$ and an extinction coefficient $\kappa = 9.22$, corresponding to aluminum [52].

We find the absorption of the light field into the qubit to be less than 1% for the configurations with lower coupling strengths, and slightly higher for the largest coupling strengths. We emphasize that we consider rather simple geometries, and carefully designed structures can likely improve these numbers. We note that, in the case of scattering between multiple QDs, the optical absorption is modified in a nontrivial way as photons may bounce back and forth between QDs, resulting in multiple passes. Detailed examination of this effect is beyond the scope of this paper.

Including all scattering pathways in the calculation, for coupling in the low end of our estimate $g_s = 2\pi \times 400$ MHz, a CPB qubit with $\omega_q = 2\pi \times 5$ GHz, and $\beta = 0.98$ we find $P_{\text{abs}} \approx 0.6, 13,$ and 31% for the single-QD, two-QD, and four-QD interfaces, respectively. For the strongest coupling of $g_s = 2\pi \times 1$ GHz we find $P_{\text{abs}} \approx 4, 40,$ and 78%, respectively.

The quantum transducer presents an ideal platform for long-distance entanglement. Using an interference protocol similar to Ref. [53], we consider two transducers $I_1$ and $I_2$ placed in either arm of a Mach-Zehnder interferometer [inset in Fig. 3(b)]. Photon scattering creates entanglement between the photon frequency and the SC qubit state. Mixing the red sideband fields on a beam splitter (BS) and detecting a photon creates entanglement between the qubits. For a single-photon input, the protocol succeeds with probability $P_{\text{succ}} = \eta P_k$, where $\eta$ is the detection efficiency, and produces a maximally entangled state of fidelity $F = 1$ once a photon is detected.

It is experimentally less challenging to use a weak coherent pulse with a low average photon number $\bar{n}$ instead. This reduces the fidelity, because the pulse may dephase or flip both qubits simultaneously. In Fig. 3(b), we show the fidelity and success probability for a coherent input pulse, calculated using the approach of Ref. [27]. The considered Raman protocol for coherent inputs has an intrinsic requirement $1 - F \geq 1 - P_{\text{succ}}/\eta$. Our result is close to this limit, but has a slightly lower fidelity due to elastic (Rayleigh) scattering. As shown in the figure, multi-QD transducers enable the generation of high-quality entanglement for much lower mean photon numbers. Exploiting the waveguide-mediated interactions thus reduces the possible detrimental decoherence of the SC qubit induced by the light, and allows for a near-deterministic interface between individual photons and SC qubits. The input pulse duration is mainly limited by the linewidth of the transitions and can be in the range of 50–100 ns, reducing the effect of decoherence. For comparison, superconducting qubits of the type considered here have demonstrated coherence times in the microsecond range [35].

VI. SUMMARY

In summary we have shown that long-range waveguide-mediated interactions can be exploited to boost the efficiency of quantum transducers. As a direct application, the proposed device can be used to provide an on-chip interface between SC qubits and optical photons. This could facilitate a breakthrough in long-distance quantum communication via a quantum repeater network [1–5] and scaling of SC quantum computers by connecting them optically [6,7]. Alternatively the proposed transducers can have applications for quantum limited sensing by exploiting efficient optical detection of low-frequency fields [8–10].

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APPENDIX

In this Appendix we show a numerical simulation of the Raman success probability for the two-quantum-dot transducer, but now for unequal decay rates of the two emitters. For simplicity, we have assumed that the emitters have the same coupling efficiency $\beta$, just different decay rates $\Gamma_1$ and $\Gamma_2$. We define $\Gamma_{1D} \equiv \Gamma_{1,1D} + \Gamma_{2,1D}$ and fix this sum in the comparisons. Equation (3) still holds, $\rho^{(2QD)} \approx (\Gamma_{1D} \overline{S}_A + \Gamma_{2D} \overline{S}_B)^2$, in the approximation where we only consider a single scattering path. However, the decay rates of the $|A\rangle$ and $|S\rangle$ states are modified. In order to verify whether the result of Eq. (4) remains a good approximation for unequal decay rates, we have performed a full numerical simulation including all scattering paths.

In Fig. 5 we plot the Raman-scattering probability as a function of relative emitter decay rates with a fixed sum of decay rates. We optimize with Newton’s method over the parameters $\delta$ (photon detuning) and $\Delta$ (detuning between QDs), for a fixed $k\Delta z = n\pi$ (optical phase acquired between QDs, where $n$ is any integer). The initial values for the algorithm were chosen to be equal to the optimal values for equal emitter parameters.

We find that the full numerics differs from the analytical approximation Eq. (4) by less than 7% over the range of relative decay rates differing by a factor 30. These minor differences can be attributed to imperfect convergence to the global minima in the numerical optimization procedure. The optimization landscape becomes increasingly rugged for very small absolute decay rates in either QD. Additionally, an offset is observed between the full numerics and the analytical approximation, even for $\Gamma_{2,1D}/\Gamma_{1,1D} = 1$. This may be attributed to the inclusion of all scattering paths in the numerics compared to only the most significant one in the analytical approximation. These results conclusively show robustness of our result to fluctuations in the parameters.