Production of muons from heavy-flavour hadron decays in p-Pb collisions at root s(NN)=5.02 TeV

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Production of muons from heavy-flavour hadron decays in p–Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV

ALICE Collaboration*

**Abstract**

The production of muons from heavy-flavour hadron decays in p–Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV was studied for $2 < p_T < 16$ GeV/c with the ALICE detector at the CERN LHC. The measurement was performed at forward (p-going direction) and backward (Pb-going direction) rapidity, in the ranges of rapidity in the centre-of-mass system (cms) $2.03 < y_{cms} < 3.53$ and $-4.46 < y_{cms} < -2.96$, respectively. The production cross sections and nuclear modification factors are presented as a function of transverse momentum ($p_T$). At forward rapidity, the nuclear modification factor is compatible with unity while at backward rapidity, in the interval $2.5 < p_T < 3.5$ GeV/c, it is above unity by more than 2σ. The ratio of the forward-to-backward production cross sections is also measured in the overlapping interval $2.96 < |y_{cms}| < 3.53$ and is smaller than unity by 3.7σ in $2.5 < p_T < 3.5$ GeV/c. The data are described by model calculations including cold nuclear matter effects.

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1. Introduction

The study of ultra-relativistic heavy-ion collisions aims at investigating the properties of strongly-interacting matter under extreme conditions of temperature and energy density. Under these conditions, Quantum Chromodynamics (QCD) calculations on the lattice predict a transition to a Quark–Gluon Plasma (QGP) in which colour confinement vanishes and chiral symmetry is partially restored [1,2]. Heavy quarks (charm and beauty) are essential probes of the properties of the QGP since they are produced in hard scattering processes in the early stage of the collision and, while propagating through the medium, interact with the QGP constituents. The nuclear modification factor $R_{AA}$ is commonly used to characterise heavy-quark interaction with the medium constituents. It is defined as the ratio between the particle yield in nucleus–nucleus (AA) collisions and a reference obtained by scaling the yield measured in proton–proton (pp) collisions by the number of binary nucleon–nucleon collisions, calculated with the Glauber model [3]. Heavy-quark production in pp collisions at various energies is described within uncertainties by perturbative QCD (pQCD) calculations [4–11]. In central Pb–Pb collisions ($\sqrt{s_{NN}} = 2.76$ TeV), a suppression of D mesons and leptons from heavy-flavour hadron decays by a factor of about 3–5 was measured for transverse momenta $p_T > 4$ GeV/c [5,12–14]. Further insights into the QGP evolution and the in-medium interactions can be gained from the study of the particle azimuthal anisotropy expressed in terms of Fourier series, where the second order coefficient $v_2$ is the elliptic flow. A positive $v_2$ was observed at low and/or intermediate $p_T$ in semi-central Pb–Pb collisions for D mesons and electrons from heavy-flavour hadron decays at mid-rapidity [15–17] and for muons from heavy-flavour hadron decays at forward rapidity [18], confirming the significant interaction of heavy quarks with the medium constituents.

Although the suppression of high-$p_T$ particle yield suggests that heavy quarks lose a significant amount of their initial energy [19–25], this suppression cannot be, a priori, exclusively attributed to the interaction of quarks with the hot and dense medium formed in the collision. Indeed, for a comprehensive understanding of Pb–Pb results, it is fundamental to quantify Cold Nuclear Matter (CNM) effects, which can modify the $p_T$ spectra in nuclear collisions independently from the formation of a QGP. Cold nuclear matter effects include the modification of the Parton Distribution Functions (PDFs) of the nuclei with respect to a superposition of nucleon PDFs, addressed by nuclear shadowing models [26,27] or gluon saturation models as the Colour Glass Condensate (CGC) effective theory [28,29]. Other CNM effects are Cronin enhancement through $k_T$ broadening [30–32] and energy loss in the initial [33] and final stages of the collision. These effects can be assessed by studying p–Pb collisions, where the formation of an extended hot and dense system is not expected. A possible presence of final-state effects in small systems at RHIC and LHC energies is suggested by measurements of long-range correlations [34–38] consistent with the presence of collective effects. This is

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further supported by the measurements of the species-dependent nuclear modification factors of identified particles in d–Au collisions [39], multiplicity dependence of $\pi^\pm$, K$^\pm$, p and $\Lambda$ production in p–Pb collisions [40], and a significant suppression of $\psi(2S)$ yields in comparison to those of J/$\psi$ [41,42].

Cold nuclear matter effects on heavy-flavour production have been thoroughly investigated at RHIC by the PHENIX and STAR Collaborations through the measurement of the production of leptons from heavy-flavour hadron decays in d–Au collisions at $\sqrt{S_{NN}} = 200$ GeV. An enhancement of the yields of electrons from heavy-flavour hadron decays, with respect to a binary-paced pp reference, was observed at mid-rapidity [43,44]. An enhancement (suppression) of muons from heavy-flavour hadron decays was measured at backward (forward) rapidity [45]. The differences observed between forward and backward rapidity are not reproduced by models based only on modifications of the initial parton densities [27]. Finally, the recent measurement of azimuthal correlations between electrons from heavy-flavour hadron decays at mid-rapidity and muons from heavy-flavour hadron decays at forward rapidity [46] shows a suppression of the yield of electron–muon pairs with $\Delta \phi = \pi$, suggesting that CNM effects modify the c$\bar{c}$ correlations. An experimental effort to quantify CNM effects on heavy-flavour production is underway also at the LHC. The measurement of the $p_T$-integrated nuclear modification factor of J/$\psi$ from B-hadron decays in p–Pb collisions at $\sqrt{S_{NN}} = 5.02$ TeV by the LHCb Collaboration [47] indicates a suppression by about 20% at forward rapidity and no suppression at backward rapidity. The measurements of the nuclear modification factors of $B^+$, $B^0$ and $B^0_s$ by the CMS Collaboration [48] and of the forward-to-backward ratio of J/$\psi$ from B-hadron decays by the ATLAS Collaboration [49] at high $p_T$ are also compatible with unity. The mid-rapidity nuclear modification factors of prompt D mesons [50] and electrons from heavy-flavour hadron and beauty-hadron decays [51,52] measured by the ALICE Collaboration are found consistent with unity.

This Letter presents differential measurements of the production of muons from heavy-flavour hadron decays for $2 < p_T < 16$ GeV/$c$ in p–Pb collisions at $\sqrt{S_{NN}} = 5.02$ TeV at forward and backward rapidity performed by the ALICE Collaboration at the LHC. Comparisons with model calculations to extract relevant information concerning CNM effects are also discussed. These measurements cover forward (2.03 < $y_{cm}$ < 3.53, p-going direction) and backward ($-4.46 < y_{cm} < -2.96$, Pb-going direction) rapidity regions. The Bjorken-x values of gluons in the Pb nucleus probed by measurements of muons from heavy-flavour hadron decays have been estimated with PYTHIA 8 (Tune 4C) [53] considering Leading Order (pair creation) and Next-to-Leading Order (flavour excitation and gluon splitting) processes. At forward rapidity, they are located in the range from about 5 · $10^{-6}$ to $10^{-2}$ and the median of the distribution is about $10^{-4}$. At backward rapidity, the Bjorken-x values are expected to vary from about $10^{-3}$ to $10^{-1}$ and the median is of the order of 10$^{-2}$.

The Letter is structured as follows. Section 2 describes the apparatus with an emphasis on the detectors used in the analysis and the data taking conditions. Section 3 addresses the analysis details. Section 4 presents the results, namely the $p_T$-differential cross sections and nuclear modification factors at forward and backward rapidity and the forward-to-backward ratio in a smaller overlapping rapidity interval (2.96 < $|y_{cm}|$ < 3.53). Finally, the results are compared with model calculations which include CNM effects.

2. Experimental apparatus and data samples

A detailed description of the ALICE detector is available in [54] and its performance is discussed in [55]. Muons are detected in ALICE using the muon spectrometer in the pseudo-rapidity interval $-4 < \eta_{\mu} < -2.5$. The muon spectrometer consists of i) a forward absorber made of carbon, concrete and steel of 10 interaction lengths ($\lambda_I$) located between the interaction point (IP) and the spectrometer that filters out hadrons, ii) a beam shield throughout its entire length, iii) a dipole magnet with a field integral of 3 T·m, iv) five tracking stations, each composed of two planes of cathode pad chambers, v) two trigger stations, each equipped with two planes of resistive plate chambers and vi) an iron wall of 7.2 $\lambda_I$ placed between the tracking and trigger systems. The following detectors are also involved in the analysis. The Silicon Pixel Detector (SPD), which constitutes the two innermost layers of the Inner Tracking System (with pseudo-rapidity coverage $|\eta_{lab}| < 2$ and $|\eta_{lab}| < 1.4$ for the inner and outer layer, respectively), is used for reconstructing the position of the collision point. Two scintillator arrays (V0) placed on each side of the IP (with pseudo-rapidity coverage $2 < \eta_{lab} < 5.1$ and $-3.7 < \eta_{lab} < -1.7$) are used for triggering purposes and to reject offline beam-induced background events. The V0 as well as the two T0 arrays, made of quartz Cherenkov counters and covering the acceptance $4.6 < \eta_{lab} < 4.9$ and $-3.3 < \eta_{lab} < -3.0$, are employed to determine the luminosity. The Zero Degree Calorimeters (ZDC) located at 112.5 m on both sides of the IP are also used in the offline event selection.

The results presented in this Letter are based on the data samples recorded by ALICE during the 2013 p–Pb run. Due to the different energy per nucleon of the colliding beams ($E_p = 4$ TeV, $E_{Pb} = 1.58$ TeV), the centre-of-mass of the nucleon–nucleon collisions is shifted in rapidity by $\Delta y = 0.465$ with respect to the laboratory frame in the direction of the proton beam. Data were collected with two beam configurations by reversing the rotation direction of the p and Pb beams. This allowed us to measure muon production in the rapidity intervals 2.03 < $y_{cm}$ < 3.53 and $4.46 < y_{cm} < -2.96$, the positive rapidities corresponding to the proton beam traveling in the direction of the muon spectrometer (p–Pb configuration) and the negative rapidities to the opposite case (Pb–p configuration).

The data samples used for the analysis consist of muon-triggered events, requiring in addition to the minimum bias (MB) trigger condition the presence of one candidate track with a $p_T$ above a threshold value in the muon trigger system. The MB trigger is formed by a coincidence between signals in the two V0 arrays (> 99% efficiency for the selection of non-single-diffractive collisions). Data were collected using two different trigger $p_T$ thresholds, of about 0.5 GeV/$c$ and 4.2 GeV/$c$, defined as the $p_T$ value for which the muon trigger probability is 50%. In the following, the low- and high-$p_T$ trigger threshold samples are referred to as MSL and MSH, respectively. The beam-induced background events were removed by using the timing information from the V0 arrays. Collisions outside the nominal timing of the LHC bunches were rejected using the information from the ZDC. The maximum instantaneous luminosity at the ALICE IP during data-taking was $10^{29}$ Hz·cm$^{-2}$, and the probability for multiple interactions in a bunch crossing (pile-up) was at most 2%. The integrated luminosities for the used data samples are $196 \pm 7 \mu b^{-1} (4.9 \cdot 10^3 \pm 0.2 \cdot 10^3 \mu b^{-1})$ in the p–Pb configuration and $254 \pm 9 \mu b^{-1} (5.8 \cdot 10^3 \pm 0.2 \cdot 10^3 \mu b^{-1})$ in the Pb–p configuration for MSL–MSH (MSH)–triggered events. The calculation of the integrated luminosities and associated uncertainties is discussed in Section 3.

3. Data analysis

3.1. Muon candidate selection

The offline selection criteria of muon candidates are similar to those described in [4,5]. Tracks were required to be reconstructed
in the kinematic region $-4 < \eta_{lab} < -2.5$ and $170^\circ < \phi_{lab} < 178^\circ$ ($\eta_{lab}$ is the polar angle at the end of the absorber). In addition, tracks in the tracking system were required to match track segments in the trigger system. This results in a very effective rejection of the hadronic background that is absorbed in the iron wall. A selection on the Distance of Closest Approach (DCA) to the primary vertex of each track weighted with its momentum ($p$) was also applied. The maximum value is set to $6\sigma_{\text{DCA}}$, where $\sigma_{\text{DCA}}$ is the resolution on this quantity. This latter further reduces the contribution from fake tracks coming from the association of uncorrelated clusters in the tracking chambers and beam-induced background tracks. The measurement of muons from heavy-flavour hadron decays is performed in the interval $2 < p_T < 16$ GeV/c by combining MSL-triggered and MSH-triggered events. The former are used up to $p_T = 7$ GeV/c, the latter at higher $p_T$. The large yield of muons from secondary light-hadron decays produced inside the front absorber prevents the measurement below $p_T = 2$ GeV/c. In the $p_T$ interval of the measurement, the background contribution consists mainly of muons from decays of primary charged pions and charged kaons produced at the interaction point. The component of muons from $J/\psi$ decays, found to be less than 1–3% of the inclusive muon yield, depending on rapidity and $p_T$, was not subtracted. Moreover, the background contribution of muons from $W$ and $Z$/$\gamma^*$ is also small in the $p_T$ interval of interest [56] (less than 2–3% at $p_T = 16$ GeV/c).

3.2 Analysis strategy

Nuclear matter effects on the production of muons from heavy-flavour hadron decays can be quantified by means of the nuclear modification factor, $R_{p^A/Pb}^{\mu^+ \rightarrow \text{HF}}$, which can be written as:

$$R_{p^A/Pb}^{\mu^+ \rightarrow \text{HF}}(p_T) = \frac{1}{A} \frac{d\sigma_{p^A/Pb}^{\mu^+ \rightarrow \text{HF}}/dp_T}{d\sigma_{pp}^{\mu^+ \rightarrow \text{HF}}/dp_T},$$

(1)

where $A$ is the mass number of the Pb nucleus, $d\sigma_{p^A/Pb}^{\mu^+ \rightarrow \text{HF}}/dp_T$ and $d\sigma_{pp}^{\mu^+ \rightarrow \text{HF}}/dp_T$ are the $p_T$-differential production cross sections of muons from heavy-flavour hadron decays in pp and p–Pb collisions, respectively.

The latter is evaluated as:

$$\frac{d\sigma_{pp}^{\mu^+ \rightarrow \text{HF}}}{dp_T} = \left( \frac{dN^{\mu^+}_{pp}/dp_T}{dN^{\mu^+}_{\text{rec}}/dp_T} \right) \cdot \frac{1}{L_{\text{int}}},$$

(2)

where $dN^{\mu^+}/dp_T$ and $dN^{\mu^+}_{\text{rec}}/dp_T$ are the $p_T$-differential yields of inclusive muons and of muons from charged-pion and charged-kaon decays, respectively. The integrated luminosity $L_{\text{int}}$ is computed as $N_{MB}/\sigma_{MB}$, where $N_{MB}$ and $\sigma_{MB}$ are the number of MB collisions and the MB trigger cross section, respectively. The latter was measured in van der Meer scans and is $2.09 \pm 0.07$ b (2.12 $\pm$ 0.07 b) for the p–Pb (Pb–p) configuration [57]. Since the analysis is based on muon-triggered events, the number of equivalent MB events is evaluated as $N_{MB} = F_{\text{MSL(MSH)}} \cdot N_{\text{MSL(MSH)}}$, where $N_{\text{MSL(MSH)}}$ is the number of analysed MSL- (MSH-) triggered events, and $F_{\text{MSL(MSH)}}$ is a normalisation factor. The number of MSL- and MSH-triggered events amounts to $1.45 \cdot 10^7$ (2.63 $\cdot$ 10$^7$) and $10^7$ (1.53 $\cdot$ 10$^7$) for the p–Pb (Pb–p) samples, respectively. The normalisation factor is determined with two different procedures described hereafter. The first procedure is based on the offline selection of muon-triggered events in the MB data sample. In this approach, $F_{\text{MSL}}$ is the inverse of the probability of meeting the MSL trigger condition in an MB event. The normalisation factor $F_{\text{MSH}}$ is obtained as the inverse of the product of the probability of meeting the MSH trigger condition in a MSL event and that of meeting the MSL trigger condition in a MB event. The second procedure is based on the run-averaged ratio of the MB trigger rate to that of muon triggers (MSL or MSH), each corrected by the fraction of events passing the event-selection criteria. Note that in both procedures, the number of MB events is corrected for pile-up. Finally, the weighted average of the results obtained with the two approaches is computed, using the statistical uncertainty as weight. The results are $F_{\text{MSL}} = 28.20 \pm 0.08$ (20.50 $\pm$ 0.04) and $F_{\text{MSH}} = 1032.8 \pm 7.2$ (798.3 $\pm$ 4.8) at forward (backward) rapidity. The quoted uncertainties are statistical.

The measured $p_T$-differential muon yield is corrected for acceptance and for the tracking and trigger efficiencies using the same procedure as for the analysis of pp collisions at $\sqrt{s} = 2.76$ and 7 TeV [4,5]. This procedure is based on a Monte Carlo simulation using as input the $p_T$ and rapidity distributions of muons from beauty-hadron decays predicted by Fixed Order Next To Leading Log (FONLL) calculations [58,1]. The detector description and its response are modelled using the GEANT3 transport package [59] taking into account the time evolution of the detector configuration. For $p_T > 2$ GeV/c, the product of acceptance and efficiency in MSL-triggered events tends to saturate at a value close to 85% and 75% at forward (p–Pb configuration) and backward rapidity (Pb–p configuration), respectively. The lower value obtained for the Pb–p system is mainly due to a lower efficiency of the tracking chambers in the corresponding data taking period. The MSH trigger efficiency plateau is only just reached at $p_T = 16$ GeV/c, which leads to values of the acceptance times efficiency slightly lower than those obtained for the MSL trigger, even in the high $p_T$ region.

The subtraction of background muons from charged-pion and charged-kaon decays is based on a data-tuned Monte Carlo cocktail. First, the contribution of muons from charged-pion and charged-kaon decays in $2.03 < y_{\text{cms}} < 3.53$ is estimated by extrapolating to forward rapidity the $p_T$-differential yields per minimum-bias event of charged pions and kaons measured by the ALICE Collaboration in the rapidity region $-0.3 < y_{\text{cms}} < 0.3$ for $p_T$ values up to $p_T = 20$ GeV/c [60]. A further $p_T$ extrapolation, by means of a power-law fit, was performed to extend the $p_T$ coverage to the charged-pion and charged-kaon momentum range, which is relevant to estimate the contribution of muons from charged-pion and charged-kaon decays up to $p_T = 16$ GeV/c.

The rapidity extrapolation of the $d^2N^{\pi^+, K^+}/dp_T dy_{\text{mid–y_{cms}}}$ mid-rapidity charged-pion and charged-kaon yields to forward rapidity is performed according to:

$$d^2N^{\pi^+, K^+}/dp_T dy_{\text{mid–y_{cms}}},$$

(3)

where the $p_T$- and $y$-dependent extrapolation factor $F_{\text{extrap}}(p_T, y)$ is obtained by means of the DPMJET event generator [61], which describes the pseudo-rapidity distribution of charged particles in $-2 < \eta_{lab} < 2$ reasonably well [62]. The HIJING 2.1 generator [63] is employed to estimate the systematic uncertainty (Section 3.3). It was also checked that compatible results are obtained with the AMPT model [64]. Then, the $(p_T, y)$ distributions of muons from charged-pion and charged-kaon decays in the acceptance of the muon spectrometer are generated with a simulation, using as input the charged-pion and charged-kaon distributions obtained with the extrapolation procedure described above. The absorber effect is accounted for by rejecting charged pions and charged kaons that do

1 The sensitivity of the product of acceptance and efficiency on the input distributions was estimated by comparing the results with those from a simulation using muons from charm decays. The differences are negligible (less than 1%).
not decay within a distance corresponding to one hadronic interaction length in the absorber. The charged-pion and charged-kaon distributions at backward rapidity, for \(-4.46 < y_{\text{cms}} < -2.96\), are estimated by using the distributions extrapolated at forward rapidity with DPMJET as a starting point, as discussed above. These \(p_T\) and \(y\) distributions are scaled by the \(p_T\)-dependent charged-particle asymmetry factor measured by the CMS Collaboration for \(1.3 < |\eta_{\text{cms}}| < 1.8\) [65]. The systematic uncertainty resulting from the different rapidity coverage is discussed in Section 3.3. Finally, the distributions of muons from charged-pion and charged-kaon decays at backward rapidity are obtained with the fast simulation procedure described above for the forward rapidity region. The obtained yields per event of muons from charged-pion and charged-kaon decays at forward and backward rapidities are then scaled by \(N_{\text{MB}}\) and subtracted from the inclusive muon yields.

The relative contribution to the inclusive muon yield due to muons from charged-pion and charged-kaon decays decreases with increasing \(p_T\) from about 27% (35%) at \(p_T = 2\) GeV/c to 2% (2%) at \(p_T = 16\) GeV/c at forward (backward) rapidity. In the smaller overlapping acceptance \(2.96 < |y_{\text{cms}}| < 3.53\) used for the measurement of the forward-to-backward ratio \(R_{\text{FB}}^{\mu^\pm-e^{-}\text{HF}}\), the background fraction decreases from about 19% (41%) at \(p_T = 2\) GeV/c to 1% (3%) at \(p_T = 16\) GeV/c at forward (backward) rapidity.

The \(p_T\)-differential cross sections of muons from heavy-flavour hadron decays in pp collisions at \(\sqrt{s} = 5.02\) TeV, needed for the computation of \(R_{\text{FB}}\) at forward and backward rapidity, are obtained by applying a pQCD-driven energy and rapidity scaling to the measured \(p_T\)-differential cross sections in pp collisions at \(\sqrt{s} = 7\) TeV in the kinematic region \(2.5 < y_{\text{cms}} < 4.0\) and \(2 < p_T < 12\) GeV/c [4]. The scaling factor and its uncertainty are evaluated using FONLL calculations [58] with different sets of factorisation and renormalisation scales and quark masses, as detailed in [66]. The current measurement of the pp \(p_T\)-differential cross section at \(\sqrt{s} = 7\) TeV is limited to \(p_T < 12\) GeV/c. Therefore, the \(p_T\)-differential cross sections in \(12 < p_T < 16\) GeV/c at \(\sqrt{s} = 5.02\) TeV are obtained from FONLL calculations at \(\sqrt{s} = 5.02\) TeV, rescaled to match the result of the data-driven procedure in \(6 < p_T < 12\) GeV/c. Note that in the limited interval \(2 < p_T < 10\) GeV/c, the \(p_T\)-differential cross section of muons from heavy-flavour hadron decays was also measured in pp collisions at \(\sqrt{s} = 2.76\) TeV. As a cross-check, it was verified that without using this measurement in the procedure for scaling to \(\sqrt{s} = 5.02\) TeV, compatible results are obtained with respect to those from the \(\sqrt{s} = 7\) TeV case, although with larger uncertainties.

The forward-to-backward ratio, \(R_{\text{FB}}^{\mu^\pm-e^{-}\text{HF}}\), defined as the ratio of the cross section of muons from heavy-flavour hadron decays at forward rapidity to that at backward rapidity in a rapidity interval symmetric with respect to \(y_{\text{cms}} = 0\),

\[
R_{\text{FB}}^{\mu^\pm-e^{-}\text{HF}}(p_T) = \frac{[d\sigma_{p\text{Pb}}^{\mu^\pm-e^{-}\text{HF}}/dp_T]_{|y_{\text{cms}}| < 2.96, y_{\text{cms}} < 3.53}}{[d\sigma_{p\text{Pb}}^{\mu^\pm-e^{-}\text{HF}}/dp_T]_{|y_{\text{cms}}| < 3.53, y_{\text{cms}} < -2.96}},
\]

is also a sensitive observable for the study of CNM effects. This ratio can be computed only in the restricted overlapping region \(2.96 < |y_{\text{cms}}| < 3.53\) covered at both forward and backward rapidity.

### 3.3. Systematic uncertainties

The measurement of the \(p_T\)-differential cross sections of muons from heavy-flavour hadron decays is affected by systematic uncertainties of the inclusive muon yield, the background subtraction and the determination of the integrated luminosity. For the nuclear modification factor, also the systematic uncertainty on the pp reference cross section must be considered.

The systematic uncertainty affecting the yield of inclusive muons contains the 2% (3%) systematic uncertainty on the muon tracking efficiency at forward (backward) rapidity [67,68] and the systematic uncertainty associated with the muon trigger efficiency of 1% with the MSL trigger and 4% with the MSH trigger. A detailed description of the procedure used to evaluate these uncertainties is found in [55,67,68]. A 0.5% systematic uncertainty due to the efficiency of the matching between tracking and trigger information is also added. A conservative \(p_T\)-dependent systematic uncertainty of 0.5% · \(p_T\) (in GeV/c) is assigned to take into account the difference between the true (unknown) residual mis-alignment of the spectrometer and the simulated one.

The systematic uncertainty of the estimate of the yield of muons from charged-pion and charged-kaon decays contains contributions from the uncertainty on i) the measured mid-rapidity \(p_T\) distributions of charged pions and kaons and their \(p_T\) extrapolation, of 5–8%, ii) the rapidity extrapolation, of 7–26% (2–27%) at forward (backward) rapidity, depending on \(p_T\), estimated by comparing the results from DPMJET and HIJING generators and iii) the absorber effect, of 15%, obtained by varying the interaction length in the absorber within reasonable limits. At backward rapidity, in addition to previous systematic uncertainties a systematic uncertainty arises from the procedure that makes use of the asymmetry factor measured by the CMS Collaboration [65] in different rapidity intervals with respect to our measurement. This uncertainty, about 15–18%, is calculated by varying the asymmetry factor between unity and two times the measured value for charged particles. An additional 15% uncertainty is included to account for the variations with \(p_T\) of the measured asymmetry factor with respect to a uniform distribution in the high \(p_T\) region. All the aforementioned uncertainties are added in quadrature to obtain the total uncertainty on the background subtraction, which results in an uncertainty on the \(p_T\)-differential cross section and nuclear modification factor of muons from heavy-flavour hadron decays of 1–7% (1–15%) at forward (backward) rapidity (Table 1).

The systematic uncertainty of the measurement of the integrated luminosity includes contributions from \(\sigma_{\text{MB}}\) and \(N_{\text{MB}}\). The systematic uncertainty of \(N_{\text{MB}}\) of about 1% reflects the difference between the normalisation factor \(F_{\text{MSL/MSH}}\) values obtained with the two different procedures described in Section 3.2. The systematic uncertainty of \(\sigma_{\text{MB}}\) amounts to 3.5% (3.2%) for the p–Pb (Pb–Pb) configuration, with a total correlated uncertainty between these

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\footnote{This results from larger uncertainties and a larger energy gap at \(\sqrt{s} = 2.76\) TeV compared to \(\sqrt{s} = 7\) TeV.}

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### Table 1

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<th>Source</th>
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<td>1% (4%) for MSL (MSH)</td>
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<td>0.5%</td>
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<td>0.5% · (p_T)</td>
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<tr>
<td>Background subtraction</td>
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<td>1–15%</td>
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<td>3.5%</td>
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<tr>
<td>(\sigma_{\mu^\pm-e^{-}\text{HF}}) ((p_T)-dependent)</td>
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<td>9–30%</td>
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<td>(\sigma_{\mu^\pm-e^{-}}) (global)</td>
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<td>3.5%</td>
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</tbody>
</table>
two configurations of 1.6%. The luminosity measurement was performed independently by using a second reference cross section, based on particle detection by the T0 detector [57]. The luminosities measured with the two detectors differ by at most 1% throughout the whole data-taking period. This value is combined quadratically with the systematic uncertainties on σ_{MB} and σ_{NB}, leading to a total uncertainty on the integrated luminosity of 3.8% (3.5%) for the p–Pb (Pb–p) configuration.

The systematic uncertainty of the pp reference at √s = 5.02 TeV accounts for the uncertainties of i) the measurement of the pT-differential cross section of muons from heavy-flavour hadron decays at √s = 7 TeV, of 8–14%, plus a global uncertainty of 3.5% from the luminosity measurement [69] quoted separately, ii) the energy scaling factor, obtained by considering different sets of factorisation and renormalisation scales and quark masses in FONLL as detailed in [66], of 3% (7%) at pT = 2 GeV/c and 2% (4%) at pT = 12 GeV/c at forward (backward) rapidity, iii) the procedure based on FONLL predictions for 12 < pT < 16 GeV/c, of 26% (30%) at forward (backward) rapidity, and iv) the rapidity extrapolation. The uncertainty on the latter amounts to 2% at forward rapidity and is negligible at backward rapidity. It is estimated from the pp cross sections at √s = 7 TeV measured in the full acceptance and in various rapidity sub-intervals [4]. These rapidity sub-intervals are combined in order to mimic the rapidity intervals investigated in the p–Pb and Pb–p configurations (Section 2), scaled with FONLL to the full rapidity coverage and compared with the measurement.

A summary of the systematic uncertainties sources previously discussed, after propagation to the measurements of dσ_{pPb}^{μ^±-HF}/dpT and dσ_{pp}^{μ^±-HF}/dpT, is presented in Table 1. The main contribution to the R_{pPb}^{μ^±-HF} systematic uncertainty comes from the pp reference, in particular in the high pT region (pT > 12 GeV/c). Most of the systematic uncertainties are uncorrelated as a function of pT, with the exception of the systematic uncertainties of mis-alignment in pp and p–Pb collisions which are correlated bin-to-bin in pT, of the detector response which is partially correlated, and of the luminosity which is fully correlated. The total systematic uncertainty on R_{pPb}^{μ^±-HF} varies within about 12–28% (18–31%) at forward (backward) rapidity.

All systematic uncertainties entering the dσ_{pPb}^{μ^±-HF}/dpT measurement at forward and backward rapidity affect the R_{FB}^{μ^±-HF} measurement, with the exception of the 1.6% contribution from the uncertainty on the luminosity, which is fully correlated between the results at forward and backward rapidity. The main contribution to the R_{FB}^{μ^±-HF} systematic uncertainty comes from the muon background at low pT (pT < 4 GeV/c) as well as the detector response and mis-alignment in the high-pT region. The total systematic uncertainty on R_{FB}^{μ^±-HF} decreases with increasing pT, from about 20% (pT = 2 GeV/c) to 10% (pT = 16 GeV/c).

4. Results and comparison to model predictions

The pT-differential cross sections of muons from heavy-flavour hadron decays measured in p–Pb collisions at √S_{NN} = 5.02 TeV at forward rapidity (2.03 < y_{cms} < 3.53) and backward rapidity (−4.46 < y_{cms} < −2.96) in the interval 2 < pT < 16 GeV/c are displayed in Fig. 1. They are further used to compute the nuclear modification factor R_{pPb}. Vertical bars represent the statistical uncertainties and empty boxes, smaller than the symbols, the systematic uncertainties that include all sources discussed in Section 3, except the normalisation uncertainties. These conventions related to the drawing of uncertainties apply also to the figures discussed in the following.

![Production cross sections of muons from heavy-flavour hadron decays as a function of pT](image-url)
describes the measurement fairly well over the whole \( p_T \) range. The same model is able to describe both the \( p_T \)-differential \( R_{\text{pPb}} \) of electrons from heavy-flavour hadron decays measured at mid-rapidity with ALICE, which is also consistent with unity within uncertainties [51], and the enhancement seen at backward rapidity in d-Au collisions at \( \sqrt{s_{NN}} = 200 \) GeV for muons from heavy-flavour hadron decays [72].

Theoretical calculations based on the Colour Glass Condensate model [74] predict that for the rapidity interval \( 2.5 < y_{\text{cm}} < 3.53 \), the \( R_{\text{pPb}} \) of muons from charm-hadron decays for the interval \( 0 < p_T < 4 \) GeV/c increases with increasing \( p_T \) from about 0.6 to 0.85. This predicted \( R_{\text{pPb}} \) is slightly smaller than that reported here for muons from heavy-flavour hadron decays, although for a slightly different rapidity interval.

The \( p_T \)-differential nuclear modification factors of muons from heavy-flavour hadron decays were also studied as a function of rapidity, by dividing each of the two intervals in two sub-intervals. The results are presented in Fig. 3. In both the forward (top panel) and backward (bottom panel) rapidity regions, no significant difference is observed between the nuclear modification factors measured in the two rapidity sub-intervals.\(^3\)

**Fig. 2.** Nuclear modification factor of muons from heavy-flavour hadron decays as a function of \( p_T \) for p-Pb collisions at \( \sqrt{s_{NN}} = 5.02 \) TeV at forward rapidity (2.03 < \( y_{\text{cm}} \) < 3.53, top) and backward rapidity (−4.46 < \( y_{\text{cm}} \) < −2.96, bottom) compared to model predictions [70–72]. Statistical uncertainties (bars), systematic uncertainties (open boxes), and normalisation uncertainties (filled box at \( p_T^{\mu} = 1 \) GeV/c) are shown. Filled (open) symbols refer to the pp reference obtained from an energy and rapidity scaling to the measurement at \( \sqrt{s} = 7 \) TeV (an extrapolation based on FONLL calculations).

**Fig. 3.** Nuclear modification factors of muons from heavy-flavour hadron decays as a function of \( p_T \) for p-Pb collisions at \( \sqrt{s_{NN}} = 5.02 \) TeV in two rapidity sub-intervals at forward (top) and backward (bottom) rapidity. Statistical uncertainties (bars), systematic uncertainties (open boxes), and normalisation uncertainties (filled box at \( R_{\text{pPb}}^{\mu} = 1 \) are shown. For visibility, the points for the rapidity intervals 2.79 < \( y_{\text{cm}} \) < 3.53 and −3.71 < \( y_{\text{cm}} \) < −2.96 are slightly shifted horizontally. Filled (open) symbols refer to the pp reference obtained from an energy and rapidity scaling to the measurement at \( \sqrt{s} = 7 \) TeV (an extrapolation based on FONLL calculations).

\(^3\) For the interval 0 < \( p_T < 4 \) GeV/c the component of muons from charm-hadron decays dominates according to FONLL calculations [58].

\(^4\) It cannot be excluded that a degree of correlation between the two rapidity sub-intervals, difficult to quantify, is present in the various systematic uncertainty sources.

5. Conclusion

In summary, the production of muons from heavy-flavour hadron decays has been measured in p-Pb collisions at \( \sqrt{s_{NN}} = 5.02 \) TeV for 2 < \( p_T < 16 \) GeV/c with the ALICE detector at the
CERN LHC. Measurements of the production cross sections and nuclear modification factors have been presented as a function of $p_T$ at forward ($2.03 < y_{cm} < 3.53$, p-going direction) and backward ($-4.46 < y_{cm} < -2.96$, Pb-going direction) rapidity. Moreover, the $p_T$-differential forward-to-backward ratio has been also studied in the smaller overlapping interval $2.96 < |y_{cm}| < 3.53$. At forward rapidity, the nuclear modification factor is compatible with unity over the whole $p_T$ range. At backward rapidity, a deviation from binary scaling is suggested in the interval $2.5 < p_T < 3.5$ GeV/c with a significance of about 2σ. The observed trends in the $R_{p\text{-}p\text{b}}^{p\text{HF}}$ measurements are reflected in the forward-to-backward ratio, which shows a clear tendency to be below unity, with a deviation of 3.7σ for $2.5 < p_T < 3.5$ GeV/c. The measured nuclear modification factors and the forward-to-backward ratio are reproduced within uncertainties by NLO pQCD calculations including nuclear modification of the PDFs. The nuclear modification factor at forward rapidity is in agreement with a model calculation including CNM effects based on a nuclear shadowing scenario, $k_T$ broadening and energy loss in cold nuclear matter. The data at backward rapidity are also reproduced by a model including incoherent multiple scattering effects. The results indicate that the suppression of the production of high-$p_T$ muons from heavy-flavour hadron decays in the 0–10% most central Pb–Pb collisions measured by ALICE is due to final-state effects induced by the hot and dense medium formed in these collisions.

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