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Ionized gas kinematics of massive elliptical galaxies in CALIFA and in cosmological zoom-in simulations

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ABSTRACT

Context. Powerful active galactic nuclei (AGN) are supposed to play a key regulatory role on the evolution of their host galaxies by shaping the thermodynamic properties of their gas component. However, little is known as to the nature and the visibility timescale of the kinematical imprints of AGN-driven feedback. Gaining theoretical and observational insights into this subject is indispensable for a thorough understanding of the AGN-galaxy coevolution and could yield empirical diagnostics for the identification of galaxies that have experienced a major AGN episode in the past.

Aims. We present an investigation of kinematical imprints of AGN feedback on the warm ionized gas medium (WIM) of massive early-type galaxies (ETGs). To this end, we take a two-fold approach that involves a comparative analysis of Hα velocity fields in 123 local ETGs from the CALIFA (Calar Alto Legacy Integral Field Area Survey) integral field spectroscopy survey with 20 simulated galaxies from high-resolution hydrodynamical cosmological SPHgal simulations. The latter were resimulated for two modeling setups, one with and another without AGN feedback.

Methods. In order to quantify the effects of AGN feedback on gas kinematics, we measured three parameters that probe deviations from simple regular rotation by using the kinemetry package. These indicators trace the possible presence of distinct kinematic components in Fourier space (k_{lim}/k_1), variations in the radial profile of the kinematic major axis (σ_{maj}), and offsets between the stellar and gas velocity fields (Δφ). These quantities were monitored in the simulations from a redshift 3 to 0.2 to assess the connection between black hole accretion history, stellar mass growth, and the kinematical perturbation of the WIM.

Results. Observed local massive galaxies show a broad range of irregularities, indicating disturbed warm gas motions, which is irrespective of being classified via diagnostic lines as AGN or not. Simulations of massive galaxies with AGN feedback generally exhibit higher irregularity parameters than without AGN feedback, which is more consistent with observations. Besides AGN feedback, other processes like major merger events or infalling gas clouds can lead to elevated irregularity parameters, but they are typically of shorter duration. More specifically, k_{lim}/k_1 is most sensitive to AGN feedback, whereas Δφ is most strongly affected by gas inflow.

Conclusions. We conclude that even if the general disturbance of the WIM velocity is not a unique indicator for AGN feedback, irregularity parameters that are high enough to be consistent with observations can only be reproduced in simulations with AGN feedback. Specifically, an elevated value for the deviation from simple ordered motion is a strong sign for previous events of AGN activity and feedback.

Key words. Galaxy: general – galaxies: kinematics and dynamics – intergalactic medium – ISM: kinematics and dynamics – galaxies: active – galaxies: evolution

1. Introduction

Soon after the discovery that most if not all massive galaxies host supermassive black holes (SMBHs) in their centers, black hole (BH) masses were also found to be correlated with properties of their host galaxies (such as the bulge mass and the stellar velocity dispersion, e.g., Silk & Rees 1998; Gebhardt et al. 2000; Merritt et al. 2000). Such scaling relations point to coevolution between SMBHs and their galaxies with a considerable mutual influence (see the reviews by Kormendy & Ho 2013 and Heckman & Best 2014). This interaction can be split into processes that fuel the SMBH creating powerful active galactic nuclei (AGNs) and also feedback by the AGN onto the surrounding galaxy. Part of the accreted matter is transformed into prodigious energy output that heats up and expels cold gas from galaxy cores, and eventually prevents its reaccretion and, consequently, shuts down any star formation (SF; Bower et al. 2017; Raouf et al. 2019).

In fact, most cosmological simulations nowadays implement AGN feedback in some way in order to achieve, for example, a match between calculated as well as observed luminosity and mass functions for massive galaxies, groups, and clusters (for a review, see Silk & Mamon 2012). Likewise, it is necessary for predicting realistic numbers of massive early-type galaxies: active – galaxies: evolution
galaxies (ETGs) with quenched nuclei and hot gas halos (e.g., Dubois et al. 2016; Penoyre et al. 2017).

On the other hand, direct observational evidence for an interaction between the central SMBH and the host galaxy is scarce. For example, X-ray imaging of massive elliptical galaxies show heated bubbles in the surrounding medium (see e.g., the review by Fabian 2012). Parsec-scale resolution observations, which were enabled by ALMA (Atacama Large Millimeter/submillimeter Array), reveal molecular outflows that are very close to the center (Audibert et al. 2019).

In the optical regime, some galaxies display bisymmetric features in the maps of the equivalent widths (EW) of strong emission lines, which are thought to be due to centrally-driven winds (Kehrig et al. 2012; Cheung et al. 2016). In fact, earlier work already uncovered a faint warm ionized gas (Kim 1989). Meanings therein). In a SAURON-based study of Seyfert galaxies, Dumas et al. (2007), for example, observed gas velocity fields with disturbances in the nuclear regions but not in the stellar velocity fields. In this study, we examine whether VFs provide diagnostics that can be applied to the general population of galaxies that contain all SMBHs that had various phases of AGN activity during their evolution. In particular, here, we examine massive ETGs to look for kinematical patterns that could provide clues as to past or ongoing AGN activity. For this purpose, we derived quantitative irregularity parameters of VFs that were introduced to quantify the influence of interactions on cluster star-forming disk galaxies (Ziegler et al. 2009; Kutemir et al. 2008, 2010). This analysis method is explained in Sect. 2.1.

In order to explore these kinematic features in a systematic way, we use a two-fold approach and analyze both observational data (Sect. 5) and snapshots from numerical simulations (Sect. 3) that are treated in the same way as the observational data cubes. We drew a sample of 123 ETGs from the CALIFA survey of local galaxies that were processed with the pipeline PORTO3D (Sect. 5.2). For the model galaxies, we exploited cosmological simulations by using SPHGal, which incorporates physically motivated implementations of AGN feedback. Previous papers have already shown that this concept produces massive galaxies whose properties (e.g., sizes, SMBH and stellar masses, star formation rates, gas fractions) are in good agreement with observations (e.g., Hirschmann et al. 2014, 2017; Sijacki et al. 2015; Schaye et al. 2015; Choi et al. 2017). We selected a sample of 20 ETGs from zoom-in simulations, which were performed in two separate runs. One was carried out without an AGN and the other run was performed with AGN and their feedback implemented. Exactly the same 20 model galaxies were already explored by Frigo et al. (2019) to investigate the impact of AGN on the stellar kinematics (orbits) and stellar populations. We extracted various snapshots that are post-processed to treat the WIM gas phase in a way that allows for direct comparison with observations. We followed their time evolution, knowing their mass assembly and SMBH accretion histories. That way, we could systematically explore the evolution of the gas velocity fields that are subject to a variety of growth processes in addition to the effects from a central AGN. Finally, in Sect. 7, we compare the results from our observational and numerical analysis and summarize our results and conclusions in Sect. 8.

2. Theoretical framework and methods

In this section, we describe kinemetry, the method we use to analyze the kinematics of the warm gas in our data sample (Sect. 2.1). We also discuss how we determined the level of current AGN activity in simulated and observed galaxies (Sect. 2.2).

2.1. Kinemetry

In order to study the effects of AGN feedback on gas kinematics, we require spatially resolved maps of the gas velocities. The means by which these maps are generated for our simulated and observed data sets are described in Sects. 3 and 5, respectively. Once the velocity fields were available, we analyzed them based on the kinemetry method introduced by Krajnović et al. (2006), which works as follows. The observed line-of-sight velocity of a rotating disk is given by

\[ V_{\text{los}}(R) = V_{\text{sys}} + V_{\text{rot}}(R) \cos \psi \sin i, \]

where \( V_{\text{sys}} \) and \( V_{\text{rot}} \) denote the systemic and rotational velocity, respectively, \( i \) is the inclination angle, \( R \) is the projected radius, and \( \psi \) is the azimuthal angle.

It can be seen from this equation that, for a given orbit, the observed line-of-sight velocity can be expressed as a simple function of the cosine of the azimuthal angle. Equation (1) can then be generalized to a Fourier series as follows:

\[ V(R, \psi) = A_0(R) + \sum_{n=1}^{N} A_n(R) \sin(n\psi) + B_n(R) \cos(n\psi). \]

For each radius of a velocity map, a grid representing each possible ellipse position angle and flattening is generated. The best-fitting ellipse is determined by minimizing the coefficients \( A_1, A_2, B_1, A_3, \) and \( B_3 \). The values of the coefficients of this best-fitting ellipse contain information regarding the fit kinematics.

In general, the \( A_n \) and \( B_n \) coefficients do not describe the same kinematic properties. For triaxial systems, such as the ETGs in our sample, however, we were able to combine the \( A_n \) and \( B_n \) coefficients of the same order as follows:

\[ k_n = \sqrt{A_n^2 + B_n^2}. \]

Lower-order coefficients (i.e., \( k_1 = \sqrt{A_1^2 + B_1^2} \)) describe the bulk motion, or in this case simple rotation, while higher-order coefficients (\( k_3 \) and \( k_5 \)) describe deviations from simple rotation. The values of the even-order coefficients (\( k_2 \) and \( k_4 \)) should be
practically zero for point-anti-symmetric velocity fields, such as ours, and so we did not fit them. In addition, the position angle and flattening of the best-fit ellipse give additional information as to the orientation and inclination of a rotating disk, for example.

To quantify irregularities in a velocity field (VF), we exploited the analysis by kinemetry with respect to three parameters, which were first defined in Kutdenir et al. (2008, 2010), as follows:

- \( k_{3,5}/k_1 \) = \( \sqrt{A_1^2 + B_1^2 + A_2^2 + B_2^2} / \sqrt{A_1^2 + B_1^2} \), the degree of deviation from simple rotation, which is normalized to the amplitude of simple rotation of the gas kinematics,
- \( \Delta \phi \) the difference between the stellar and gas kinematic position angle (PA), and
- \( \sigma_{PA} \) the standard deviation of the gas kinematic position angles measured at different radii.

Kinemetry was initially run on the stellar kinematics at steps of 0.1 \( r_e \) from 0.1 to 1.5 \( r_e \), where \( r_e \) denotes the effective radius, in order to determine the stellar PAs. Then it was run on the gas kinematics at the same radii to determine the gas PAs, for which the position angles and flattennings of the best-fitting ellipses were allowed to vary between successive radii. From the resulting list of gas PAs, \( \sigma_{PA} \) was calculated, while a list of values for \( \Delta \phi \) was determined by subtracting the gas position angles from the stellar position angles. Finally, we ran kinemetry on the gas kinematics again, with the position angles and flattennings of the ellipses fixed to their “global” (median) values, in order to calculate values for \( k_{3,5}/k_1 \).

Here, we apply the same thresholds for the parameters as given by Kutdenir et al. (2008). They based their definitions of “irregularity” on a kinemetry analysis of isolated field galaxies from the Spitzer Infrared Nearby Galaxies Survey (SINGS, Daigle et al. 2006), which did not show any signatures of past or ongoing interactions. We thus classify a galaxy’s kinematics as “irregular” if its maximum value for \( k_{3,5}/k_1 \) is equal to or above 0.15, the maximum value of \( \Delta \phi \) is equal to or above 25°, and the value of \( \sigma_{PA} \) is equal to or above 20.

The kinemetric center of a map must be defined before it can be used with kinemetry. For the simulated data, this was trivial, as each simulated galaxy is positioned so that the center of the resulting map coincides with the center of the galaxy. For the observed galaxies, however, this is more difficult. There are several approaches to defining the kinemetric center of a galaxy, including, for example, finding the pixel with the steepest velocity gradient (Arribas et al. 1997) or the greatest velocity dispersion. Some of the harmonic coefficients \( (A_0, A_2, B_2) \) are also sensitive to incorrect definitions of the center (Krajnović et al. 2006). All of these methods assume regular kinematics, however, this is not the case for all of our data. Therefore, we define the center of an observed galaxy as the point with the greatest continuum flux within a small box around the centroid of the map; this avoids capturing bright, neighboring objects as spurious centers.

Kinemetry is programmed to automatically stop its fitting when it reaches the edge of a map. Again, this was not a problem for the simulated galaxies, which were positioned in such a way as to fully fill out their frames. For observed galaxies, it was noted that the fitting was sometimes carried out past the galaxies’ edges, resulting in incorrect parameter values, if the fitting was not manually stopped beforehand. For this reason, only the pixels that fulfilled certain criteria (e.g., sufficiently accurate velocity measurements, see Sect. 5 for more details) were used for the fitting. For some observed galaxies, this meant that only a relatively small portion of the pixels in a map were usable, and these pixels were not necessarily distributed evenly across the map. A series of tests was carried out in order to examine the effects of excluding portions of the velocity map of a simply rotating disk on the values of the irregularity parameters. We find that the main effect of excluding portions of a map is an increase in the derived values of \( k_{3,5}/k_1 \), whereas the position angle is not as significantly affected.

2.2. Spectroscopic classification after WHAN

In order to explore whether ongoing accretion-powered nuclear activity is typically accompanied by an enhanced level of irregular motions in the WIM, as a consequence of AGN feedback, one needs to first check whether an ETG shows spectroscopic evidence for an AGN. This is usually done by means of emission-line diagnostic diagrams.

In this study, we used the so-called WHAN classification scheme (Cid Fernandes et al. 2010, 2011) to identify, among our observed galaxies, those that host an AGN (see Sect. 5.2). Galaxies were assigned to one of the following four categories based on their H\( \alpha \) equivalent widths (EW(H\( \alpha \))) and their N\( \text{II}/\text{H}\alpha \) flux ratios: systems with a log[N\( \text{II}]/\text{H}\alpha > -0.4 \) are subdivided into strong AGN (EW(H\( \alpha \)) > 6 \( \AA \)), weak AGN (3 \( \leq \) EW(H\( \alpha \)) \( \leq \) 6 \( \AA \)), retired (0.5 \( \leq \) EW(H\( \alpha \)) \( \leq \) 3 \( \AA \)), and passive (EW(H\( \alpha \)) < 0.5 \( \AA \)). In our work, galaxies fulfilling the criteria of either strong or weak AGN are considered to be currently affected by the energetic output from a Seyfert nucleus.

We note that the nature of ETGs falling in the locus of retired or passive galaxies is a subject of controversy. The EW(H\( \alpha \)) of a significant fraction of these systems (e.g., ~40% of the sample of CALIFA ETGs studied by Papaderos et al. 2013) (see also Singh et al. 2013) lie within 1 \( \leq \) EW(H\( \alpha \)) (\( \AA \)) \( \leq \) 3, which is consistent with predictions from photoionization models (e.g., Cid Fernandes et al. 2011; Gomes et al. 2016) for galaxies whose ionizing radiation is solely powered by an evolved (>100 Myr) post-asymptotic-giant-branch (pAGB) stellar population. This fact has been interpreted by many authors as evidence that these retired, and no longer star-forming, ETGs lack even a weak AGN, as proposed by Cid Fernandes et al. (2010). However, this interpretation is disputed by Papaderos et al. (2013). These authors show that, in the absence of a gaseous reservoir of sufficient density, 70–90% of Lyman continuum (LyC) radiation produced by pAGB sources in most (60%) CALIFA ETGs escapes into the halo without being locally reprocessed into nebular emission. This high LyC photon escape fraction therefore implies a radical reduction of nuclear EW(H\( \alpha \))’s by \( \gtrsim 1 \) dex and, in practice, prevents detection of an AGN through optical spectroscopy. Additionally, Papaderos et al. (2013) point out that in the triaxial geometry of ETGs, the old stellar background along the line of sight can strongly dilute nuclear EWs, thereby shifting a strong Seyfert source (EW(H\( \alpha \)) \( \gg \) 6 \( \AA \)) into the locus of retired or passive galaxies. Following the above considerations, an EW(H\( \alpha \)) in the range of 0.5–3 \( \AA \) is not compelling evidence against a strong AGN in retired galaxies (RGs), but it is merely a necessary, yet not sufficient, condition for pure pAGB photoionization.

For the sake of completeness, we note that ETGs falling in the class of RGs according to the WHAN classification are usually classifiable on Baldwin, Phillips, and Terlevich (BPT) diagrams (Baldwin et al. 1981) as low-ionization nuclear emission regions (LINERs; Heckman 1980).

As for our simulated galaxies, we followed two separate runs, one with BHs and the corresponding feedback that was...
implemented and one without AGN. For the former, we quantified the activity of the AGN by the black hole accretion rate (BHAR) in comparison to the star formation rate. The time evolution of a galaxy is characterized by the growth in stellar mass through mergers and accretion.

3. Cosmological zoom-in simulations of massive galaxies

In this section, we begin with a brief description of the hydrodynamic SPH code used to simulate our sets of massive galaxies (Sect. 3.1.1), outline the simulation setup (Sect. 3.1.2), and explain the generation of velocity maps of the warm ionized gas of our simulated galaxies (Sect. 3.2).

3.1. Simulation sample

The sets of simulated galaxies that are examined in this work have been introduced by Hirschmann et al. (2017) and Choi et al. (2017), and we urge readers to consult these works for more details that go beyond the brief summary we provide here.

3.1.1. The simulation code SPHGal

The cosmological zoom-in simulations of massive galaxies were generated using the code SPHGal, which is a modified version of the smooth particle hydrodynamics (SPH) code GADGET3 (Springel et al. 2005). As outlined in Hu et al. (2014), SPHGal incorporates several refinements of the classic SPH implementation in order to pass all standard hydrodynamical tests, which have been reported to be problematic for SPH techniques in the past. Our simulation code also includes recipes for different baryonic processes, such as star formation, feedback from stars and AGN, chemical enrichment, metal-line cooling, as well as an ultraviolet photo-ionization background (Haardt et al. 2001).

Star formation and the resulting chemical evolution (described in Aumer et al. 2013 and Núñez et al. 2017) are modeled by a stochastic conversion of gas particles whose densities are above a temperature-dependent threshold, thus becoming Jeans unstable, into star particles. We assume chemical enrichment via type-Ia and type-II supernovae (SNe) and AGB stars, where we traced 11 elements (H, He, C, N, O, Ne, Mg, Si, S, Ca, and Fe) in both gas and star particles. For gas particles, we included metal diffusion to allow for a more realistic mixing of metals released into the ambient gas (Aumer et al. 2013).

Star formation is regulated by both stellar and AGN feedback. We adopted the approach outlined in Núñez et al. (2017) to account for mass, energy, and momentum release from young massive stars as well as AGB stars and SN (type-II and -Ia) explosions. AGN feedback is tied to the prescription for BH growth. BHs are represented by collisionless sink particles; a BH seed of \( 10^5 \, M_\odot \) is placed at the density minimum of any dark matter halo, whose mass exceeds \( 10^{11} \, M_\odot \). BHs can further grow via two channels: gas accretion and merger events with other BHs. Gas accretion is assumed to follow a statistical Bondi-Hoyle approach (Bondi 1952; Choi et al. 2012).

To model AGN feedback, we relied on a physically motivated approach including both mechanical and radiative feedback (Ostriker et al. 2010; Choi et al. 2017). Specifically, we incorporated the effect of AGN-driven winds, which are motivated by observed broad-absorption-line winds, by randomly kicking gas particles in the vicinity of the BH with a velocity of \( 10000 \, \text{km s}^{-1} \) perpendicular to the gaseous disk to mimic biconical gaseous outflows. We adopted a wind efficiency of 0.005 as described by Eq. (3) of Choi et al. (2017), which does not distinguish between different BH accretion regimes (i.e., independent of the Eddington ratio). In addition, we also included radiative feedback from Compton and photoionization heating due to X-ray radiation from the accreting BH, radiation pressure associated with X-ray heating, and the Eddington force (Ostriker et al. 2010). In contrast to many state-of-the-art cosmological simulations, with our AGN feedback model, our simulations predict a realistic amount of hot halo gas and X-ray luminosities, which are consistent with observations. It is important to note that in our simulations, most of the work from an accreting BH is done in the radiatively efficient mode, that is, when the BH is accreting at high Eddington ratios. As shown in various recent studies (Hirschmann et al. 2017, 2019; Choi et al. 2017, 2018; Brennan et al. 2018; Frigo et al. 2019), adopting the outlined subgrid models, and in particular the sophisticated prescription for AGN feedback, allows one to simulate massive galaxies with many realistic properties, such as star formation histories, baryon conversion efficiencies, galaxy sizes, stellar populations, gas fractions, and hot-gas X-ray luminosities.

3.1.2. Simulation setup

The initial conditions for the cosmological zoom-in simulations were drawn from Oser et al. (2010, 2012) and Hirschmann et al. (2012, 2013), adopting a WMAP3 cosmology (\( h = 0.72, \Omega_m = 0.74, \Omega_b = 0.26, \sigma_8 = 0.77 \), see e.g., Spergel et al. 2003). The dark matter (DM) haloes that were chosen to be resimulated, were selected from a “parent” dark matter-only N-body simulation, starting at \( z = 43 \), with \( 512^3 \) particles within a box with comoving, periodic boundary conditions and a box length of 72 Mpc \( h^{-1} \) (Moster et al. 2010). At \( z = 0 \), the selected DM haloes have virial masses between \( 2.2 \times 10^{12} M_\odot h^{-1} \) and \( 2.2 \times 10^{13} M_\odot h^{-1} \), All DM particles within twice the virial radius of these haloes were traced back in time, and then replaced with higher-resolution DM and gas particles with masses of \( m_{\text{dm}} = 2.5 \times 10^7 M_\odot \), and \( m_{\text{gas}} = 4.2 \times 10^6 M_\odot \), respectively (see Oser et al. 2010, for more details). Ten of the most massive resimulated haloes, which were each run with and without AGN feedback, were finally selected to be analyzed in this work.

Our AGN feedback model is very efficient in removing the majority of the warm and cool gas content of our simulated massive galaxies by \( z = 0 \). To be able to properly study the warm gas kinematics of galaxies, we consider the evolution of the gas content of galaxies only down to \( z = 0.2 \) so that a reasonably large amount of warm gas is present. A comparison to observed local massive CALIFA ETGs is then performed at \( z = 0.5 \). This comparison is justified, as by \( z = 0.5 \), our simulated galaxies have developed early-type morphologies and have masses similar to that of selected CALIFA galaxies.

3.2. Generating mock velocity maps

In order to generate mock 2D gas velocity maps of simulated galaxies, which resemble those created via integral-field spectroscopy, we used an extended version of the publicly available PYGAD analysis package. This includes a stellar population and kinematics tool as described in Frigo et al. (2019), following the analysis presented in Jesseit et al. (2007, 2009) and Naab et al. (2014).

With this post-processing code, the positions and velocities of the simulated galaxies were centered on the densest nuclear regions using a shrinking sphere technique on the stellar
component. We then calculated the eigenvectors of the reduced inertia tensor (Bailin & Steinmetz 2005) of all stellar particles within ten percent of the virial radius, and used them to align the galaxies’ principal axes with the coordinate system, such that the x-axis is the long axis and the z-axis is the short axis. In projection, the gas particles are mapped onto a regular two-dimensional grid, either with a pixel size of 0.4 kpc (at z = 0) for our examination of the galaxies’ evolution histories, or with a pixel size of 1.0 kpc for comparison with the observed CALIFA galaxies to resemble more closely the average spaxel size of CALIFA IFU data. An overview of the warm gas velocity maps generated this way is given in Fig. A.1 for the galaxies simulated with AGN feedback and in Fig. A.2 for those without AGN feedback. To finally obtain the three irregularity parameters (see Sect. 2.1) for the warm gas component of our simulated galaxies, we applied the kinemetry tool to the warm gas velocity maps as described in Sect. 2.1.

4. Ionized gas kinematics of simulated galaxies

In this section, we start by investigating the kinematics of the warm gas content and the related properties of three example simulated galaxies, which were run with and without AGN feedback. Specifically, we discuss their gas velocity maps, inclination, and projection effects on their irregularity parameters as well as the cosmic evolution of corresponding galaxy stellar masses, BH accretion rates, warm gas mass fractions, and the three irregularity parameters $k_{3.5}/k_1, \Delta \phi$, and $\sigma_{PA}$. We then continue to examine the statistics of irregularity parameters for all simulated galaxies at $z = 0.5$ and at $z = 1.3$, which were run with and without AGN feedback (Sect. 4.2).

4.1. Three case studies

We chose our three galaxy test cases such that their merger histories would be fundamentally different as follows. Galaxy 0094 has experienced a recent major merger at $z \sim 1$, galaxy 0215 has had no mergers (major or minor) at all after $z \sim 3$, and galaxy 0290 has undergone two minor mergers after $z \sim 2$.

In Fig. 1, we start by showing velocity and density maps of the warm gas of our three example galaxies 0094 (first and fourth row), 0215 (second and fifth row), and 0290 (third and sixth row) with (two left columns) and without AGN feedback (two right columns) at $z = 1.3$ (top three rows) and $z = 0.5$ (bottom three rows). In general, at $z = 1.3$, warm gas motions are more irregular and regular rotation features are not as strongly pronounced compared to lower redshifts, such as $z = 0.5$. Figure 1 also shows that AGN feedback has, on average, a more significant influence on the warm gas kinematics at $z = 0.5$ than at $z = 1.3$. Specifically, by $z = 0.5$, AGN feedback prevents to a large extent the development of an extended disk-like gas structure with ordered rotation, and additionally lowers the warm gas density due to gas heating and ejection.

By taking advantage of the gas velocity maps in Fig. 1, we computed the mean and maximum values of the irregularity parameters $k_{3.5}/k_1, \Delta \phi$, and $\sigma_{PA}$ within $1.5 r_5$ of our three example galaxies. For these calculations, we consider ten different inclinations of the galaxies between face-on ($0^\circ$) and edge-on ($90^\circ$), to explicitly study the effect of inclination on the irregularity parameters. Figure 2 depicts the mean (dashed lines) and maximum (solid lines) irregularity parameters, which are plotted pairwise against each other (different rows) for galaxies 0094 (left column), 0215 (middle column), and 0290 (right column), with a color-coded inclination angle.

4.1.1. Galaxy 0094

The galaxy 0094’s stellar mass assembly history is characterized by a major merger at $z \sim 1$ (orange lines in top left panel in Fig. 3), which, in the run including AGN, triggers a strong burst of gas accretion onto the central BH (second left panel in Fig. 3). This high rate of BH accretion in turn results in a phase of significant gas heating and ejection, so that the total galaxy stellar mass remains constant after $z \sim 1$, as in-situ star formation is strongly suppressed due to the lack of available dense gas (see also Choi et al. 2017). Also the warm gas fractions are strongly reduced after $z \sim 1$, causing subsequent fluctuations in all three irregularity parameters.

The bottom three left panels of Fig. 3 show that the values of $k_{3.5}/k_1, \sigma_{PA}$, and to a lesser extent $\Delta \phi$ are sensitive to the fraction of warm gas that is present in the galaxy. When the warm gas mass fraction strongly drops between $z \sim 1$ and $z \sim 0.7$ (a timespan of 1.5 Gyr), all three irregularity parameters significantly increase, for instance, into irregular ranges above the gray area. Then, as the warm gas mass fraction rises almost to its pre-feedback levels between $z \sim 0.7$ and $z \sim 0.3$ (a timespan of 2.9 Gyr), $k_{3.5}/k_1$ and $\sigma_{PA}$ drop sharply into regular ranges, while $\Delta \phi$ remains near 180°. Finally, when the warm gas mass fraction drops to zero shortly before $z = 0.3$, $k_{3.5}/k_1$ and $\sigma_{PA}$ rise into the irregular ranges again.

We explain these fluctuations in irregularity parameters as follows: AGN efficiently heats and removes warm gas (and it is actually also consumed via star formation). Infalling gas clouds then replenish the warm gas content, and their angular momenta govern the further gas kinematics of the galaxy, leading to counterrotation of the gas disk with respect to the stellar motion. We note that $k_{3.5}/k_1$ and $\sigma_{PA}$ appear to be quite sensitive to
Fig. 1. Velocity and density maps (with velocities overplotted as white arrows) of the warm gas content of the galaxies 0094 (first and fourth row), 0215 (second and fifth row), and 0290 (third and sixth row), at $z = 1.3$ (top three rows) and at $z = 0.5$ (bottom three rows), simulated with (first and second columns) and without AGN feedback (third and fourth columns). The line across the velocity maps is oriented at the median position angle of the best-fitting ellipses within 1.5 $r_e$, the extent of the solid line illustrates the galaxy’s effective radius. The plotted ellipses are the best-fitting ellipses at every radius with flattenings and position angles as free parameters at each radius. Following the definitions of regularity and irregularity of Kutudemir et al. (2008, 2010), regular ranges of $k_{3.5}/k_1$ and $\Delta \phi$ are illustrated by solid lines of the ellipses; the irregular $k_{3.5}/k_1$ range is illustrated by dotted lines, irregular $\Delta \phi$ by dashed lines, and irregular values of both $k_{3.5}/k_1$ and $\Delta \phi$ by dashed-dotted lines.
the amount of warm gas present and thus to past AGN activity, which is largely responsible for the removal and heating of the warm gas. Whereas, $\Delta \phi$ is likely more sensitive to changes in the angular momentum of the warm gas that is brought in via infalling gas clouds.

In the run with AGN feedback, the galaxy 0094 also undergoes a minor merger at $z \sim 2$, which is associated with a spike in the irregularity parameters (in particular $\Delta \phi$), but the values of the parameters drop quickly back to nearly zero. This is likely because no significant AGN activity is triggered: the bolometric AGN luminosity at this redshift is $2.4 \times 10^{43}$ erg s$^{-1}$, corresponding to 0.3% of the maximum Eddington luminosity, as compared to $1.9 \times 10^{45}$ erg s$^{-1}$, representing 6.8% of the Eddington luminosity at the peak in the accretion rate at $z \sim 1$.

Since AGN-driven winds originate from the BH at the center of the galaxy, we may expect that the disturbances in the gas, and thus the increased values of the irregularity parameters, should propagate radially outward over time. For Galaxy 0094, we, however, do not find a significant relation between the radius, at which $k_{3.5}/k_1$ is maximal, and the elapsed time since the peak in the BH accretion rate. This may be due to the fact that the time between output snapshots, ranging between 114 Myr and 171 Myr, is too long to properly capture the radial propagation of irregular gas motions. This is the case even if typical gas dynamical timescales are larger than the times between two snapshots, ranging between 412 Myr and 10.36 Gyr from $z = 1$ to $z = 0.2$.

Turning to the run without AGN feedback, the galaxy’s evolution is rather similar to the run with AGN feedback until the major merger event at $z \sim 1$. Without AGN feedback, this merger is associated with a brief spike in all three irregularity parameters, but the parameters quickly drop to values close to zero and stay low. The warm gas mass fraction is similarly unaffected overall, and the total stellar mass continues to rise as stars are able to form from available dense gas. This indicates that a merger can temporarily disturb the gas kinematics. However, if there is still a large amount of gas present, disturbed gas motions quickly revert to regularity and infalling gas clouds have a much smaller effect on the kinematical behavior (see, however, the description of Galaxy 0215 for a counterexample in the following Sect. 4.1.2).

### 4.1.2. Galaxy 0215

In both the run with and without AGN feedback, galaxy 0215 has a fairly quiet mass assembly history (top middle panel of Fig. 3), as it does not experience any major or minor mergers after $z = 2.8$. In the run with AGN feedback, the BH accretion rate does not show any major peaks (second middle panel of Fig. 3), remaining mostly constant until $z = 0.2$, and the warm
gas mass fractions do not exhibit any major decreases, which are typically associated with peaks in AGN activity and feedback. Consequently, the parameters stay within the regular range for the course of most of galaxy 0215’s evolution (fourth, fifth, and sixth middle panels of Fig. 3).

Differences in the runs with and without AGN feedback begin to arise at $z \sim 0.8$. While the irregularity parameters do not increase over cosmic time in the run with AGN feedback, in the run without AGN feedback, around $z \sim 0.6$, a gas cloud falls into galaxy 0215. This is indicated by the strong increase in the warm gas mass fraction (blue line in third middle panel of Fig. 3). As a consequence, $\Delta \phi$ immediately rises up to around $180^\circ$ in the run without AGN feedback, while the other parameters stay low. Only around $z \sim 0.2$, do $k_{3,5}/k_1$ and $\sigma_{PA}$ also begin to rise, thus reacting to the decreasing warm gas mass fraction as a consequence of gas consumption via star formation.

We conclude that irrespective of AGN feedback, an infalling gas cloud can cause the orientation of a gas disk to change, resulting in high values of $\Delta \phi$. Depending on the circumstances, the gas disk may settle in its new configuration, leading to values of $\Delta \phi$ that remain high over time (i.e., counter-rotating gas disk), whereas the other two irregularity parameters $k_{3,5}/k_1$ and $\sigma_{PA}$ are not necessarily permanently increased without any significant continuous energy input, for instance, from an AGN. This suggests that $k_{3,5}/k_1$ and $\sigma_{PA}$ may be more sensitive to AGN feedback as compared to $\Delta \phi$.

4.1.3. Galaxy 0290

The evolutionary history of galaxy 0290 is similar to that of galaxy 0094, as the former also experiences a strong burst of BH activity, which is temporary even with super-Eddington accretion, at $z \sim 1.5$. However, in this case, the AGN peak is not associated with any major merger event (first and second right panels of Fig. 3). The corresponding feedback from the accreting BH causes the warm gas mass fraction to smoothly drop after $z \sim 1.5$.

A minor merger at $z \sim 1$ causes a further peak in the BH accretion rate that is followed by a more severe decline in the warm gas fractions. This decline is associated with an increase of all three irregularity parameters (fourth, fifth, and sixth right panels of Fig. 3). Even after this minor merger event, the BH of galaxy 0290 continues to episodically accrete some gas. This results in peaks of the BH accretion rate (i.e., feedback), which we find to be clearly related with spikes in the irregularity parameters, confirming our previous conclusion that gas outflows can lead to a stronger deviation from simple ordered rotation of the warm gas content.

Without AGN feedback, the minor merger at $z \sim 1$ also causes short-lived spikes in the irregularity parameters, however,

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1 This is an interesting example showing that peaks in AGN activity can be, but are not necessarily, fuelled by a merger event, (see Steinborn et al. 2018, for a statistical analysis)
with much lower values than in the case with AGN feedback. Specifically, \( \sigma_{PA} \) versus \( k_{3.5}/k_1 \) stay within the regular ranges (gray shaded areas and blue lines in fourth, fifth, and sixth right panels of Fig. 3). As seen before for galaxy 0094, without AGN feedback, irregularities in the gas motion are quickly reverted into ordered rotation.

From these three test cases of massive early-type galaxies, we may conclude that generally both merger events and high levels of AGN feedback, which are not necessarily associated with mergers, can lead to a severe lack of coherent motions of the warm gas content. This is reflected by an increase of all three irregularity parameters. However, without any energy or momentum release due to a central AGN, the perturbed gas motions typically return to ordinary rather quickly after a merger event leading to an immediate decrease of the irregularity parameters. Solely \( \Delta \phi \), that is, the deviation of gaseous rotation from stellar rotation, can be increased for longer durations of time simply as a consequence of a large infalling gas cloud, as it may change the angular momentum of the warm gas. Nevertheless, bursts in AGN activity (not necessarily related to merger events, though) and associated AGN feedback are necessary to produce longer-term disordered gaseous motions and related permanent high levels of all three irregularity parameters as a consequence of heating and ejecting warm gas and to large extent preventing its reaccretion back onto the galaxy (see Brennan et al. 2018).

### 4.2. Sample of 20 simulated massive galaxies

In this section, we investigate the statistics of the irregularity parameters of our full galaxy sample, which was run with and without AGN feedback. The irregularity parameters of each galaxy were calculated at 25 random projections. Since the maximum values of these parameters (computed within \( r_{re} \)) are generally more sensitive to AGN activity, the warm gas content, and the orientation of each galaxy than the mean values, we present the statistics of the maximum values for the remainder of this article.

Figures 4 and 5 show \( k_{3.5}/k_1 \) versus \( \sigma_{PA} \) (top row), \( \Delta \phi \) versus \( \sigma_{PA} \) (middle row), and \( \Delta \phi \) versus \( k_{3.5}/k_1 \) (bottom row) for all ten simulated galaxies with (orange, left column) and without (blue, right column) AGN feedback, at \( z = 1.3 \) and \( z = 0.5 \), respectively. The irregularity parameters for edge-on orientation (i.e., uncommitted by any spurious increase caused by face-on orientations, as explained in Sect. 4.1) are shown by the triangles. In order to additionally represent the range of irregularity parameters spanned for various galaxy orientations, the contours represent the kernel density estimates of the irregularity parameters for each galaxy in our sample at 25 different, randomly chosen orientations, which are color-coded by number density.

A priori, we would expect galaxies with AGN feedback to have higher irregularity parameters than those without since the gas in galaxies with AGN is exposed to energy and momentum injection from the central accreting BH, in addition to other sources of disturbance, such as mergers and stellar feedback. However, as we have also seen for the three test cases (Sect. 4.1), infalling gas may also lead to sustained high values of \( \Delta \phi \), irrespective of AGN feedback.

Figure 4 shows that at \( z = 1.3 \), AGN feedback does not strongly affect the irregularity parameters yet: irrespective of feedback, their values hardly exceed the regular boundaries (dashed lines) independent of the projections of the simulated galaxies. Only with AGN feedback does the \( k_{3.5}/k_1 \) parameter extend up to slightly larger values (\( k_{3.5}/k_1 < 0.5 \)) as opposed to when it is without AGN feedback (\( k_{3.5}/k_1 < 0.2 \)). Specifically, for galaxies at edge-on projection (triangles), Fig. 4 additionally illustrates that the irregularity parameters of seven and six out of ten galaxies with and without AGN feedback, respectively, lie within the regular range (dashed lines) of the \( k_{3.5}/k_1 \) versus \( \Delta \phi \) panels (top row). Fully irrespective of AGN feedback, eight of ten edge-on projected galaxies reside in the regular range of the \( \sigma_{PA} \) versus \( \Delta \phi \) and of the \( \sigma_{PA} \) versus \( k_{3.5}/k_1 \) panels (middle and bottom rows).

At \( z = 0.5 \), however, the situation changes, which is consistent with our a priori expectation: the density contours of Fig. 5 illustrates that the ranges of all three irregularity parameters, in particular \( \sigma_{PA} \) and \( k_{3.5}/k_1 \), extent to significantly higher values for galaxies with AGN feedback than for those without this process. This points toward a strong impact of AGN feedback on largely destroying any ordered rotation or motion of the warm gas content as well as distorting any alignment with the stellar motion. Specifically for galaxies in edge-on view, we find that with AGN feedback three, five, and four out of ten galaxies reside within the \( k_{3.5}/k_1 \) versus \( \Delta \phi \), the \( \sigma_{PA} \) versus \( \Delta \phi \), and the \( \sigma_{PA} \) versus \( k_{3.5}/k_1 \) panels, respectively. Whereas without AGN feedback, the vast majority of galaxies have regular kinematic features (7/10, 8/10, and 9/10, respectively).

Table 1 summarizes the means and standard deviations of the maximum values of the irregularity parameters for the edge-on projected galaxies at \( z = 1.3 \) and \( z = 0.5 \), which indicates a similar conclusion as discussed for Figs. 4 and 5. The average irregularity parameters of galaxies at \( z = 1.3 \) are similar with and without AGN feedback. In fact, the kinematics of galaxies without AGN feedback can be even slightly less regular than those with AGN feedback. However, at \( z = 0.5 \), the average irregularity parameters are higher with AGN feedback than without. This difference is more pronounced for \( k_{3.5}/k_1 \) and \( \sigma_{PA} \) as compared to \( \Delta \phi \), as the latter parameter may also increase for galaxies without AGN feedback due to infalling gas clouds.

### 5. Observational data from the CALIFA survey

In this section, we briefly describe the source of our observed data (Sect. 5.1) before detailing the means by which the data were cleaned and analyzed (Sect. 5.2).

#### 5.1. The CALIFA survey

The Calar Alto Legacy Integral Field Area Survey (CALIFA, Sánchez et al. 2012, 2016) investigated a representative sample of galaxies in the local Universe, encompassing a wide range of morphologies and luminosities. It explored the diversity in basic characteristics, such as the kinematics of their stars and gas, the emission properties of their ionized gas, and their stellar populations, which were spatially resolved to scales between 400 pc and 1200 pc. The galaxies were diameter-selected to fit an extent of two half-light radii onto the spectrograph instrument field. From an SDSS-based “mother sample” of 937 galaxies, 667 were observed having redshifts between 0.005 and 0.03. Two thirds have late-type, disk-dominated morphologies, while in our study, we concentrate on the ~200 ETGs in order to match the simulated objects that are all spheroidal at \( z = 0 \).

The observations were carried out using the PMAS/PPak spectrograph (Potsdam Multi Aperture Spectrograph; Roth et al. 2005; Kelz et al. 2006) that is mounted on the Calar Alto observatory’s 3.5m-telescope. This instrument features a $74'' \times 62''$ hexagonal field of view (FoV). We note that 331 fibers of 2.7” sample the FoV and 36 fibers further sample the sky near the
Fig. 4. $\sigma_{PA}$ vs. $k_{35}/k_1$ (top row), $\sigma_{PA}$ vs. $\Delta \phi$ (middle row), and $k_{35}/k_1$ vs. $\Delta \phi$ (bottom row), for simulated galaxies with AGN feedback (left column) and without AGN feedback (right column) at $z = 1.3$. The triangle-shaped markers represent the maximum values within 1.5 $r_e$ for our galaxies inclined edge-on, while the colored contours represent the range of maximum values exhibited by each of our galaxies at 25 random orientations. The dashed lines indicate the upper boundaries of the parameter ranges within which a galaxy’s kinematics are considered regular.

For our study, we selected 123 early-type CALIFA galaxies, whose V500 data were processed by PORTO3D in exactly the same way as described by Papaderos et al. (2013) and Gomes et al. (2016) for a subsample of 32 ETGs, which were examined with respect to the kinematics and emission characteristics of their warm gas component. PORTO3D is a pipeline designed to perform post-processing and spectral fitting of IFS data. After data quality was assessed, individual spectra (per spaxel) were extracted, deredshifted, rebinned to 1 Å, and fit with the publicly available stellar population synthesis code STARLIGHT (Cid Fernandes et al. 2005). Spectral fits were computed spaxel-by-spaxel using a base of simple stellar populations (SSPs) from both Bruzual & Charlot (2003) and MILES (Sánchez-Blázquez et al. 2006; Vazdekis et al. 2010; Falcón-Barroso et al. 2011), covering a range of ages between 5 Myr and 13 Gyr. The results from these two modeling runs were combined in order to derive the most likely stellar population vectors and their main properties (e.g., stellar metallicities and ages). For each of these modeling runs, the best-fitting stellar continuum was then subtracted from each spaxel to create pure FoV. Observations were carried out at low ($V500$, $R \sim 850$, and spectral coverage is between 3750 Å and 7500 Å) and medium ($V1200$, $R \sim 1700$, and spectral coverage is between 3700 Å and 4200 Å) spectral resolution, with each galaxy covered by two to three dithered exposures per mode. Once the raw data were taken, they were processed by the CALIFA pipeline (Husemann et al. 2013), which removes cosmic rays, carries out flux calibration and extinction corrections, and interpolates the data onto a 78′′ $\times$ 72′′ grid. All processed data cubes were made public and provided to the community via regular data releases, the final one being the DR3 (Sánchez et al. 2016).
Fig. 5. $\sigma_{PA}$ vs. $k_{3.5}/k_1$ (top row), $\sigma_{PA}$ vs. $\Delta\phi$ (middle row), and $k_{3.5}/k_1$ vs. $\Delta\phi$ (bottom row), for simulated galaxies with AGN feedback (left column) and without AGN feedback (right column) at $z = 0.5$. The triangle-shaped markers represent the maximum values within 1.5 $r_e$ for our galaxies inclined edge-on, while the colored contours represent the range of maximum values exhibited by each of our galaxies at 25 random orientations. The dashed lines indicate the upper boundaries of the parameter ranges within which a galaxy’s kinematics are considered regular.

Table 1. Means and standard deviations of the maxima of irregularity parameters for simulated galaxies with and without AGN feedback at $z = 1.3$ and $z = 0.5$.

<table>
<thead>
<tr>
<th></th>
<th>$z$</th>
<th>$\mu$(Max. $k_{3.5}/k_1$)</th>
<th>$\sigma$(Max. $k_{3.5}/k_1$)</th>
<th>$\mu$(Max. $\Delta\phi$)</th>
<th>$\sigma$(Max. $\Delta\phi$)</th>
<th>$\mu$((\sigma_{PA}))</th>
<th>$\sigma$((\sigma_{PA}))</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1.3 AGN</td>
<td>0.12</td>
<td>0.06</td>
<td>14.81</td>
<td>15.93</td>
<td>3.12</td>
<td>1.75</td>
</tr>
<tr>
<td></td>
<td>NoAGN</td>
<td>0.11</td>
<td>0.05</td>
<td>20.08</td>
<td>19.07</td>
<td>3.76</td>
<td>2.87</td>
</tr>
<tr>
<td></td>
<td>0.5 AGN</td>
<td>0.30</td>
<td>0.42</td>
<td>52.70</td>
<td>56.81</td>
<td>7.66</td>
<td>7.79</td>
</tr>
<tr>
<td></td>
<td>NoAGN</td>
<td>0.10</td>
<td>0.06</td>
<td>41.30</td>
<td>62.87</td>
<td>3.31</td>
<td>1.12</td>
</tr>
</tbody>
</table>

emission-line maps, which were in turn combined to improve on the determination of EWs and velocity centroids of emission lines. PORTO3D incorporates a number of routines that allow for a precise subtraction of the best-fitting stellar continuum and, most importantly, a continuum rectification technique that eliminates small-scale residuals in spectral fitting and permits reliable extraction of weak emission lines at a level of <1 Å in equivalent width. This way, two-dimensional maps with various quantities of interest were computed for all ETGs in our sample. These maps include the stellar and H$\alpha$ velocity and velocity dispersion, and their uncertainties, H$\alpha$ fluxes and EWs, and the [N II]/H$\alpha$ flux ratio for every spaxel. The interpolated spaxel scale of the CAL-IFA data ($1'' \times 1''$) corresponds on average to a spatial resolution of 0.5–1 kpc at the galaxies’ typical distances (100–200 Mpc). As with the simulated galaxies, we did not perform any binning on the maps in order to preserve small-scale features.

We did, however, perform smoothing and masking on the velocity maps in the following manner. First, the H$\alpha$ velocity
map \((V_\alpha)\) was median-filtered with a radius of 1 pixel (resulting in \(V_\alpha\_med1\)) and 2 pixels (resulting in \(V_\alpha\_med2\)), including the central pixel. Then, the relative absolute difference between the input velocity map and \(V_\alpha\_med1\) was calculated. Pixels with particularly high (\(>0.67\), an empirically determined cut-off) relative absolute differences were set to zero (bad), and pixels with very low relative absolute differences (\(<10^{-7}\)) were also set to zero because large, contiguous blocks of undefined velocities all have the same value after median filtering, resulting in very low relative absolute differences. The remaining pixels were set to one (good), resulting in a “mask” differentiating between dubious and useful pixels. The resulting set of good pixels was then adaptively filtered with ESO-MIDAS, using the algorithm by Richter et al. (1991), which smooths maps based on the local gradient. This smoothed image \((V_\alpha\_adap)\) was then also median-filtered (resulting in \(V_\alpha\_med\_adap\)) and the absolute relative difference between \(V_\alpha\_adap\_med\) and \(V_\alpha\_adap\) was calculated. Finally, the pixels in the original map \((V_\alpha)\) with values of this second absolute relative difference greater than 0.67 were replaced by their corresponding values in \(V_\alpha\_adap\_med\) and the bad pixels in \(V_\alpha\) were replaced with their respective values in \(V_\alpha\_pre\_smooth\). A final mask consisting of the previously mentioned one and zero values (and further values, such as \(-1001\) for pixels outside the FoV and \(<-1001\) for previously masked regions, such as foreground stars) was also output, and only the pixels marked as one in the final, smoothed map were used for our analysis.

Of the 123 total galaxies (our full sample), we further selected a subsample of 49 galaxies (the clean sample) by visually inspecting both the original and smoothed H\(\alpha\) velocity maps to ensure the presence of a relatively well defined, nearly contiguous velocity field. This was done in order to avoid a possible spurious increase in \(k_{\text{rad}}/k_{\text{med}}\) caused by gaps in the map (as explained above). However, this may have introduced a bias in favor of relatively gas-rich galaxies with an EW(H\(\alpha\)) of typically 1–3 \(\AA\) over their entire extent (type i and ii as well as ETGs in the notation by Papaderos et al. 2013, and Gomes et al. 2016). In addition to disturbing the gas in a galaxy, AGN feedback can also remove it. This effect is ignored if one excludes the gas-poorer galaxies, that is, systems falling in the type ii ETG class defined in Papaderos et al. (2013). Therefore, in the following, we present statistics for both the full and the clean sample. The smoothed H\(\alpha\) velocity maps of these 49 galaxies are presented in Fig. A.3. The data were analyzed in the same manner as the data from the simulations (see Sect. 3). We present the results of this analysis in the coming subsections.

We assume that AGN feedback is a ubiquitous process and thus that all the galaxies in our sample have been influenced by it at some point, but perhaps there is an enhanced effect if the galaxy is currently active. The activity status was assessed with a WHAN analysis (see Sect. 2.2), allowing the division into strong and weak AGN, on the one hand, and the remaining inactive ones, consisting of retired and passive galaxies, on the other (Fig. 6). For this classification, we used the mean nonzero EW(H\(\alpha\)) and log[N/H] values per spaxel for each galaxy. When we present the statistics of the values of the irregularity parameters in the coming subsections, we present them separately for these two populations.

6. Gas kinematics of CALIFA galaxies

In this section, we begin by examining the values of irregularity parameters at specific radial bins for three test cases (Sect. 6.1) before investigating the statistics for the entire sample in Sect. 6.2, as we did in Sect. 4.2.

6.1. Three case studies

We present velocity maps of the warm gas of NGC0932, NGC 6146, and UGC 10205 (Fig. 7) and examine at which radial bin the irregularity parameters have values exceeding the threshold for undisturbed disk rotation. The radial coverage between 0.1 \(r_e\) and 1.5 \(r_e\) is subdivided into 15 bins. In Table 2, we list the means, maxima, and minima of the three irregularity parameters and the radii at which they show irregularity, if any.

6.1.1. NGC 0932: Current AGN activity

NGC 0932 is, on average, regular in all three parameters at all radii. In fact, it is the only galaxy in our sample whose maximum values for all three parameters fall within the regular range. A visual inspection of the gas velocity map reveals a slight irregularity in the center, which may be due to the presence of an AGN (as indicated by the WHAN analysis). The map of the H\(\alpha\) flux reveals high values in the center of the galaxy as well as in a fragmented ring-like structure around the galaxy’s edge. This structure is located more than 1.5 \(r_e\) away from the center and would thus not normally be analyzed. However, we extended the fitting to the galaxy’s edge and found that \(k_{\text{rad}}/k_{\text{med}}\) was relativel high (\(-0.10\)) in the center. This corresponds closely to the feature in the H\(\alpha\) flux map, which falls to \(-0.04\) for most of the radial extent before rising to 0.09 again in the very outermost radius, apparently following the H\(\alpha\) flux distribution. We note that \(\Delta \phi\) also follows this trend, but not as closely. Overall, we find that \(k_{\text{rad}}/k_{\text{med}}\) and \(\Delta \phi\) react to disruption caused by AGN feedback in the center, and stellar feedback in the outer ring, of this galaxy.

6.1.2. NGC 6146: No current AGN activity

NGC 6146 is irregular with respect to \(k_{\text{rad}}/k_{\text{med}}\) at radii 9, 10, 11, 12, 13, 14, and 15, corresponding to 13′′5, 15′′1, 16′′6, 18′′1, 19′′6, 21′′1, and 22′′6, respectively. It is irregular with respect to \(\Delta \phi\) at radii 11, 12, 13, and 14, which correspond to 16′′6, 18′′1, 19′′6, and 21′′1, respectively. Additionally, its \(\sigma_{PA}\) value is regular.
The maximum values for $k_3.5/k_1$ and $\Delta \phi$ fall outside the regular ranges, but in different regions for UGC 10205. We note that $k_3.5/k_1$ tends to be irregular in the middle to outer parts of the studied area (radii 10, 11, 12, 13, and 14, or 19′/4, 21′/3, 23′/2, 25′/2, and 27′/2), while $\Delta \phi$ is irregular in the inner parts (radii 1, 2, and 3, or 1′/9, 3′/9, and 5′/8).

There is a degree of twisting present in the inner portions of the gas kinematics, but not the stellar kinematics, which could indicate triaxiality with respect to kinematics in the same manner as isophotal twist. The different degrees of twisting would explain the increased values of $\Delta \phi$ in the center. Indeed, there appears to be a lane of Hα-emitting gas that is present along the major axis of the galaxy, with a twist near the center (see Fig. 7). This would explain these elevated $\Delta \phi$ values. The elevated values of $k_3.5/k_1$ toward the edge of the galaxy may be a reaction to the decreased amounts of warm gas, as with NGC 6146.

### 6.2. Observational sample of 49 CALIFA galaxies

In this section, we present the general statistics of our observed sample. Figure 8 shows an overview of the values of $k_3.5/k_1$ versus $\sigma_{PA}$ (top row), $\Delta \phi$ versus $\sigma_{PA}$ (middle row), and $\Delta \phi$ versus $k_3.5/k_1$ (bottom row) for those galaxies in our clean sample that we determined via the WHAN analysis to be currently AGN-affected (left column) and not currently AGN-affected (right column). As already pointed out in Sect. 2.2, the latter objects, which are classified as retired or passive according to WHAN, fall in their majority on the locus of LINERs in BPT.
diagrams. Additionally, they could therefore host some level of accretion-powered nuclear activity which, due to an extensive LyC photon escape, evades detection through optical emission-line spectroscopy. The round markers represent the maximum values of the irregularity parameters within the observed radial range (1.5 $r_e$), and the dashed lines indicate the boundaries of the parameter ranges within which a galaxy’s kinematics are considered to be regular with respect to each parameter in a similar manner to Figs. 4 and 5 in Sect. 4.2. In order to facilitate comparison with the simulations, we have also included the kernel density estimate contours for the values of the irregularity parameters for the simulated galaxies with AGN feedback at 25 different, randomly chosen orientations at $z = 0.5$ from Fig. 5. We performed the comparison in this manner because our simulated galaxies with AGN feedback at $z = 0.5$ are the closest proxies to our observed galaxies. This is because all observed galaxies are assumed to have felt the effects of AGN feedback, and $z = 0.5$ is the latest time at which all of the simulated galaxies in our sample have substantial amounts of warm gas. The comparison is discussed in more detail in the following section.

Of the full sample of 123 galaxies, the harmonic fit performed by kinemetry did not converge for nine galaxies, and thus they are excluded from our analysis. Table 3 presents an overview of the mean values and standard deviations of the maximum values of the irregularity parameters within 1.5 $r_e$ for the full sample (123 galaxies) and the clean sample (49 galaxies). In this table, we also present separate statistics for the case in which we include RGs in the sample bin with currently AGN-active and nonactive galaxies.

For the clean sample, current AGN activity does not enhance any irregularity parameters. In fact, it slightly reduces the observed parameter range. Of the clean-sample of currently-AGN-affected galaxies, 1/9 is regular with respect to $k_3,5/k_1$ versus $\Delta \phi$, 1/9 is regular with respect to $\Delta \phi$ and $\sigma_{PA}$, and 2/9 are regular with respect to $k_3,5/k_1$ and $\sigma_{PA}$. The range of maximum $k_3,5/k_1$ values exhibited is 0.08–0.40, the range of maximum $\Delta \phi$ values is 18.0°–87.08°, and the range of $\sigma_{PA}$ values is

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**Fig. 8.** $\sigma_{PA}$ vs. $k_3,5/k_1$ (top row), $\sigma_{PA}$ vs. $\Delta \phi$ (middle row), and $k_3,5/k_1$ vs. $\Delta \phi$ (bottom row), for observed galaxies with (left column) and without (right column) current AGN activity. The colored contours represent the range of values exhibited by each simulated galaxy at 25 random orientations. Only galaxies simulated with AGN feedback were included. The round markers represent the maximum values within 1.5 $r_e$ for observed galaxies. The dashed lines indicate the upper boundaries of the parameter ranges within which a galaxy’s kinematics are considered regular.
2.11–17.68. Without current AGN activity, these numbers are 2/40, 10/40, and 10/40, respectively. The range of maximum $k_{3.5}/k_1$ values is 0.04–1.94, the range of maximum $\Delta \phi$ values is $6.87^\circ$–179.03$^\circ$, and the range of $\sigma_{PA}$ values is 1.15–71.82. The galaxies mostly span the parameter ranges evenly, with galaxies tending to cluster more closely at lower parameter values while still mostly remaining outside the regular ranges.

Both the means and the standard deviations of the maxima of the parameters are significantly lower for currently AGN-affected galaxies than for currently AGN-unaffected galaxies in the clean sample. We find variations of this result when we explore the full sample or include RGs (lines 3–8 in Table 3). In all cases, currently AGN-affected galaxies exhibit lower irregularity parameter values and, in many cases, lower scatter than currently non-AGN-affected galaxies.

A reason for this result could be that AGN feedback becomes more efficient after the peak in the accretion rate, as self-regulation means that feedback reduces the accretion rate. Thus, current AGN activity indicates both a lack of previous recent feedback and a reservoir of gas that is available for accretion; they both tend to reduce the values of the parameters.

### 7. Comparison between simulations and observations and discussion of results

In this section, we compare the results from our observed and simulated data samples and discuss some caveats of our analysis. Figure 8 shows that the observed galaxies follow the contours of the simulated galaxies with AGN feedback at different orientations fairly closely. As we have seen, it is important to keep in mind that orientations that are close to face-on can increase the values of the parameters, in both simulations and observations, as well. Nonetheless, we find that AGN feedback is a necessary process that is adopted in simulations to be more consistent with the range of observed irregularity parameters, whereas without AGN feedback, the extent of irregularity parameters would be significantly too small.

In total, the observed galaxies tend to occupy wider parameter ranges. For the clean observed sample, the maximum values of $k_{3.5}/k_1$ range from 0.08 to 0.40 for currently AGN-affected galaxies and from 0.04 to 1.94 for currently unaffected galaxies, or 0.04 to 1.94 overall, compared to 0.03 to 1.51 for the galaxies simulated with AGN feedback. The observed galaxies display $\Delta \phi$ values of $18.0^\circ$ to $87.08^\circ$ (current AGN) and $6.87^\circ$ to 179.03$^\circ$ (no current AGN), or $6.87^\circ$ to 179.03$^\circ$ overall, compared to 4.81$^\circ$ to $180.0^\circ$ for the simulated galaxies. Finally, the maximum values of $\sigma_{PA}$ range from 2.11 to 17.68 for currently AGN-affected galaxies and 1.15 to 71.82 for currently non-AGN affected clean-sample observed galaxies, or 1.15 to 71.82 overall, compared to 1.26 to 28.01 for the simulated galaxies. The differences are most striking for $k_{3.5}/k_1$, for which the parameter range is 28% larger for observed galaxies, and $\sigma_{PA}$, for which the parameter range is 164% larger. We discuss possible reasons for these differences in the next subsection.

As we saw with the three observed case studies (Sect. 6.1), high irregularity parameter values correlate with regions of strong Hα emission, such as central regions near an active nucleus or star-forming rings closer to the periphery, where stellar feedback distorts gas kinematics. High irregularity parameter values were also measured in regions with minimal flux in the outer areas of galaxies. As we saw with the simulated case studies in Sect. 4.1, the irregularity parameters, especially $k_{3.5}/k_1$ and $\sigma_{PA}$, are sensitive to the level of energy input from feedback sources as well as the amount of warm gas that is present.

There are several reasons why we presume the observed galaxies present higher values for the irregularity parameters than for the simulated galaxies. First, as several spatially resolved studies of ETGs with wide-FoV IFS arrays have revealed, these seemingly simple systems actually show a remarkable degree of morphological and kinematical complexity both in their WIM and stellar component (e.g., Gomes et al. 2016). For instance, their stellar kinematics exhibit a wide heterogeneity – ranging from overall pressure-supported to rotational patterns, and even counter-rotating components or rotation along the galaxy’s minor axis. Likewise, their WIM also shows a kinematical diversity – from a complete lack of coherent motions all the way to ordinary rotation throughout the galaxy extent, or within an oblate component (Sarzi et al. 2006), with cases of kinematically distinct outflows or ionization cones (Kehrig et al. 2012), which are referred to as gas flows or rotation in some cases (Roy et al. 2018).

Secondly, a quantification of the degree of irregularity in the WIM becomes even more challenging due to the variation of these characteristics as a function of galactocentric radius. The WIM may actually be affected by a superposition of different gas excitation mechanisms, such as AGN-driven inflows, AGN-driven outflows, and ionization cones with low-level star formation (e.g., Trager et al. 2000; Salim et al. 2012). For instance, Papaderos et al. (2013) describes two main classes of radial EW(Hα) profiles for ETGs: type I systems (~40% of their sample) show a radially constant EW(Hα) of 0.5–2.4 Å (hereafter EW(Hα)_0, or ~40% of their sample) show a radially constant EW(Hα) of 0.5–2.4 Å (hereafter EW(Hα)_0, or PAGB photoionization models. On the contrary, type ii ETGs (~60%) are characterized by positive EW(Hα) gradients with a central EW(Hα)<0.5 Å that gradually raises to EW(Hα)_0 in the galaxy periphery. The faintness of line emission in the central parts of type ii ETGs presumably reflects an inwardly decreasing (increasing) WIM density (LyC photon escape fraction J_{LyC}), and obviously strongly impedes studies of gas kinematics. The
situation is further complicated by faint star-forming spiral-like features in the periphery of some type i ETGs (classified as i+ by Gomes et al. 2016) that locally give rise to EW(Hα) values >10 Å, that is, several times larger than EW(Hα)pABG. Such fine features, which are traceable in i and ETGs on scales of a few arcsec (e.g., NGC 932), are definitely beyond the resolution of our simulations.

Furthermore, the inherent kinematical complexity of ETGs might be slightly enhanced by noise in the observational data. This is because of the generally very faint emission (on the order of 0.5–3 Å) in most of these systems that, depending on the quality of fitting and subtraction of the underlying stellar continuum, leaves uncertainties of typically no less than ~20 km s$^{-1}$ in velocity determinations for individual spaxels. Even though such small-scale random uncertainties in $V_r$ maps should leave irregularity parameters from kinemetry unaffected, an attempt was made to mimic a similar degree of noise into the simulated data by splitting each particle into 60 randomized pseudoparticles. However, this did not markedly alter the irregularity determinations for the simulated galaxy sample, as expected.

Finally, it is also possible that the implementation of AGN feedback in the simulations needs to be refined. As stated previously, AGN feedback in simulations is necessary for suppressing late, in-situ star formation and thus obtaining realistic numbers of slow-rotating, massive early-type galaxies. However, the specific implementation of AGN feedback we used may still need to be reworked, in that the warm gas is currently being heated too strongly. The other subgrid physics models that regulate, for example, stellar feedback may also need to be adjusted. Furthermore, observed galaxies are subject to additional mechanisms which can disturb their gas kinematics, such as winds driven by cosmic rays (e.g., Wiener et al. 2017) or OB stars that migrate into low-density regions after their formation (Li et al. 2015). These mechanisms were not included in the model used to generate our simulated galaxies, and their inclusion could have helped to bridge the gap.

Additionally, our spatial resolution in this study was set to 1 kpc, which is the average physical scale of the observed CALIFA data, but that could be insufficient for capturing part of the feedback phenomena expected from an AGN since, for example, collimated gas outflows might give rise to localized shocks and eventually trigger in situ star formation in the circumnuclear and peripheral zones of ETGs. The dynamic range of simulations is currently limited, however. At the moment, it is impossible to simultaneously resolve the typical Jeans length of ionized gas and accurately model the potentially massive galaxies that contain it. Stellar and AGN feedback as well as other processes, to the extent that they are understood, must be included in the form of empirically motivated sub-resolution implementations, omitting the cosmological context.

Moreover, our choice of the times at which snapshots were extracted from the simulations (typically every 100–200 Myr) might have been too coarse for optimally monitoring brief kinematical perturbations owing to AGN feedback. Even though this time resolution is finer than the typical dynamical time of the WIM (several hundred Myr for most of the considered models), it might significantly exceed the timescale for the regularization of the warm gas kinematics via differential shearing and energy dissipation through cloud-cloud collisions, as well as the visibility timescale of AGN-driven outflows and associated shocks. Also, the timescale over which kinematical perturbations in the WIM are effectively detectable, both in simulated and observed maps, likely depends on the radial dependence of various physical properties (e.g., gas density and velocity dispersion), which are poorly known for ETGs.

8. Summary and conclusions

In this article, we analyze the velocity fields of massive early-type galaxies for indications of AGN feedback processes exploiting both a simulated and an observed data sample. Zoom-in simulations with the GADEGET3-based SPHGal code were investigated of 20 objects following different merger and accretion histories conducted once with and once without full prescriptions of AGN and their feedback processes. The simulations with AGN feedback show, in general, realistic gas properties throughout cosmic history, such as less ordered rotation at $z > 1$ and a decreasing WIM mass fraction with cosmic epoch for AGN hosts. Our 114 observed local galaxies from the CALIFA survey were subdivided into AGN active as well as passive and retired galaxies according to a WHAN analysis. A further subsample was created to contain only 49 high-quality velocity fields.

We examine the velocity fields (VFs) of the warm ionized gas on spatial scales of 1 kpc with the kinemetry tool. To quantify possible peculiar features in the VFs due to AGN feedback processes, we measured three irregularity parameters with certain thresholds above which distortions are significant. These parameters encompass $k_{1.5}/k_1$ for deviations from simple orderly rotation revealing distinct kinematic components, $\Delta \phi$ for the mean angle between the orientations of the stellar and gas VFs, and $\sigma_{PA}$ for the standard deviation of the position angles of the gas VF measured at different radii spanning 1.5 $r_e$.

From the simulations, the observed galaxies, and the comparison of both, we find that:

- AGN feedback can significantly disturb regular warm gas kinematics and it often increases the values of the irregularity parameters.
- Inclination can artificially increase the values of the irregularity parameters turning an object from edge-on toward face-on.
- There is no propagation of the maxima inside-out visible after a peak in the BHAR following subsequent snapshots. However, the output intervals may have been chosen too small to see this effect.
- Interaction, in particular, major merger and accretion processes can also corrupt the gas VF and, thus, increase the values of the irregularity parameters. This increase generally vanishes quickly in the absence of AGN feedback as the gas disk settles into its new configuration.
- This new configuration may be out of alignment with the stellar component, however, keeping $\Delta \phi$ elevated. Therefore, $k_{1.5}/k_1$ and $\sigma_{PA}$ are more sensitive to the presence of AGN feedback than $\Delta \phi$.
- The distribution of the WIM component in observed local galaxies can deviate from a smooth disk and be rather heterogeneous.
- Localized regions of strong Hα emission (in central areas near an active nucleus or in star-forming rings further out) or particularly weak Hα emission (in gas-poor areas near the edge of a galaxy) can also lead to elevated values of the irregularity parameters.
- Galaxies classified as currently AGN-affected or non-AGN-affected by means of WHAN analysis do not show statistical differences in the values of their irregularity parameters. A galaxy whose BH was active in the past may still have a
disturbed VF in the present, even though the AGN’s activity has ceased.

- Simulations need a process like AGN feedback to be consistent with the large range of irregularity parameters spanned by observed massive CALIFA ETGs.

- Tensions in irregularity parameters of observed and simulated galaxies point toward deficiencies in modeling AGN feedback (or other baryonic processes).

This study has explored one way to measure the extent to which the warm gas kinematics of massive early-type galaxies can be disrupted by AGN feedback. However, since the vast majority of galaxies will feel the effects of BH activity at some point, and other phenomena such as mergers or stellar feedback can disrupt the gas VFs as well, the exact contribution of AGN feedback is hard to pinpoint. We reiterate that our sample of 20 simulated and 49 (clean sample) or 114 (full sample) observed galaxies provides only sparse statistics. Future investigations of the WIM kinematics should incorporate smaller spatial scales both in observations and simulations. The latter would also benefit from shorter timesteps between snapshots.

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References


Appendix A: Velocity maps

The following pages present an overview of the velocity maps of the simulated and observed galaxies in our sample.

Fig. A.1. Velocity maps of the warm gas in the ten galaxies in our simulated data sample with (top two rows) and without (bottom two rows) AGN feedback at z = 1.3. Each galaxy is oriented edge-on, each map has an extent of 10 × 10 kpc, and the colors scale between −350 km s\(^{-1}\) and 350 km s\(^{-1}\). The line extending across the maps is oriented at the median position angle of the best-fitting ellipses within 1.5 \(r_e\). The solid portion of the line has the length of the galaxy’s effective radius from the center along the major axis, while the dotted portion represents the remaining fit portion up to 1.5 \(r_e\). The plotted ellipses are the best-fitting ellipses at every radius; the ellipses’ flattenings and position angles were allowed to vary between radii. The standard deviation of these ellipses’ position angles is \(\sigma_{PA}\), and the position angles were compared with those of the stellar velocity to compute \(\Delta \phi\). We note that \(k_3/k_1\) was calculated based on a different set of ellipses at the same radii with fixed position angles (all oriented along the solid line) and flattenings (the median flattening of the first set of ellipses). The linestyles of the ellipses correspond to the values of the irregularity parameters as follows: a solid line means that both \(k_3/k_1\) and \(\Delta \phi\) are within the regular ranges, a dotted line means that \(k_3/k_1\) is irregular, a dashed line means that \(\Delta \phi\) is irregular, and a dashed-dotted line means that both are irregular.

Fig. A.2. Velocity maps of the warm gas in the ten galaxies in our simulated data sample with (top two rows) and without (bottom two rows) AGN feedback at z = 0.5. Each galaxy is oriented edge-on, each map has an extent of 10 × 10 kpc, and the colors scale between −350 km s\(^{-1}\) and 350 km s\(^{-1}\). The line extending across the maps is oriented at the median position angle of the best-fitting ellipses within 1.5 \(r_e\). The solid portion of the line has the length of the galaxy’s effective radius from the center along the major axis, while the dotted portion represents the remaining fit portion up to 1.5 \(r_e\). The plotted ellipses are the best-fitting ellipses at every radius; the ellipses’ flattenings and position angles were allowed to vary between radii. The standard deviation of these ellipses’ position angles is \(\sigma_{PA}\), and the position angles were compared with those of the stellar velocity to compute \(\Delta \phi\). We note that \(k_3/k_1\) was calculated based on a different set of ellipses at the same radii with fixed position angles (all oriented along the solid line) and flattenings (the median flattening of the first set of ellipses). The linestyles of the ellipses correspond to the values of the irregularity parameters as follows: a solid line means that both \(k_3/k_1\) and \(\Delta \phi\) are within the regular ranges, a dotted line means that \(k_3/k_1\) is irregular, a dashed line means that \(\Delta \phi\) is irregular, and a dashed-dotted line means that both are irregular.
Fig. A.3. Velocity maps of the warm gas in the 49 galaxies in our observed data sample. Asterisks by galaxy names denote those currently affected by AGN activity, as determined by the WHAN analysis. Only those data points contained in the “masks” (see main text) are plotted. The star in each map marks the brightest continuum pixel, which was used as the center of the map for kinematic fitting. The line extending across the maps is oriented at the median position angle of the best-fitting ellipses within 1.5 $r_e$. The solid portion of the line has the length of the galaxy’s effective radius from the center along the major axis, while the dotted portion represents the remaining fit portion up to 1.5 $r_e$. The plotted ellipses are the best-fitting ellipses at every radius; the ellipses’ flattenings and position angles were allowed to vary between radii. The standard deviation of these ellipses’ position angles is $\sigma_{\text{PA}}$, and the position angles were compared with those of the stellar velocity to compute $\Delta \phi$. We note that $k_{3,5}/k_1$ was calculated based on a different set of ellipses at the same radii with fixed position angles (all oriented along the solid line) and flattenings (the median flattening of the first set of ellipses). The linestyles of the ellipses correspond to the values of the irregularity parameters as follows: a solid line means that both $k_{3,5}/k_1$ and $\Delta \phi$ are within the regular ranges, a dotted line means that $k_{3,5}/k_1$ is irregular, a dashed line means that $\Delta \phi$ is irregular, and a dashed-dotted line means that both are irregular.