Collider constraints on Z0models for neutral current B-anomalies

Allanach, B.C.; Butterworth, J.M.; Corbett, Tyler Shane

Published in:
Journal of High Energy Physics (Online)

DOI:
10.1007/JHEP08(2019)106

Publication date:
2019

Document version
Publisher's PDF, also known as Version of record

Document license:
CC BY

Citation for published version (APA):
Collider constraints on $Z'$ models for neutral current B-anomalies

B.C. Allanach, a J.M. Butterworth b and Tyler Corbett c, 1

a DAMTP, University of Cambridge, Wilberforce Road, Cambridge, CB3 0WA, United Kingdom
b Department of Physics & Astronomy, University College London, Gower St, London, WC1E 6BT, United Kingdom
c The Niels Bohr International Academy, University of Copenhagen, Blegdamsvæj 17, Copenhagen, DK-2100, Denmark

E-mail: B.C.Allanach@damtp.cam.ac.uk, j.butterworth@ucl.ac.uk, corbett.t.s@gmail.com

ABSTRACT: We examine current collider constraints on some simple $Z'$ models that fit neutral current $B$-anomalies, including constraints coming from measurements of Standard Model (SM) signatures at the LHC. The ‘MDM’ simplified model is not constrained by the SM measurements but is strongly constrained by a 139 fb$^{-1}$ 13 TeV ATLAS di-muon search. Constraints upon the ‘MUM’ simplified model are much weaker. A combination of the current $B_s$ mixing constraint and ATLAS’ $Z'$ search implies $M_{Z'} > 1.2$ TeV in the Third Family Hypercharge Model example case. LHC SM measurements rule out a portion of the parameter space of the model for $M_{Z'} < 1.5$ TeV.

KEYWORDS: Beyond Standard Model, Heavy Quark Physics

ArXiv ePrint: 1904.10954

1Corresponding author.
1 Introduction

Data involving the effective Lagrangian operator $b\bar{s}\mu^+\mu^-$ are currently disagreeing with Standard Model (SM) predictions. Each individual measurement typically disagrees at the 2–3σ level and over many measurements, a coherent picture is emerging. In particular $R_{K^{(*)}} \equiv BR(B \to K^{(*)}\mu^+\mu^-)/BR(B \to K^{(*)}\ell^+\ell^-)$ are predicted to be 1.00 in the SM, for lepton invariant mass squared bin $m_{ll}^2 \in [1.1, 6]$ GeV$^2$. In this bin, current LHCb measurements [1, 2] imply $R_K = 0.846^{+0.054+0.016}_{-0.060-0.014}$ and $R_{K^*} = 0.69^{+0.111}_{-0.070} \pm 0.05$. The branching ratio $B_s \to \mu^+\mu^-$ [3–6] is also measured to be lower than the SM prediction, which should be accurate to the percent level. Angular distributions in the $B \to K^{(*)}\mu^+\mu^-$ decays have [7–10] a higher level of disagreement with SM predictions [11, 12], although here theoretical uncertainties in the SM prediction are significant. There are several other indications of disagreements between SM predictions and measurements and broadly speaking, the data are consistent with a beyond-the-SM (BSM) contribution to the $b\bar{s}\mu^+\mu^-$ vertex [13–20]. We call these disagreements between measurements and SM predictions the Neutral Current B-Anomalies (NCBAs). Measurements of relevant quantities from Belle II with different systematic uncertainties are eagerly awaited [21], as are updates from the LHC experiments.

The operators giving BSM contributions favoured by fits to the flavour data are

$$\mathcal{L}_{bs\mu\mu} = (\bar{b}_L\gamma^\mu s_L)(C_{LL}\bar{\mu}_L\gamma^\mu\mu_L + C_{LR}\bar{\mu}_R\gamma^\mu\mu_R) + \text{H.c.}, \quad (1.1)$$
where $C_{LL}$ and $C_{LR}$ are Wilson coefficients, with dimensions of inverse mass squared. There have been several global fits of such BSM operators that explain recent data involving $b\bar{s}\mu\mu$: [22–27]. Details of the fit methodology and results vary, but they all find that a fit involving $C_{LL} \neq 0$ and $C_{LR} \in [-C_{LL}, C_{LL}]$ can provide a significant improvement over a poor fit to the SM. There is evidence against sizeable BSM operators involving $b_R$ and $s_R$ in the global fits. For definiteness, we shall use the results of the fit of ref. [25]. There, $C_{LL} \neq 0$ only provides a good fit to NCBA data (6.5σ better than the SM prediction).

A vector-like coupling (i.e. $C_{LL} = C_{LR}$) to muons is a 5.8σ better fit than the SM at the best-fit point, whereas an axial coupling ($C_{LL} = -C_{LR}$) coupling to muons is 5.6σ better than the SM at the best-fit point.

At tree-level, a BSM contribution to $C_{LL}$ or $C_{LR}$ can come from leptoquarks and/or $Z_0$s, either of which must have flavour dependent couplings. Here, we shall focus on the $Z'$ possibility. Many models based on spontaneously broken flavour-dependent gauged U(1) symmetries [28, 29] have been proposed from which such $Z'$s may result, for example from $L_{\mu} - L_\tau$ and related groups [28, 30–62]. Some models also have several abelian groups [63] leading to multiple $Z'$s. Some other models [64, 65] generate the $b\bar{s}\mu^+\mu^-$ operator with a loop-level penguin diagram.

In ref. [66], Run I di-jet and di-lepton resonance searches (and early Run II searches) were used to constrain simple $Z'$ models that fit the NCBAs. In refs. [62, 67], the sensitivity of future hadron colliders to $Z'$ models that fit the NCBAs was estimated. A 100 TeV future circular collider (FCC) [68] would have sensitivity to the whole of parameter space for one model (MDM) and the majority of parameter space for another (MUM). However, given recent updates on LHC $Z'$ searches released by the ATLAS experiment and on the NCBAs, it seems that the time is ripe for a fresh analysis of the resulting constraints upon $Z'$ models that fit the NCBAs.

ATLAS has released 13 TeV 36.1 fb$^{-1}$ $Z' \rightarrow t\bar{t}$ searches [69, 70], which impose $\sigma \times BR(Z' \rightarrow t\bar{t}) < 10 \text{ fb}$ for large $M_{Z'}$. There is also a search [71] for $Z' \rightarrow \tau^+\tau^-$ for 10 fb$^{-1}$ of 8 TeV data, which rules out $\sigma \times BR(Z' \rightarrow \tau^+\tau^-) < 3 \text{ fb}$ for large $M_{Z'}$. These searches constrain, in principle, some of the flavourful $Z'$ models that we introduce below, but they produce less stringent constraints upon the models that we study than an ATLAS search for $Z' \rightarrow \mu^+\mu^-$ in 139 fb$^{-1}$ of 13 TeV $pp$ collisions [72]. We shall therefore concentrate upon this search, recasting it for some models that solve the NCBAs. The constraints are in the form of upper limits upon the fiducial cross-section $\sigma$ times branching ratio to di-muons $BR(Z' \rightarrow \mu^+\mu^-)$ as a function of $M_{Z'}$. At large $M_{Z'} \approx 6 \text{ TeV}$, $\sigma \times BR(Z' \rightarrow \mu^+\mu^-) < 0.015 \text{ fb}$ [73] and indeed this will prove to be the most stringent $Z'$ direct search constraint (being stronger than the others mentioned above) on the models which we study.

In section 2, we introduce simplified models $Z'$ which can provide a good fit to the NCBAs, examining the important $B_s$ mixing constraint in section 2.1. In section 2.2, we define the mixed-up muon (MUM) and mixed-down muon (MDM) simplified models, followed by the more complete Third Family Hypercharge Model (TFHM). In section 3, we describe how we recast the ATLAS $Z' \rightarrow \mu^+\mu^-$ search and outline how other Run I and Run II measurements are checked against the model. Example parameter space points for each model are listed for illustration in section 4, before the combined collider constraints
upon the models are presented. We summarise in section 5. In appendix A we define the fields. Properties of the three models studied throughout their parameter space are relegated to appendix B.

2 Models and constraints

We consider two representative models of $Z'$, following ref. [67], which introduced the naı\ve and the 33$\mu\mu$ models. The tree-level $Z'$ Lagrangian couplings that should be present in $Z'$ models in order to explain the NCBAs are

$$\mathcal{L}_{Z'} = \left( g_{sb} \overline{s}_L \overline{Z}' b_L + \text{h.c.} \right) + g_{\mu\mu} \overline{\mu}_L \overline{Z}' \mu_L + \ldots $$

A global fit to NCBAs and $V_{ts}$ in ref. [25] found that the couplings and masses of $Z'$ particles are constrained to be

$$g_{sb} g_{\mu\mu} = -x \left( \frac{M_{Z'}}{36 \text{TeV}} \right)^2,$$

if $g_{sb}$ and $g_{\mu\mu}$ are real, where $x = 1.06 \pm 0.16$ in the recent fit to the NCBAs from ref. [25]. Throughout this paper, we shall enforce eq. (2.2), typically taking the central value from the fit. In general, $g_{sb}$ and $g_{\mu\mu}$ are complex. However, here, we take $g_{\mu\mu}$ to be real and positive and $g_{sb}$ to be negative. In the models we introduce below, $g_{sb}$ may have a small imaginary part. Since the full effects of complex phases are outside the scope of this work, whenever we refer to $g_{sb}$ below, we shall implicitly refer to the real part of its value.

2.1 $B_s$ mixing constraint

$Z'$ models are subject to a number of constraints, a particularly strong one originating from measurements of $B_s - \overline{B_s}$ mixing, which constrains a function of $g_{sb}$ and $M_{Z'}$. A Feynman diagram depicting the $Z'$ contribution is shown in figure 1. The bound on a non-SM contribution depends upon the hadronic decay constant $f_{B_s}$ and bag parameter $B_s$. The experimental measurement of the mixing parameter $\Delta M_s$ is [74] $\Delta M_s^{\exp} = (17.757 \pm 0.021) \text{ps}^{-1}$. We use a determination of the SM prediction using recent lattice data and sum rules [75]

$$\Delta M_s^{\text{SM}} = (18.5^{+1.2}_{-1.5}) \text{ps}^{-1}.$$
In order to calculate the resulting bound on $Z'$ models, we follow ref. [76]. In a model inducing the BSM operator

$$\mathcal{L}^{NP} = -\frac{4G_F}{\sqrt{2}} (V_{tb} V_{ts}^*)^2 \left[ c_{sb}^{LL} (\overline{s} \gamma_\mu b_L)(\overline{t} \gamma^\mu t_L) + \text{H.c.} \right],$$

(2.4)

where $G_F = 1.1663787(6) \times 10^{-5}$ GeV$^{-2}$ is the Fermi coupling constant, the SM prediction of $B_s$ mixing is modified to

$$M_{pred} = 1 + c_{sb}^{LL}/R_{SM} \Delta M_{S}^{SM},$$

where $R_{SM} = 1.3397 \times 10^{-3}$. Our flavour changing $Z$'s induce the Wilson coefficient

$$c_{sb}^{LL} = \frac{\eta^{LL}}{4\sqrt{2}GFZ'^2}(V_{tb}V_{ts}^*)^2.$$  

(2.5)

$\eta^{LL}$ takes renormalisation between $M_{Z'}$ and $M_Z$ into account. It is a slow (logarithmic) function of $M_{Z'}$: $\eta^{LL} = 0.79$ for $M_{Z'} = 1$ TeV, whereas $\eta^{LL} = 0.75$ for $M_{Z'} = 10$ TeV (we shall be concerned here with $M_{Z'} \leq 6$ TeV). Here, we shall take $\eta^{LL} = 0.79$ whatever $M_{Z'}$, since this value gives the stronger limit out of the two numbers quoted and since $\eta^{LL}$ is quite insensitive to $M_{Z'}$ anyway. Eq. (2.3) implies the 2σ lower bound $\Delta M_{S}^{SM} > 15.5 \text{ ps}^{-1}$, leaving room for a BSM contribution to make up a shortfall to the experimental 2σ upper bound if (by substituting $|V_{tb}V_{ts}^*| = 0.04$ into eq. (2.5))

$$|g_{sb}| \lesssim M_{Z'}/(194 \text{ TeV}).$$  

(2.6)

This places a strong constraint upon $Z'$ models that explain the NCBAs [76].

2.2 Model definitions and couplings

Following ref. [62], we begin with simplified models originating from assuming that the $Z'$ only couples to left-handed quarks and to left-handed leptons. Our direct search collider constraints are not strongly dependent upon the spin-structure of the $Z'$ couplings and so this model should suffice to cover others (for example sharing the BSM operator between left-handed and right-handed muons). The $Z'$ couplings to the mass eigenstate fermions in the model are

$$\mathcal{L} = \overline{u}_L \nu L (Q) V \nu L u_L + \overline{d}_L \nu L (Q) \nu L d_L + \overline{u}_L U (L) U \nu L u_L + \overline{e}_L L (L) L \nu L e_L,$$

(2.7)

where we have written the Cabibbo-Kobayashi-Maskawa (CKM) matrix as $V$ and the Pontecorvo-Maki-Nakagawa-Sakata matrix as $U$ (see appendix 2.2 for field definitions). $\Lambda^{(Q)}$ and $\Lambda^{(L)}$ are 3 by 3 matrices of dimensionless couplings. In order to reproduce a $Z'$ coupling to left-handed muons, as required to fit the $B$-anomalies, we use

$$\Lambda^{(L)} = g_{\mu\mu} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}.$$  

(2.8)

The two simplified models introduced involve two different limiting assumptions for $\Lambda^{(Q)}$, in order to provide an estimate of how much the assumption changes predictions:

---

This inferred bound has changed in recent years due to changes in data and lattice inputs: pre-2016, the denominator was 148 TeV [19], whereas from 2016–2019 the inferred denominator became 600 TeV [76].
1. The ‘mixed-up-muon’ (MUM) model, with

\[
\Lambda^{(Q)} = g_{sb} \begin{pmatrix}
0 & 0 & 0 \\
0 & 1 & 0 \\
1 & 0 & 0
\end{pmatrix},
\] (2.9)

2. The ‘mixed-down-muon’ (MDM) model, with

\[
\Lambda^{(Q)} = g_{tt} V^\dagger \begin{pmatrix}
0 & 0 & 0 \\
0 & 0 & 1 \\
0 & 1 & 0
\end{pmatrix} V.
\] (2.10)

Matching \(\Lambda^{(Q)}\) here with eq. (2.1) identifies

\[
g_{sb} = V_{ts}^* V_{tb} g_{tt}.
\] (2.11)

In the present article, we are not concerned with the effects of small complex phases: we shall take \(g_{tt}\) to be real.\(^2\) \(g_{tt} > 0\) ensures \(g_{sb} < 0\) as required by eq. (2.2), since \(V_{ts} \approx -0.04\) and \(V_{tb} \approx 1\).

We may characterise the MUM and MDM simplified models by three important parameters: \(M_{Z'}\), \(|g_{sb}|\) and \(g_{tt}\). In practice, we shall use \(M_{Z'}\) and \(|g_{sb}|\), whilst fixing \(g_{tt}\) so as to fit the central values of the NCBAs in eq. (2.2). We note here that, since the MUM and MDM models are simplified, in reality the \(Z'\) might have more couplings than the ones introduced and so could be wider than predicted in the strict MUM or MDM limit. One could, instead of calculating the \(Z'\) width \(\Gamma\), use the MUM or MDM limit as a lower bound and allow it to vary independently of \(g_{sb}\) and \(g_{tt}\). We expect that increasing \(\Gamma\) will weaken search constraints, and so in some sense, neglecting this ‘additional width’ effect (which is the approach we shall take) is conservative.

The Third Family Hypercharge Model (TFHM) is based [61] on a \(U(1)_F\) gauge extension to the Standard Model, only the Higgs doublet, a new complex scalar SM singlet and third family fermions have non-zero \(U(1)_F\) quantum numbers. The heavy \(Z'\) comes from spontaneously breaking the \(U(1)_F\) and it is thus a more complete model than the MUM and MDM models. The model explains, in broad brush-strokes, the hierarchical heaviness of the third family of charged fermions and the smallness of CKM mixing angles. Anomaly cancellation implies that the \(U(1)_F\) quantum numbers of the third family are proportional to their hypercharges. The \(Z'\) couplings are, up to corrections \(\mathcal{O}\left(\frac{M_Z^2}{M_{Z'}^2}\right)\)

\[
\mathcal{L}_{\chi\psi} = g_F \left(\frac{1}{6} \overline{u}_L \Lambda^{(u_L)} Z' u_L + \frac{1}{6} \overline{d}_L \Lambda^{(d_L)} Z' d_L - \frac{1}{2} \overline{\nu}_L \Lambda^{(\nu_L)} \nu' L - \frac{1}{2} e_L \Lambda^{(e_L)} Z' e_L \right.
\]
\[
+ \frac{2}{3} \overline{u}_R \Lambda^{(u_R)} Z' u_R - \frac{1}{3} \overline{d}_R \Lambda^{(d_R)} Z' d_R - \overline{e}_R \Lambda^{(e_R)} Z' e_R\right),
\] (2.12)

\(^2\)Although we include the effects of phases in the CKM matrix in our numerical simulations, they are not important for our results and we ignore them in analytic discussion.
where we have defined the 3 by 3 dimensionless Hermitian coupling matrices
\[
\Lambda^{(I)} \equiv V_I^\dagger \xi V_I, \quad (2.13)
\]
\[
I \in \{u_L,d_L,e_L,\nu_L,u_R,d_R,e_R\} \text{ and }
\]
\[
\xi = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}. \quad (2.14)
\]
The $V_I$ are unitary 3 by 3 matrices in family space and $g_F$ is the dimensionless gauge coupling of $U(1)_F$. For definiteness, we shall examine the phenomenological example case introduced in ref. [61]:
\[
V_{d_L} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{sb} - \sin \theta_{sb} \\ 0 & \sin \theta_{sb} & \cos \theta_{sb} \end{pmatrix} \quad \text{and} \quad V_{e_L} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}, \quad (2.15)
\]
$V_{u_L} = V_{d_L} V_y$, $V_{u_R} = V_{d_R} = V_{e_R} = 1$. To summarise, in the TFHM example case (TFH-Meg), we have free parameters $|g_F|$, $M_{Z'}$ and $\theta_{sb}$. In practice, we vary $M_{Z'}$ and $\theta_{sb}$, setting $g_F$ so as to satisfy the central value of the NCBAs, i.e. eq. (2.2), which translates to
\[
g_F = \frac{M_{Z'}}{36 \text{ TeV}} \sqrt{\frac{24x}{\sin(2\theta_{sb})}} \quad (2.16)
\]
with $x = 1.06$.

3 Re-casting collider constraints

In its recent $Z' \rightarrow \mu^+\mu^-$ search, ATLAS defines [72] a fiducial cross-section $\sigma$ where each muon has transverse momentum $p_T > 30$ GeV and pseudo-rapidity $|\eta| < 2.5$. The di-muon invariant mass, $m_{\mu\mu} > 225$ GeV. No evidence for a significant bump in $m_{\mu\mu}$ was found, and so 95% upper limits on $\sigma \times BR(\mu^+\mu^-)$.

Re-casting constraints from such a bump-hunt in different $Z'$ models is fairly simple: we must just calculate $\sigma \times BR(\mu^+\mu^-)$ for the model in question and apply the bound at the relevant value of $M_{Z'}$ and $\Gamma/M_{Z'}$. Efficiencies are taken into account in the experimental bound and so there is no need for us to perform a detector simulation. For generic $z \equiv \Gamma/M_{Z'}$, we interpolate/extrapolate the upper bound $s(z, M_{Z'})$ on $\sigma \times BR(\mu^+\mu^-)$ from those given by ATLAS at $z = 0$ and $z = 0.1$. In practice, we use a linear interpolation in $\ln s$:
\[
s(z, M_{Z'}) = s(0, M_{Z'}) \left[ \frac{s(0.1, M_{Z'})}{s(0, M_{Z'})} \right] \exp(z). \quad (3.1)
\]
Figure 2 shows examples of such a fit for five different values of $M_{Z'}$ compared to ATLAS upper limits. One point not lying on the line is due to a statistical fluctuation in data, but generally, the figure validates eq. (3.1) as being a reasonable fit within the range
Figure 2. Examples of the fit in eq. (3.1) (shown by lines) compared to ATLAS data (shown by points), for various values of $M_{Z'}$, shown as a label by each line.

$\Gamma/M_{Z'} \in [0, 0.1]$. In general, we shall also use eq. (3.1) to extrapolate out of this range, however this will only turn out to play a rôle in part of the TFHMeg parameter space, which we shall delineate.

For the TFHMeg, we made a UFO file\(^3\) by using FeynRules [77, 78]. The MUM model and MDM model files are taken from ref. [62]. These UFO files allow the MadGraph calculation of $\sigma \times BR(Z' \rightarrow \mu^+\mu^-)$ by MadGraph 2.6.5 [79]. MadGraph estimates $\sigma \times BR(Z' \rightarrow \mu^+\mu^-)$ of the tree-level production processes shown in figure 3 in 13 TeV centre of mass energy $pp$ collisions. We use 5-flavour parton distribution functions in order to re-sum the logarithms associated with the initial state $b$-quark [80].

3.1 Constraints from Contur

Introducing the BSM terms discussed above leads to other possible new processes and signatures in $pp$ collisions in addition to the di-muon channel already considered. For example, in the TFHMeg model, the $Z'$ has a branching fraction in the range 10–20% to $b\bar{b}$, up to 40% to $t\bar{t}$ and 20–30% to $\tau^+\tau^-$. It is often produced in association with additional $b$-jets, and the cross section for associated production with an isolated photon

---

\(^3\) The UFO file is included in the Supplementary material information submitted with the arXiv version of this paper.
can be as high as a few femtobarns. Many relevant measurements of such signatures have already been made by the LHC experiments, and we use the Contur [81] tool to check whether these measurements already disfavour any of the parameter space of our model. We use Herwig7 [82, 83] and its UFO interface to calculate the cross section for all the new processes implied at the LHC by our models, and to inclusively generate the implied events. These events are then passed to Rivet [84] version 2.7, which contains an extensive library of particle-level collider measurements, especially from LHC Run I but also increasingly now from Run II. While these will not be as sensitive as individual searches using the full data set, they have the advantage of relative model-independence and ease of reinterpretation. All these measurements are in agreement with the SM, and Contur therefore treats them as SM background to a potential contribution from our models, evaluating whether the presence of an additional BSM contribution (in particular a $Z'$ mass peak) would have been visible within the experimental uncertainty. This is then converted into an exclusion limit. Previous studies [81, 85, 86] have shown that this approach typically gives a comparable sensitivity to dedicated searches and can sometimes pick up unexpected additional signatures.

4 Results

In table 1, we display one point for each model studied, where the model parameters are chosen to fit the NCBAs and to be close to the exclusion of the ATLAS di-muon search in each case. We see that each point has a narrow $Z'$: $\Gamma/M_{Z'} \leq 0.02$ (however, there are other points with larger values, as we shall see). In each model, the branching ratio into neutrinos is identical to that of muons and tagging an additional jet would result in a monojet $Z' \rightarrow$ invisible signature at the LHC. In the MUM model, we note the possible flavour changing channels $Z' \rightarrow t\bar{c} + \bar{c}t$, $Z' \rightarrow b\bar{s} + \bar{s}b$, which could also be used for searches. In the TFHMeg, decays to top pairs are 6 times more prevalent than those into muon pairs, which could prove to be an important channel for searches, as could decays into tau pairs (4 times more prevalent than muon pairs). Although these channels have a higher branching ratio than di-muons, the current bounds are sufficiently weaker such that di-muons (the only channel currently having been analysed for the full 139 fb$^{-1}$ LHC Run II dataset) provide the strongest constraint. The table is instructive by exemplifying which PDFs are important for $Z'$ production in each case. In the MDM model and the TFHMeg, $b\bar{b} \rightarrow Z'$ dominates, whereas in the MUM model, $b\bar{s} \rightarrow Z'$ dominates. The upper limit from
Table 1. Illustration of example points in parameter space. The third parameter listed in each case is derived in terms of the two above it by the best fit to the NCBAs, i.e. eq. (2.2) with $x = 1.06$. 'channel' lists the contribution to the total $Z'$ cross-section times branching ratio from the various quark parton distribution functions (PDFs). For each production mode, we list the $Z'$ fiducial production cross-section times branching ratio into muon pairs $\sigma \times BR$. Other production modes have cross-sections that are smaller than $10^{-3}$ fb. The upper limit on the cross-section is the 95% $CL_s$ bound derived from the ATLAS di-muon search \cite{72} according to eq. (3.1).

Since the ATLAS di-muon search is shown for the particular $M_{Z'}$ of the parameter point, for the narrow width limit. In what follows, we include the dependence of these upper limits upon the width, as described in section 3.

Figure 4a displays the collider constraints on the MDM model. We see that the bounds from the ATLAS di-muon $Z'$ search rule out a significant portion of parameter space that fits the central value of the NCBAs and is otherwise allowed. The shape of the various regions shown in figure 4a can be understood by looking at the properties of the model across parameter space, as shown in figure 6.

Since the $Z'$ is produced through the quark coupling, the higher $g_{sb}$, the higher the $Z'$ production cross-section, although it is suppressed by higher values of $M_{Z'}$ through the PDFs, as shown in figure 6c. Fitting the NCBAs means that $g_{\mu\mu}$ is small at small $M_{Z'}$ and large $|g_{sb}|$, as displayed by figure 6d. This region has small $BR(Z' \to \mu^+\mu^-)$, as figure 6b shows, which limits the exclusion of the ATLAS di-muon search in the top left-hand corner.
Figure 4. Collider constraints on the central fits of the models to NCBAs for (a) the MDM model, (b) the MUM model and (c) the TFHMeg. The allowed region is shown in white. Everywhere throughout the parameter plane shown, the third parameter is fixed by the central fit to the NCBAs: $g_{\mu\mu}$ as in eq. (2.2) in (a) and (b), and $g_F$ as in eq. (2.16) in (c), each with $x = 1.06$. The region marked ‘non-perturbative’ in (a) has $\Gamma_{Z'}/M_{Z'} > 1$, whereas the dotted lines display where $\Gamma_{Z'}/M_{Z'} = 0.1$ for each model (this quantity increases toward the right-hand side of each plot). The $B_s$ mixing constraint from eq. (2.6) excludes the ‘$B_s$ mixing excl’ region. In (c), the region excluded by the LEP lepton flavour universality is shown by the legend as ‘LEP LFU excl’ and is calculated in ref. [61]. The ATLAS 139 fb$^{-1}$ di-muon $Z'$ exclusion region is marked ‘ATLAS excl (central)’ in each plot. Varying the NCBA fit to be $2\sigma$ toward the SM limit results in the smaller ‘$(-2\sigma)$’ exclusion region. The dark crosses show the locations of the example points listed in table 1. In (c), we also display the region excluded by CONTUR at the 95% $CL_s$ level.
of figure 4a. Conversely, the region with large $M_{Z'}$ and small $|g_{sb}|$ requires such a large value of $g_{µµ}$ that the model becomes non-perturbative (where the $Z'$ width is equal to or larger than the mass), and we could not trust our results there. Fortunately, this does not impact any of the bounds we have derived.

Constraints on the MUM model are summarised in figure 4b. We see here that the $B_s$ mixing constraint already covers all of the region which the ATLAS di-muon search excludes (which is hardly visible in the plot), in contrast to the MDM model shown in figure 4a. The production processes do not benefit from the large $b\bar{b}$ contribution present in the MDM model, as table 1 illustrates. This is essentially because the MDM model has a $Z'bb$ coupling $\propto g_{ab}/|V_{ts}|$ i.e. enhanced by $1/|V_{ts}| \sim 25$. We may understand the shape of the ATLAS constraint by referring to figure 7 in appendix B: the branching ratio into muons increases for smaller $|g_{ab}|$ and larger $M_{Z'}$, which competes with the cross-section which increases toward the top left-hand corner of figure 4b. Everywhere that the ATLAS di-muon constraints are active, the $Z'$ is narrow.

Combined constraints on the TFHMeg are shown in figure 4c. We see that the ATLAS di-muon search has a strong effect on the parameter space when combined with the $B_s$ mixing constraint: $M_{Z'} > 1.2 \text{ TeV}$, for a central fit to the NCBAs. The region excluded by LEP flavour universality was calculated in ref. [61], and occurs because the $Z$ picks up small differences in its couplings to electrons as compared to muons due to $Z-Z'$ mixing. The model is non-perturbative for $M_{Z'} \geq 8.4 \text{ TeV}$ [61]. The white region is a relatively small portion of parameter space, but really one should take the weaker limits at ‘‘(−2σ)’, given the possibility of statistical variations of the fit to the NCBAs. The region to the right-hand side of the dotted line has $\Gamma/M_{Z'} > 0.1$, and so involves an extrapolation of the fit to data given in eq. (3.1) for this region (rather than an interpolation).

Contours exclusion limits are displayed at the left-hand side of the figure and the excluded region is marked ‘Contour excl’. There are no such exclusion limits in the parameter region shown for MDM or MUM, as the detailed Contour plots in figure 5 show. The Contour constraints show ‘due diligence’, in that the interesting parameter space is not yet ruled out by a large number of LHC SM measurements. Even though some measurements do receive BSM contributions to the fiducial cross section (for example the ATLAS 13 TeV $t\bar{t}b\bar{b}$ [87] and 8 TeV di-lepton-plus-di-jet measurements [88], and the CMS 13 TeV $t\bar{t}$ measurement [89]), the measurement precision is not yet sufficient to have a strong exclusion impact. Such exclusion as there is comes mainly from the ATLAS 8 TeV high-mass Drell-Yan measurement [90], and thus does not have the reach of the 13 TeV full Run II search.

5 Summary

Our focal results are the combined dominant constraints on $Z'$ models (the MUM model, the MDM model and the TFHMeg) which fit the NBCAs and are shown in figure 4. The $B_s$ mixing constraint is important, as well as a recent ATLAS $Z'\mu^+\mu^-$ search, performed on $139 \text{ fb}^{-1}$ of 13 TeV pp LHC collisions. The ATLAS search is probing the otherwise allowed parameter space of the MDM simplified model, and we may expect the TeV HL-LHC to
increase coverage of the parameter space [62, 67]. On the other hand, the MUM simplified model is currently more constrained by the $B_s$ mixing constraint, and likely will require an increase in energy [62, 67] (for example to HE-LHC [91] or FCC, [68]) for di-muon searches to probe the remaining parameter space. The $B_s$ mixing constraint is particularly constraining, but there has been significant movement on it in the last four years, mainly due to different estimates of the SM contribution. The 95% CL bound has been $M_{Z'}/g_{sb} > 148, 600, 194 \text{ TeV}$, respectively. We might therefore expect further movement upon the bound in the future, and this could have a large impact on the constraints. Taking the current bound of 194 TeV at face value, we extract (from the ‘$(−2\sigma)$’ bounds in figure 4c and from figure 8b) that $\sigma \times BR(\tau') \rightarrow t\bar{t} ≥ 2.6 \times 10^{-3} \text{ fb}$ in the TFHMeg at a centre of mass energy $\sqrt{s} = 13 \text{ TeV}$. The lower bound is saturated for $M_{Z'} = 3.5 \text{ TeV}$, $\theta_{ab} = 0.1$. At $\sqrt{s} = 14 \text{ TeV}$, we estimate (from this point) the minimum cross-sections in table 2. Since the nominal integrated luminosity for the HL-LHC is $L = 3000 \text{ fb}^{-1}$, we may expect at least $S = 30$ signal $Z' \rightarrow \mu^+\mu^−$ events. We are therefore hopeful of the TFHMeg HL-LHC $Z'$ search prospects.\footnote{Background estimates, which are beyond the scope of this work, would be required to properly calculate the sensitivity.}

### Acknowledgments

This work has been partially supported by STFC consolidated grants ST/P000681/1 and ST/N000285/1. BCA and JMB thank the (Re)interpreting the results of new physics searches at the LHC workshop, where part of this work was carried out. BCA thanks A Lenz and the Cambridge SUSY Working Group for discussions. This work has received funding from the European Union’s Horizon 2020 research and innovation programme as part of the Marie Skłodowska-Curie Innovative Training Network MCnetITN3 (grant agreement no. 722104).

### A Field definitions

We use the following field definitions in terms of representations of $SU(3) \times SU(2)_L \times U(1)_Y$: $Q_L = (3, 2, +1/6) = (u_L, d_L)^T$, $L_L = (1, 2, -1/2) = (\nu_L, e_L)^T$, $Z' = (1, 1, 0)$, where bold face denotes a 3-dimensional vector in family space. These fields are implicitly written in the mass eigenbasis.

<table>
<thead>
<tr>
<th>Channel</th>
<th>$\mu^+\mu^−$</th>
<th>$t\bar{t}$</th>
<th>$\tau^+\tau^−$</th>
<th>$b\bar{b}$</th>
<th>$\bar{\nu}\nu_j$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\sigma \times BR/\text{fb}$</td>
<td>0.010</td>
<td>0.056</td>
<td>0.04</td>
<td>0.017</td>
<td>0.010</td>
</tr>
</tbody>
</table>

Table 2. HL-LHC ($\sqrt{s} = 14 \text{ TeV}$) minimum fiducial cross section times branching ratios for different final-state channels in the TFHMeg.
Figure 5. Contour constraints on the MDM model (top), the MUM model (middle) and the TFHMeg (bottom). In the left-hand panels, we show regions excluded at the 68% and 95% $CL_s$ levels. In the right-hand panels, we show the $CL_s$ values, where 95% excluded values are $> 0.95$. Everywhere throughout the parameter plane shown, the NCBAs are fit by fixing $g_{\mu\mu}$ and $g_F$ as in eqs. (2.2), 2.16, respectively, for $x = 1.06$. 
Figure 6. Properties of the central fit of the MDM model to NCBAs. In (a), we show the $Z'$ width divided by its mass, $\Gamma/M_{Z'}$. In (b), the branching ratio into di-muons is shown, in (c) the fiducial $Z'$ production cross section multiplied by its branching ratio into di-muons is displayed. (d) shows $g_{\mu\mu}$ coming from the central fit to NCBAs. The white region is non-perturbative.
**Figure 7.** Properties of the central fit of the MUM model to NCBAs. In (a), we show the $Z'$ width divided by its mass, $\Gamma/M_{Z'}$. In (b), the branching ratio into di-muons is shown, in (c) the fiducial $Z'$ production cross section multiplied by its branching ratio into di-muons is displayed. (d) shows $g_{\mu\mu}$ coming from the central fit to NCBAs.
Figure 8. Properties of the TFHMeg. Everywhere throughout the parameter plane shown, the NCBAs are fit by fixing $g_F$ as in eq. (2.16) for $x = 1.06$ and shown in panel (d).

B Properties of the models

We display the CONTR constraints on the different models in figure 5. There are essentially no constraints upon the MDM model, whereas the MUM model is somewhat constrained for $M_{Z'} < 100$ GeV. The strongest constraints are upon the TFHMeg, which extend to $M_{Z'} = 1.5$ TeV, for low $\theta_{sb}$ (where $g_F$ is high).

We display some properties of the MDM model across parameter space in figure 6, some of the MUM model in figure 7 and some of the TFHMeg in figure 8.

Open Access. This article is distributed under the terms of the Creative Commons Attribution License (CC-BY 4.0), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.
References

[1] LHCb collaboration, Test of lepton universality with $B^0 \rightarrow K^{*0} \ell^+ \ell^-$ decays, JHEP 08 (2017) 055 [arXiv:1705.05602] [inspire].


[4] CMS collaboration, Measurement of the $B^0 \rightarrow \mu^+ \mu^-$ Branching Fraction and Search for $B^0 \rightarrow \mu^+ \mu^-$ with the CMS Experiment, Phys. Rev. Lett. 111 (2013) 101804 [arXiv:1307.5028] [inspire].

[5] CMS and LHCb collaborations, Observation of the rare $B_d^0 \rightarrow \mu^+ \mu^-$ decay from the combined analysis of CMS and LHCb data, Nature 522 (2015) 68 [arXiv:1411.4413] [inspire].


[8] LHCb collaboration, Angular analysis of the $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ decay using 3 fb$^{-1}$ of integrated luminosity, JHEP 02 (2016) 104 [arXiv:1512.04442] [inspire].

[9] ATLAS collaboration, Angular analysis of $B^0_d \rightarrow K^* \mu^+ \mu^-$ decays in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector, ATLAS-CONF-2017-023 (2017) [inspire].

[10] CMS collaboration, Measurement of the $P_t$ and $P_{\Delta}$ angular parameters of the decay $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ in proton-proton collisions at $\sqrt{s} = 8$ TeV, CMS-PAS-BPH-15-008 (2017) [inspire].


[26] K. Kowalska, D. Kumar and E.M. Sessolo, *Implications for New Physics in $b \to s \mu \mu$ transitions after recent measurements by Belle and LHCb*, arXiv:1903.10932 [nSPIRE].


[34] A. Crivellin, G. D’Ambrosio and J. Heeck, *Explaining $h \to \mu^+\mu^-$, $B \to K^\ast \mu^+\mu^-$ and $B \to K\mu^+\mu^-/B \to K\ell^+\ell^-$ in a two-Higgs-doublet model with gauged $L_\mu - L_\tau$*, Phys. Rev. Lett. 114 (2015) 151801 [arXiv:1501.00993] [nSPIRE].


[86] ATLAS collaboration, *Measurements of inclusive and differential fiducial cross-sections of $t\bar{t}$ production with additional heavy-flavour jets in proton-proton collisions at $\sqrt{s} = 13$ TeV with the ATLAS detector*, JHEP 04 (2019) 046 [arXiv:1811.12113] [insPIRE].

