Measurement of deuteron spectra and elliptic flow in Pb-Pb collisions at root s(\(\sqrt{s}\))=2.76 TeV at the LHC

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Measurement of deuteron spectra and elliptic flow in Pb–Pb collisions at √s_{NN} = 2.76 TeV at the LHC

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Abstract The transverse momentum (p_T) spectra and elliptic flow coefficient (v_2) of deuterons and anti-deuterons at mid-rapidity (|y| < 0.5) are measured with the ALICE detector at the LHC in Pb–Pb collisions at √s_{NN} = 2.76 TeV. The measurement of the p_T spectra of (anti-)deuterons is done up to 8 GeV/c in 0–10% centrality class and up to 6 GeV/c in 10–20% and 20–40% centrality classes. The v_2 is measured in the 0.8 < p_T < 5 GeV/c interval and in six different centrality intervals (0–5, 5–10, 10–20, 20–30, 30–40 and 40–50%) using the scalar product technique. Measured π^±, K^± and p+pT transverse-momentum spectra and v_2 are used to predict the deuteron p_T spectra and v_2 within the Blast-Wave model. The predictions are able to reproduce the v_2 coefficient in the measured p_T range and the transverse-momentum spectra for p_T > 1.8 GeV/c within the experimental uncertainties. The measurement of the coalescence parameter B_2 is performed, showing a p_T dependence in contrast with the simplest coalescence model, which fails to reproduce also the measured v_2 coefficient. In addition, the coalescence parameter B_2 and the elliptic flow coefficient in the 20–40% centrality interval are compared with the AMPT model which is able, in its version without string melting, to reproduce the measured v_2(p_T) and the B_2(p_T) trend.

1 Introduction

The study of light (anti-)nuclei produced in relativistic heavy-ion collisions allows us to investigate the expansion and cooling down of the hot dense medium produced in heavy-ion collisions, the Quark Gluon Plasma (QGP), and the hadronisation mechanism. Proton and deuteron p_T spectra measured at the LHC by a Large Ion Collider Experiment (ALICE) [1], show a clear dependence on the charged particle multiplicity, which can be explained by models that take into account the radial expansion of the emitting particle source [2]. To investigate different production scenarios, other observables, such as the coalescence parameter (B_A), which corresponds to the nucleons coalescence probability, and the elliptic flow (v_2) of light nuclei as a function of the transverse momentum, have been already studied at SPS, RHIC and LHC [2–5]. The B_A values at higher p_T complement the available results [2]. Measurements of the elliptic flow [6] allow for the investigation of collective effects among produced particles. The angular distribution of all the reconstructed charged particles with respect to the symmetry plane Ψ_n [7] can be expanded into a Fourier series

\[ E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left( 1 + \sum_{n=1}^{\infty} 2v_n \cos (n (\varphi - \Psi_n)) \right), \]

(1)

where E is the energy of the particle, \( \vec{p} \) the momentum, \( \varphi \) the azimuthal angle, y the rapidity, Ψ_n the angle of the spatial plane of symmetry of harmonic n [8–10] and

\[ v_n = \langle \cos (n (\varphi - \Psi_n)) \rangle. \]

(2)

The second term of the Fourier series (v_2) is called elliptic flow. It is directly linked to the almond shaped overlap region of the colliding ions in non central interactions and it can be related to the hydrodynamic properties of the QGP [11]. It is thus sensitive to the system conditions in the early stages of the evolution of a heavy-ion collision [7]. For identified hadrons v_2 gives details about the hadronization mechanism. The deuteron is a pn bound state, whose binding energy (∼ 2.24 MeV) is about two orders of magnitude lower than the hadronisation temperature. Thus if it is produced at hadronisation, it is likely that it would suffer from medium induced breakup in the hadronic phase. The v_2 measurements for d and \( \overline{d} \) provide an important test for the universal scaling of the elliptic flow [12] since it is expected to scale both with the v_2 of its constituent hadrons and with the v_2 of the constituent quarks.
Comparing the measured azimuthal anisotropy of the deuteron momentum distributions to the proton distributions, the STAR experiment [5] observed a mass number scaling in the $0.3 < p_T < 3$ GeV/c region leading to the conclusion that the mechanism of light nuclei formation at RHIC energies is mainly due to the coalescence of hadrons.

In this paper (anti-)deuteron transverse-momentum spectra and elliptic flow $v_2$ measured by ALICE in Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV are presented. The paper is organised as follows: in Sect. 2 a brief description of the ALICE detector is given and in Sect. 3 the event and track selections used in the present analysis are described. In Sect. 4 the different techniques used to identify deuterons and antideuterons are presented, together with the efficiency and acceptance corrections used for the determination of the transverse momentum spectra. In Sect. 5 the technique used to evaluate the deuteron elliptic flow and the obtained results are described, together with the comparison of deuteron and lighter particles elliptic flow. Section 6 is devoted to the comparison of the measured deuteron transverse momentum spectra and elliptic flow with different theoretical models, namely the Blast-Wave model, which is a hydro-based model [13–16], the coalescence model [17] and the dynamic coalescence model implemented in the AMPT generator [18]. Finally, in Sect. 7 the conclusions of this work are presented.

2 The ALICE detector

A detailed description of the ALICE detector can be found in [19] and references therein. For the present analysis the main sub-detectors used are the V0 detector, the Inner Tracking System (ITS), the Time Projection Chamber (TPC), the Time of Flight (TOF) and the High Momentum Particle Identification Detector (HMPID) which are located inside a maximum 0.5 T solenoidal magnetic field. The V0 detector [20] is formed by two arrays of scintillation counters placed around the beampipe on either side of the interaction point: one covering the pseudorapidity range $2.8 < \eta < 5.1$ (V0-A) and the other one covering $-3.7 < \eta < -1.7$ (V0-C). The collision centrality is estimated using the multiplicities measured in the V0 detector as detailed in Sect. 3. The V0 detector is also employed in the elliptic flow measurement as described in Sect. 5.

The ITS [21], designed to provide high resolution track points in the vicinity of the interaction region, is composed of three subsystems of silicon detectors placed around the interaction region with a cylindrical symmetry. The Silicon Pixel Detector (SPD) is the subsystem closest to the beampipe and it is made of two layers of pixel detectors. The third and the fourth layers are formed by Silicon Drift Detectors (SDD), while the outermost two layers are equipped with double-sided Silicon Strip Detectors (SSD). The inner radius of the SPD, 3.9 cm, is limited by the beampipe, while the TPC defines the radial span of the detector to be 43 cm. The ITS covers the pseudorapidity range $|\eta| < 0.9$ and it is hermetic in azimuth.

The same pseudorapidity range is covered by the TPC [22], which is the main tracking detector, consisting of a hollow cylinder whose axis coincides with the nominal beam axis. The active volume, filled with a gas at atmospheric pressure, has an inner radius of about 85 cm, an outer radius of about 250 cm, and an overall length along the beam direction of 500 cm. The gas is ionised by charged particles traversing the detector and the ionisation electrons drift, under the influence of a constant electric field of $\sim 400$ V/cm, towards the endplates where their arrival point is measured. The trajectory of a charged particle is estimated using up to 159 combined measurements (clusters) of drift times and radial positions of the ionisation electrons. The charged-particle tracks are then built by combining the hits in the ITS and the reconstructed clusters in the TPC. The tracks are then back-propagated to the beampipe to locate the primary collision position (primary vertex) with a resolution of about 100 $\mu$m in the direction transverse to the beams for heavy-ion collisions. The TPC is used for particle identification through the specific energy loss (dE/dx) measurement in the TPC gas.

The TOF system [23] covers the full azimuth for the pseudorapidity interval $|\eta| < 0.9$. The detector is based on the Multi-gap Resistive Plate Chambers (MRPCs) technology and it is located, with a cylindrical symmetry, at an average distance of 380 cm from the beam axis. The particle identification is based on the difference between the measured time-of-flight and its expected value, computed for each mass hypothesis from track momentum and length. The detector time resolution is about 80 ps.

The HMPID detector [19] consists of seven identical Ring Imaging Cherenkov (RICH) modules, in proximity focusing configuration, located at 475 cm from the beam axis. The HMPID, with its surface of about 12 m$^2$, covers a limited acceptance of $|\eta| < 0.55$ and $1.2^o < \phi < 58.5^o$. A HMPID module has three independent radiators, each one consisting of a 15 mm thick layer of liquid $C_6F_{14}$ (perfluorohexane) with a refractive index of $n = 1.289$ at a photon wavelength $\lambda = 1.75$ nm. They are coupled to multi-wire proportional chamber based photon detectors with CsI photocathodes. The HMPID complements the particle identification capabilities provided by the TPC and TOF detectors, extending the $p_T$ reach up to 4 GeV/c for pions and kaons and up to 6 GeV/c for protons [24].

3 Data sample

The analyses presented here are based on the data collected in the year 2011. In total, the data sample consists of nearly
40 million Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV after offline event selection. The events are collected using a trigger logic that requires the coincidence of signals on both sides of the V0 detector (V0-A and V0-C). An online selection based on the V0 signal amplitudes is used to enhance the sample of central and semi-central collisions through two separate trigger classes. The scintillator arrays have an intrinsic time resolution better than 0.5 ns, and their timing information is used together with that from the Zero Degree Calorimeters [19] for offline rejection of events produced by the interaction of the beams with residual gas in the vacuum pipe. Furthermore, in the offline selection only events with a reconstructed primary vertex position along the $z$ direction in the fiducial region $|V_z| < 10$ cm are selected.

The V0 detectors are used also to determine the centrality of Pb–Pb collisions. The amplitude distribution of V0 is fitted with a Glauber Monte Carlo to compute the fraction of the hadronic cross section corresponding to a given range of amplitude. From the Glauber Monte Carlo fit it is possible to classify events in several centrality percentiles selecting the corresponding production spectra to $p_T = 8$ GeV/c using the HMPID detector.

4.1 Particle identification

The TPC and TOF combined analysis presented in this paper adopts the same identification strategy used in the previous ALICE measurement of light (anti-)nuclei production [2]. With the large data sample collected in 2011 the deuteron transverse-momentum spectra measurement is extended up to 6 GeV/c. It is required that the measured energy-loss signal of a track as measured in the TPC lies in a $3\sigma$ window around the expected value for a given mass hypothesis. In addition, from the measured time-of-flight $t$ of the track, the mass $m$ of the corresponding particle can be obtained as:

$$m^2 = \frac{p^2}{c^4} \cdot \left(\frac{c^2 t^2}{L^2} - 1\right).$$

The total momentum $p$ and the track length $L$ are determined using the tracking detectors.

The $m^2 - m_{PDG}^2$ distribution, where $m_{PDG}$ is the nominal mass of deuteron as reported in [28], is measured for all $p_T$ intervals up to 6 GeV/c and it is fitted with a Gaussian function with an exponential tail. This is necessary to describe the asymmetric response of TOF. The background has two main components: the wrong association of a track with a TOF cluster and the exponential tail of lower mass particles. For this reason the background is modelled using the sum of two exponential functions. An example of the fit used to extract the deuteron yield in the $4.4 \leq p_T < 5$ GeV/c interval for the 0–10% centrality range is shown in the left panel of Fig. 1.

The TPC and TOF combined analysis is extended by using the HMPID measurement. With the available statistics and due to the limited geometrical acceptance of the HMPID only results in the 0–10% central Pb–Pb collisions are extracted.
The event and track selections are similar to those of the combined TPC and TOF analysis, but in addition it is required that the track is propagated to the charged-particle cluster in the MWPC of the HMPID. A maximal distance of 5 cm between the centroid of the charged-particle cluster and the track extrapolation on the cathode plane is required to reject the fake associations in the detector. This selection, tuned via Monte Carlo simulations, represents the best compromise between loss of statistics and the probability of an incorrect association. The particle identification in the HMPID detector is based on the measurement of the Cherenkov angle ($\theta_{\text{Ch}}$) which allows us to determine the square mass of the particle by the following formula:

$$m^2 = p^2 \cdot (n^2 \cos^2 \theta_{\text{Ch}} - 1),$$

where $n$ is the refractive index of the liquid radiator ($\text{C}_6\text{F}_{14}$ with $n = 1.29$ at temperature $T = 20$ $^\circ$C for photons with an energy of 6.68 eV) and $p$ is the momentum of the track.

In the 0–10% centrality class, where the total number of hits in the HMPID chambers is large, the reconstruction of the Cherenkov angle is also due to photons that are not associated to the particle. These wrong photon associations reduce the particle identification efficiency and similar effects are observed in the Monte Carlo simulations. The response function is a Gaussian distribution for correctly assigned rings and the raw yields are extracted by using an unfolding technique. The background mainly originates from fake photon associations and it is described with a second degree polynomial plus a $1/x^4$ term. Signal and background shapes are tuned via Monte Carlo simulations, as done for lighter mass particles [24].

An example of the distribution of the mass squared measured with the HMPID detector in the $p_T$ interval $5 \leq p_T < 6$ GeV/$c$ for positive tracks in the 0–10% centrality interval is shown in the right part of Fig. 1. Solid lines represent the total fit (signal plus background); dotted lines correspond to the background and dashed lines to deuterons signal.

### 4.2 Corrections

The final $p_T$ spectra of (anti-)deuterons are obtained by correcting the raw spectra for the tracking efficiency and geometrical acceptance. The correction is defined in the same way for the two PID techniques (i.e. TPC–TOF and HMPID) and it is computed as the ratio of the number of detected particles to the number of generated particles within the relevant phase space. The HIJING event generator [29] is used to generate background events. To these deuterons and antideuterons are explicitly added with a flat distribution both in transverse momentum and in azimuth. The GEANT3 transport code [30] is used to transport the tracks of the particles through the ALICE detector geometry. GEANT3 includes a limited simulation of the interaction of deuterons and antideuterons with the material because of the lack of experimental data on collisions of light nuclei with the different materials. For the present study, GEANT3 was modified as discussed in [2]: the cross-section of anti-nuclei are approximated in a simplified empirical model by a combination of the anti-proton ($\sigma_{\text{PA}}$) and anti-neutron ($\sigma_{\text{NA}}$) cross sections, following the approach presented in [31]. A full detector simulation with GEANT4 (v10.01) [32] has been performed in order to cross check the tracking efficiency estimation performed with the modified GEANT3. Since there was a dedicated effort in the GEANT4 code to interpolate the available measurements of the cross section of interaction between anti–nuclei and nuclei [33], the correction for the interaction of (anti-)deuterons with the detector material from GEANT3 is scaled to match the expected value from GEANT4. Half of
The track-fitting algorithm in ALICE takes into account the Coulomb scattering and energy loss using the mass hypothesis of the pion. The energy loss of heavier particles, such as the deuterons, is considerably higher than the energy loss of pions, therefore a track-by-track correction is necessary. This correction is obtained from the difference between the generated and the reconstructed momentum in a full Monte Carlo simulation of the ALICE detector. As already discussed in [2], the effect of this correction is negligible for high \( p_T \) deuterons. This momentum correction was included in systematics checks for the elliptic flow determination and its effect was found to be negligible.

4.3 Systematic uncertainties and results

The systematic uncertainties for the two spectra analyses mainly consist of three components, in order of relevance:

- transport code: the uncertainty on the hadronic cross section of the (anti-)deuterons with the material, estimated taking the difference between the efficiencies evaluated with GEANT3 and GEANT4;
- the fitting uncertainties for the signal extraction, studied by changing the functional form of the fitting function. The uncertainty has been estimated computing the RMS of the results of these variations;
- the track selection bias assessed through the variation of the track selection criteria. Among the probed selections there are the PID fiducial cut in the TPC and the track DCA\(_z\) selection, whose variations turned into a negligible contribution (\( \lesssim 1\% \)) to the systematic uncertainties. Since the effects of the variation of the DCA\(_z\) selection are negligible, we can conclude that the production spectra of deuterons are not affected by secondary particles originating from material in the high \( p_T \) region.

The other contributions to the systematic uncertainties are related to the limited knowledge of the material budget, the PID and the \( \epsilon_{\text{dist}} \) correction for the HMPID analysis. Table 1

![Figure 2](image_url)
d) is performed in the TOF detector is fitted to the spectra at high transverse momenta, as the data sample used for the analysis extracted in [2] have smaller systematic uncertainties and larger coverage of the Transition Radiation Detector and a HMPID PID – 4 tracks selection 7767 Signal extraction 3 3 13 (15) 15 (18) Transport code 8 (10) 8 (10) Material budget 3 3 10–20%, 20–30%, 30–40% and 40–50%). The identification of deuterons (d) and anti-deuterons (d) for all the centrality intervals and in the transverse-momentum interval p_T > 1.4 GeV/c. This is possible since the results for the two separated particles are compatible within statistical uncertainties. For lower momenta (0.8 ≤ p_T < 1.4 GeV/c) only anti–deuterons are used to avoid effects related to secondary deuterons created through the interaction of particles with the material. The d+d signal in the TOF detector is fitted with a Gaussian with an exponential tail, while the background is fitted with an exponential. An example of the ΔM distribution, where ΔM = m – m_{PDG}, for deuterons plus anti–deuterons with 2.20 ≤ p_T < 2.40 GeV/c and centrality interval 30–40% is shown in the left part of Fig. 4.

Table 1 Details of the systematic uncertainties assigned in the TPC and TOF-combined and HMPID analyses. The values in the parentheses refer to the systematic for the anti-deuteron spectra when different to the deuteron ones.

<table>
<thead>
<tr>
<th>pT interval (GeV/c)</th>
<th>TPC-TOF</th>
<th>HMPID</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.4–5.0 (%)</td>
<td>5.0–6.0 (%)</td>
<td>5.0–6.0 (%)</td>
</tr>
<tr>
<td>Transport code</td>
<td>8 (10)</td>
<td>8 (10)</td>
</tr>
<tr>
<td>Signal extraction</td>
<td>3 3</td>
<td>13 (15) 15 (18)</td>
</tr>
<tr>
<td>Track selection</td>
<td>7 7</td>
<td>6 7</td>
</tr>
<tr>
<td>Material budget</td>
<td>3 3</td>
<td>3 3</td>
</tr>
<tr>
<td>HMPID ε_dist</td>
<td>– 5</td>
<td></td>
</tr>
<tr>
<td>HMPID PID</td>
<td>– 4</td>
<td></td>
</tr>
</tbody>
</table>

illustrates the details about the systematic uncertainties for the spectra analyses in each p_T interval presented in this paper.

The results of the two analyses in the 0–10% centrality interval and in the p_T range between 5 and 6 GeV/c are compatible within the uncertainties, thus in the final spectra they are combined using a weighting procedure. The weights used in the combination are the uncorrelated systematic uncertainties, given that the statistical uncertainties of the two analyses are partially correlated. The resulting spectra are shown in the upper panel of Fig. 3 for p_T > 4.4 GeV/c. For lower transverse momenta, as the data sample used for the analyses at high p_T presented in this paper was collected with a larger coverage of the Transition Radiation Detector and a lower performance of the Silicon Pixel Detector, the spectra extracted in [2] have smaller systematic uncertainties and they are used in Fig. 3. The spectra extracted with the two data samples are compatible within the systematic uncertainties.

The bottom panels of Fig. 3 show the ratios between the deuteron and anti-deuteron spectra for the different centrality classes as a function of the transverse momentum. As already observed in [2] and predicted by coalescence and thermal models the ratio is compatible with unity over the full transverse momentum region. The integrated yield and the mean transverse momentum are extracted by fitting the spectra in each centrality interval with the Blast-Wave function [34] and they are in agreement within the experimental uncertainties with the values shown in [2].

5 Elliptic flow measurements

5.1 Analysis technique

The determination of the deuteron elliptic flow is performed over the same sample of Pb–Pb collisions at √s_{NN} = 2.76 TeV as already described in Sect. 3, and the full event sample is divided into 6 different centrality intervals (0–5%, 5–10%, 10–20%, 20–30%, 30–40% and 40–50%). The identification of deuterons (d) and anti-deuterons (d) is performed in the 0.8 < p_T < 5 GeV/c transverse momentum interval as follows: for momenta up to 1.4 GeV/c the energy loss in the TPC gives a clean sample of (anti-)deuterons by requiring a maximum deviation of the specific energy loss of 3σ with respect to the expected signal; above 1.4 GeV/c a hit on the TOF detector is required, similarly to what has been described in the Sect. 4.1. In order to increase the statistics, deuterons and anti-deuterons are combined (d+d) for all the centrality intervals and in the transverse-momentum interval p_T > 1.4 GeV/c.
The $v_2$ coefficient is measured using the Scalar Product (SP) method [7,35], a two-particle correlation technique, using a pseudo-rapidity gap $|\Delta \eta| > 0.9$ between the identified hadron under study and the reference flow particles. The applied gap reduces the non-flow effects (e.g. jets), which are correlations not arising from a collective motion. The results presented in this paper are obtained by dividing each event into three sub-events A, B and C, using three different pseudo-rapidity regions. The reference particles were taken from sub-events A and C, using the V0-A (2.8 < $\eta$ < 5.1) and V0-C (-3.7 < $\eta$ < -1.7) detectors, respectively, while deuterons were taken from sub-events B within $|\eta| < 0.8$. The $v_2$ coefficient was then calculated as described in [35]

$$v_2 = \sqrt{\frac{\langle \hat{\rho}_2^B \cdot \hat{Q}_2^A \rangle \langle \hat{\rho}_2^B \cdot \hat{Q}_2^C \rangle}{\langle \hat{Q}_2^A \cdot \hat{Q}_2^C \rangle}}, \quad (6)$$

where the two brackets in the numerator indicate an average over all the particles of interest and over all the events, $M_A$ and $M_C$ are the estimates of multiplicity from the V0-A and V0-C detectors, and $\hat{Q}_2^A$, $\hat{Q}_2^C$ are the complex conjugates of the flow vector [36] calculated in sub-event A and C, respectively, and $\hat{\rho}_2^B$ is the unit flow vector measured in sub-event B. The contribution to the measured elliptic flow ($v_2^{Tot}$) due to misidentified deuterons ($v_2^{Bkg}$) is removed by studying the azimuthal correlations versus $\Delta M$. This method is based on the observation that, since $v_2$ is additive, candidates $v_2^{Tot}$ can be expressed as a sum of signal ($v_2^{Sig}(\Delta M)$) and background ($v_2^{Bkg}(\Delta M)$) weighted by their relative yields $N_{Sig}$ and $N_{Bkg}$, respectively.

$$v_2^{Tot}(\Delta M) = v_2^{Sig}(\Delta M) \frac{N_{Sig}(\Delta M)}{N_{Tot}(\Delta M)} + v_2^{Bkg}(\Delta M) \frac{N_{Bkg}(\Delta M)}{N_{Tot}(\Delta M)}.$$

(7)

where $N_{Tot}$ is the total number of candidates, $N_{Sig}$ and $N_{Bkg}$ are the numbers of background and signal for a given mass and $p_T$ interval. The yields $N_{Sig}$ and $N_{Bkg}$ are extracted from fits to the $\Delta M$ distributions obtained with the TOF detector for each centrality and $p_T$ interval. The $v_2^{Tot}$ vs $\Delta M$ for $d+\bar{d}$ for $2.2 \leq p_T < 2.4$ GeV/c in events with 30–40% centrality is shown in the right panel of Fig. 4, where the points represent the measured $v_2^{Tot}$ and the curve is the fit performed using Eq. 7. The $v_2^{Bkg}$ was parametrized as a first-order polynomial ($v_2^{Bkg}(\Delta M) = p_0 + p_1 \Delta M$).

5.2 Systematic uncertainties and results

The systematic uncertainties are determined by varying the event and track selections. The contribution of each source is estimated, for each centrality interval, as the root mean square deviation of the $v_2(p_T)$ extracted from the variations of the cut values relative to the results described above. The total systematic uncertainty was calculated as the quadratic sum of each individual contribution. The event sample is varied by changing the cut on the position of the primary vertex along the beam axis from $\pm 10$ to $\pm 7$ cm, by replacing the centrality selection criteria from the amplitude of the signal of the V0 detector to the multiplicity of the TPC tracks and by separating runs with positive and negative polarities.
of the solenoidal magnetic field. The systematic uncertainties related to these changes are found to be smaller than 1%. Additionally, systematic uncertainties related to particle identification are studied by varying the number of standard deviations around the energy loss expected for deuterons in the TPC and, similarly, for the time of flight in the TOF detector and by varying the distance of closest approach in the DCA_{xy} of accepted tracks. These contributions are found to be around 2% for all the analysed transverse-momentum and centrality intervals. The systematic uncertainties originating from the determination of N^{Bkg}, N^{Tot} and N^{BS} in Eq. 7, are studied by using different functions to describe the signal and the background. The function adopted to describe the $v_2^{Bkg}(\Delta M)$ is varied using different polynomials of different orders. The contribution to the final systematic uncertainties is found to be around 3% for all the analysed transverse-momentum and centrality intervals. The main contributions to the systematic uncertainties of deuteron elliptic flow are related to TPC and TOF occupancy [35]. These contributions were studied in detail in [35] and are adopted in the present analysis, leading to absolute systematic uncertainties of 0.02 (TPC) 0.01 (TOF) for TPC and TOF occupancy, respectively. A summary of all the systematic uncertainties can be found in Table 2.

Table 2 Summary of the systematic uncertainties for the determination of the deuterons $v_2$ coefficient

<table>
<thead>
<tr>
<th>Source</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Event Selections</td>
<td>&lt; 1%</td>
</tr>
<tr>
<td>Particle Identification</td>
<td>2%</td>
</tr>
<tr>
<td>Fit to $v_2^{Tot}$ vs $\Delta M$</td>
<td>3%</td>
</tr>
<tr>
<td>TPC and TOF occupancy (absolute value)</td>
<td>0.02 (TPC) 0.01 (TOF)</td>
</tr>
</tbody>
</table>

The measured $v_2$ as a function of $p_T$ for d+Au is shown in Fig. 5. Each set of points corresponds to a different centrality class: 0–5, 5–10, 10–20, 20–30, 30–40 and 40–50%, as reported in the legend. Vertical lines represent statistical errors, while boxes are systematic uncertainties. The value of $v_2(p_T)$ increases progressively from central to semi-central collisions. This behaviour is consistent with the picture of the final-state anisotropy driven by the collision geometry, as represented by the initial-state eccentricity which decreases from peripheral to central collisions.

5.3 Comparison with other identified particles and test of scaling properties

In order to study the spectra and the elliptic flow of deuterons simultaneously, the latter has been determined in the same centrality intervals selected for the $p_T$ spectra (0–10, 10–20 and 20–40%) (see Sect. 4). The measured $v_2$ coefficient for d+Au is compared with that of pions and protons [35]. The results in the 20–40% centrality interval are shown in Fig. 6. The $v_2$ of $\pi^\pm$ (empty circles), p+Pb (filled squares) and d+Au (filled circles) as a function of $p_T$ are shown in the top left panel of the figure. It is observed that at low $p_T$ deuterons follow the mass ordering observed for lighter particles, which is attributed to the interplay between elliptic and radial flow [15,37]. The second column of Fig. 6 is used to test the scaling properties of $v_2$ with the number of constituent quarks ($n_q$). It has been observed at RHIC [38–40] that the various identified hadron species approximately show a follow a common behaviour [41], while nuclei follow an atomic mass number scaling in the 0.3 < $p_T$ < 3 GeV/c interval [5]. The $v_2$ coefficient divided by $n_q$ is shown as a function of $p_T/n_q$ in the upper panel: the experimental data indicate only an approximate scaling at the LHC energy for deuterons. To quantify the deviation, the $p_T/n_q$ dependence of $v_2/n_q$ for protons and anti-protons is fitted with a seventh-order-polynomial function and the ratio of $(v_2/n_q)/(v_2/n_q)_{Fit}$ is calculated for each particle. A deviation from the $n_q$ scaling of the order of 20% for $p_T/n_q > 0.6$ is observed for deuterons; the same behaviour is observed in the other centrality intervals (not shown). Finally, in the third column, the measured $v_2/n_q$ is shown as a function of the transverse kinetic energy scaled by the number of constituent quarks $(K E_T)/n_q = (m_T - m_0)/n_q$ of each particle. This scaling, introduced by the PHENIX collaboration [42] for low $p_T$, was initially observed to work well – within statistical uncertainties – at RHIC energies in central A–A collisions [38,41]. However, recent publications report deviations from this scaling for non central Au–Au collisions [43]. Also at the LHC energy the proposed scaling does not work properly (deviations up to ~ 20%) [35], and the scaling is not valid for...
6 Comparison with different theoretical models

6.1 Comparison with Blast-Wave model

Fig. 6 $v_2$ of $\pi^\pm$ (empty circles), $p+\bar{p}$ (filled squares) and $d+\bar{d}$ (filled circles) measured in the 20–40% centrality interval. A detailed description of each panel can be found in the text.

The deviations are quantified in the bottom panel, where the ratio of $(v_2/n_q)/(v_2/n_q)_{\text{fit}}$ for each particle is shown. Significant deviations are found for $K E_T/n_q < 0.3$ GeV/c, indicating that also for light nuclei the scaling with $n_q$ does not hold at the LHC energy. For $K E_T/n_q > 0.3$ GeV/c, data exhibit deviations from an exact scaling at the level of 20%.

The nuclear fireball model was introduced in 1976 to explain midrapidity proton-inclusive spectra [13]. This model assumes that a clean cylindrical cut is made by the projectile and target leaving a hot source in between them. Protons emitted from this fireball should follow a thermal energy distribution, and are expected to be emitted isotropically. Such a model, called Blast-Wave model, has evolved since then, with more parameters to describe both the $p_T$ spectra and the anisotropic flow of produced particles [14–16]. As described in [15], the transverse mass spectrum can be expressed as

$$\frac{dN}{dy \, m_T^2 \, d\phi_p} \sim \int_0^{2\pi} d\phi_s \, K_1(\beta_s(\phi_s)) \, e^{\alpha_s(\phi_s) \cos(\phi_s - \phi_p)},$$

where $\phi_s$ and $\phi_p$ are the azimuthal angles in coordinate and momentum space; the arguments $\alpha_s(\phi_s)$ and $\beta_s(\phi_s)$ are based on a $\phi_s$-dependent radial flow rapidity $\rho(\phi_s)$ and $K_1$ is a modified Bessel function of the second kind.

The elliptic flow coefficient $v_2$ is obtained by taking the azimuthal average over $\cos(2\phi_p)$ with this spectrum, $v_2 = \langle \cos(2\phi_p) \rangle$. The integral on $\phi_p$ can be evaluated analytically

$$v_2(p_T) = \frac{\int_0^{2\pi} d\phi_s \, \cos(2\phi_s) \, I_2(\alpha_s(\phi_s)) \, K_1(\beta_s(\phi_s))}{\int_0^{2\pi} d\phi_s \, I_0(\alpha_s(\phi_s)) \, K_1(\beta_s(\phi_s))},$$

where $I_0$ and $I_2$ are modified Bessel functions of the first kind. However, the Blast-Wave fit matched data even better after the STAR Collaboration added a fourth parameter, $s_2$, [16] which takes into account the anisotropic shape of the source in coordinate space. With the introduction of the $s_2$ parameter, the elliptic flow can be expressed as
protons and neutrons which are close in space and have similar velocities. In this production mechanism, the cross section for the production of a cluster with mass number $A$ is related to the probability that $A$ nucleons have relative momenta less than $p_0$, which is a free parameter of the model [17]. This provides the following relation between the production rate of the nuclear cluster emitted with a momentum $p_A$ and the nucleons emitted with a momentum $p_p$:

$$E_A \frac{d^3N_A}{dp_A^3} = B_A \left( E_p \frac{d^3N_p}{dp_p^3} \right)^A,$$

where $p_0$ is commonly named coalescence radius while $M$ and $m$ are the nucleus and the nucleon mass, respectively. The left panel of Fig. 8 shows the obtained $B_2$ values for deuterons in three different centrality regions studied in the present work. The measured $B_2$ values are plotted versus the transverse momentum per nucleon ($p_T/A$). A clear decrease of the $B_2$ parameter with increasing centrality and an increase with transverse momentum is observed. The measured $B_2$ at higher $p_T$ bins presented in this paper follow the trend already observed for smaller momenta, confirming that the experimental result is in contrast to the expectations of the simplest coalescence model [17], where the $B_2$ is expected to be flat. As already observed in [2], the observed behaviour can be qualitatively explained by position-momentum correlations which are caused by a radially expanding source [45], but better theoretical calculations at the LHC energies are needed.

Since elliptic flow is additive, it is possible to infer the expected $v_2$ of a composite state (like a deuteron) formed via coalescence starting from Eq. 11. In the region where the coalescence occurs, the elliptic flow of a nucleus can be expressed as a function of the elliptic flow of its constituent nucleons. For a deuteron, assuming that protons and neutrons behave in the same way, the following relation is expected [46]:

$$v_{2,d}(p_T) = \frac{2v_{2,p}(p_T/2)}{1 + 2v_{2,p}^2(p_T/2)}.$$

It is then possible to obtain the expected deuteron elliptic flow starting from the one measured for protons [35]. The results for different centrality intervals are shown in the right part of Fig. 8, where the measured elliptic flow (markers) is compared with simple coalescence predictions (shaded bands) from Eq. 13 for the three different centrality inter-

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### Table 3: Blast-Wave parameters computed by fitting the pion, kaon and proton transverse-momentum spectra and elliptic flow. See the text for more details

<table>
<thead>
<tr>
<th>Fit parameters</th>
<th>Centrality classes</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T$ (MeV)</td>
<td>0–10%</td>
</tr>
<tr>
<td>$s_2 \times 10^{-2}$</td>
<td>$1.6 \pm 0.2$</td>
</tr>
<tr>
<td>$\rho_0 \times 10^{-1}$</td>
<td>$0.9 \pm 0.1$</td>
</tr>
<tr>
<td>$\rho_0 \times 10^{-1}$</td>
<td>$0.5 \pm 0.1$</td>
</tr>
</tbody>
</table>

The left panel of Fig. 8 shows the obtained $B_2$ values for deuterons in three different centrality regions studied in the present work. The measured $B_2$ values are plotted versus the transverse momentum per nucleon ($p_T/A$). A clear decrease of the $B_2$ parameter with increasing centrality and an increase with transverse momentum is observed. The measured $B_2$ at higher $p_T$ bins presented in this paper follow the trend already observed for smaller momenta, confirming that the experimental result is in contrast to the expectations of the simplest coalescence model [17], where the $B_2$ is expected to be flat. As already observed in [2], the observed behaviour can be qualitatively explained by position-momentum correlations which are caused by a radially expanding source [45], but better theoretical calculations at the LHC energies are needed.

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$$v_{2,d}(p_T) = \frac{2v_{2,p}(p_T/2)}{1 + 2v_{2,p}^2(p_T/2)}.$$
Fig. 7 Combined Blast-Wave fit to $p_T$ and $v_2(p_T)$ distributions using Eqs. 8 and 10. The six upper panels show the $p_T$ spectra and the ratio between data and fit, while the six panels in the bottom part shows the $v_2(p_T)$ and the ratio between data and fit. In each panel, $\pi^\pm$ (empty circles), $K^\pm$ (diamonds), $p+p$ (filled squares) and $d+d$ (filled circles) are shown. For $\pi^\pm$, $K^\pm$ and $p+p$ the long dashed curves represent the combined $p_T$ and $v_2$ Blast-Wave fit. Deuteron curves (dash dotted lines) are predictions from lighter particles Blast-Wave combined fit. Each column shows a different centrality intervals (0–10% left, 10–20% middle and 20–40% right).

vals presented in the paper. Also here the simple coalescence is not able to reproduce the measured elliptic flow of deuterons. This behaviour is different with respect to what has been observed at lower energies, where an atomic mass number scaling was observed in the $0.3 < p_T < 3 \text{ GeV}/c$ interval [5]. Improved versions of the coalescence model, for instance based on a realistic phase space distribution of the constituent protons and neutrons, might describe the elliptic flow of deuterons at LHC energy better.

6.3 Comparison with AMPT

The AMPT model is a hybrid model [18] with the initial particle distributions generated with HIJING [29]. In the default
version of AMPT, the jet quenching in HIJING is replaced by explicitly taking into account the scattering of mini-jet partons via the Zhang’s parton cascade (ZPC) model [47]. In the version with string melting, all the hadrons produced from the string fragmentation in HIJING are converted to their valence quarks and antiquarks, whose evolution in time and space is guided by the ZPC model. After the end of their scatterings, quarks and antiquarks are converted to hadrons via a spatial coalescence model. In both versions of the AMPT model, the scatterings among hadrons are described by a relativistic transport (ART) model [48]. The (anti-)deuterons are produced and dissolved within ART via the NN ↔ π d reaction in the hadronic stage of AMPT. The Monte Carlo predictions [49] for the deuteron coalescence parameter \( B_2 \) and elliptic flow \( v_2 \) are compared with the measured one in this section. For the simulation, an impact parameter \( b = 8 \text{ fm} \) was used: this value corresponds to the mean value of the impact parameter in the 20–40% centrality interval [26]. The comparisons between data and Monte Carlo results can be seen in Fig. 9: in the left top panel the measured \( B_2 \) is shown (filled markers) together with the published AMPT expectations (lines), while in the bottom panel the ratios between
the data and models are shown. In the top right panel the measured elliptic flow (filled markers) and the AMPT expectations are displayed. From the bottom right panel of Fig. 9 it is possible to observe that the default version of AMPT (empty circles) is able to reproduce the measured deuteron elliptic flow, while the simulated $B_2$ is able to reproduce the behaviour of the measured one but is larger by a factor 2. The AMPT with String Melting enabled (dotted line in the top panels and full squares in the bottom panels) is unable to reproduce neither the measured $B_2$ nor the $v_2(p_T)$ parameter of the (anti-)deuterons. It is worth to emphasize that the standard AMPT does not reproduce the lighter hadrons $v_2(p_T)$ neither [35].

7 Conclusions

In this paper we presented the deuteron spectra up to $p_T = 8$ GeV/c produced in Pb–Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV extending significantly the $p_T$ reached by the spectra shown in [2] for central and semi-central collisions. The $v_2$ of (anti-)deuterons is measured up to 5 GeV/c and it shows an increasing trend going from central to semi-central collisions, consistent with the picture of the final state anisotropy driven by the collision geometry. At low $p_T$ the deuteron $v_2$ follows the mass ordering, indicating a more pronounced radial flow in the most central collisions, as it is observed also for lighter particles. Similarly the $n_\parallel$ scaling violation seen for the elliptic flow of lighter particles at the LHC energies is confirmed for the elliptic flow of the deuteron. The Blast-Wave model, fitted on the spectra and the elliptic flow of pions, kaons and protons, describes within the experimental uncertainties the deuteron production spectra for $p_T > 1.8$ GeV/c and the deuteron $v_2(p_T)$ suggesting common kinetic freeze-out conditions. At lower transverse momenta the model underestimates the measured spectra with a discrepancy up to 2σ. The coalescence parameter $B_2$, evaluated up to $p_T/A = 4$ GeV/c, rapidly increases with the transverse momentum confirming the experimental observation made in [2]. The simplest formulation of the coalescence model [17] predicts a flat $B_2$ distribution and it does not reproduce the observed trend. The same model fails to reproduce the measured elliptic flow of deuterons. On the contrary, the AMPT model without String Melting [18] is able to reproduce the observed elliptic flow of deuterons and it correctly predicts the shape of the $B_2$ distribution but it overestimates the data by about a factor of 2. When enabling the String Melting mechanism the AMPT model is unable to predict neither the measured $B_2$ nor the $v_2(p_T)$ of the (anti-)deuterons.

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